## GCSE <br> STATISTICS <br> 8382/1H

HIGHER TIER PAPER 1
Mark scheme
2019
V1.0

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.
It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Principal Examiners have prepared these mark schemes for specimen papers. These mark schemes have not, therefore, been through the normal process of standardising that would take place for live papers.

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| M | Method marks are awarded for a correct method which could lead to a correct answer. |
| :---: | :---: |
| A | Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied. |
| B | Marks awarded independent of method. |
| ft | Follow through marks. Marks awarded for correct working following a mistake in an earlier step. |
| SC | Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth. |
| M dep | A method mark dependent on a previous method mark being awarded. |
| B dep | A mark that can only be awarded if a previous independent mark has been awarded. |
| oe | Or equivalent. Accept answers that are equivalent. eg accept 0.5 as well as $\frac{1}{2}$ |
| [a, b] | Accept values between $a$ and $b$ inclusive. |
| 3.14... | Allow answers which begin 3.14 eg 3.14, 3.142, 3.1416 |
| Use of brackets | It is not necessary to see the bracketed work to award the marks. |

Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

## Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

Questions which do not ask students to show working
As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

## Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

## Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then $M$ marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1}$ | 6 | B1 | Any indication |
| :--- | :--- | :--- | :--- |


| $\mathbf{2}$ | 95 | B1 | Any indication |
| :--- | :--- | :--- | :--- |


| 3 | $\frac{1}{36}$ | B1 | Any indication |
| :---: | :---: | :---: | :--- |


| $\mathbf{4}$ | -1 | B1 | Any indication |
| :--- | :--- | :--- | :--- |


| 5(a) | Carry out a check that values are <br> consistent i.e. within the possible <br> values for a $\%$ and/or are similar to <br> other values in the table. | B1 | oe |
| :--- | :--- | :--- | :--- |


| 5(b) | 115 circled and 15 stated | B1 | oe |
| :--- | :--- | :--- | :--- |


| 5(c) | It decreased (in 2009) and then <br> increased (every year) | B1 |  |  |
| :---: | :--- | :---: | :--- | :--- |
|  | Additional Guidance |  |  |  |
|  |  |  |  |  |


| Q Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |


| 5(d) | 0.08 or 84.1 (million) | M1 | for 0.08 accept $0.075-0.085$ <br> for 84.1 accept $84.05-84.15$ (million) |
| :---: | :---: | :---: | :---: |
|  | $0.08 \times 84.1$ (million) | M1dep | using their values in range |
|  | 6.728 (million) | A1 | $6.30375-7.15275$ (million) |
|  | 6.3-7.2 (million) (to 2 sf ) | B1ft | ft their answer rounded to the nearest 100,000 |
|  | Additional Guidance |  |  |


| 6(a) | 0.3 | B1 | oe |
| :--- | :--- | :--- | :--- |


| 6(b) | their $0.3 \times$ their 0.3 | M1 | ft their part (a) only if it's between 0 and 1 exclusive |
| :---: | :---: | :---: | :---: |
|  | 0.09 | A1ft | oe |
|  |  |  | ft their part (a) only if it's between 0 and 1 exclusive |
|  |  |  | SC1 0.9 |
|  | Additional Guidance |  |  |


| 6(c) | $1-0.3-0.18$ | M1 | oe |  |
| :--- | :--- | :---: | :--- | :--- |
|  | 0.52 | A1 | oe |  |
|  | Additional Guidance |  |  |  |
|  |  |  |  |  |


| 6(d) | No, we don't know the probability of <br> if being windy if it's raining | B1 | oe we do not know whether rain and <br> wind are independent |  |
| :---: | :--- | :---: | :---: | :---: |
|  | Additional Guidance |  |  |  |


| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 7(a) | $132 / 12$ | M1 |  |  |  |
| :--- | :--- | :---: | :--- | :---: | :---: |
|  | 11 | A1 |  |  |  |
| $\sqrt{1560 / 12}-\left(\right.$ their $\left.11^{2}\right)$ | M1 |  |  |  |  |
|  | 3 | A1 ft |  |  |  |
|  | Additional Guidance |  |  |  |  |


| 7(b) | $500+$ (their 11 )(100) ( = 1600) | M1 |  |
| :--- | :--- | :---: | :--- |
|  | Their $1600 \div 16$ | A1 ft |  |
|  | Den is right | B1ft | If M1 awarded |
|  | Additional Guidance |  |  |
|  |  |  |  |


| 7(c) | On average Den earns more | B1 ft |  |  |
| :--- | :--- | :---: | :--- | :--- |
|  | Peter has less variation in earnings | B1 ft |  |  |
| Additional Guidance |  |  |  |  |
|  |  |  |  |  |


| 7(d) | Ticked Yes and appropriate as no <br> apparent extreme values <br> or <br> appropriate as all values used in <br> calculation | B1 | oe |  |
| :--- | :--- | :--- | :--- | :--- |
|  | Additional Guidance |  |  |  |


| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 8 | All three sampling methods correctly <br> named | B3 | A - Quota <br> B - Systematic <br> C - Random <br> B2 - two methods named correctly <br> B1 - one method named correctly |
| :--- | :--- | :---: | :--- | :--- |
|  | In A every gym is represented <br> whereas in B and C this might not <br> be the case. | M1 | oe |
| In C every trainer has an equal <br> chance of being selected which is <br> not true of A and B | M1 | oe |  |
| B is somewhat easier to carry out <br> than C (A depends on the choice of <br> selection chosen by the <br> management) | M1 | oe |  |
| Reasoned choice of one of the <br> methods | A1 |  |  |


| Q | Answer | Mark | Comments |  |
| :---: | :---: | :---: | :---: | :---: |
| 9(a) | Same price | Additional Guidance |  |  |
|  |  |  |  |  |
|  |  |  |  |  |


| 9(b)(i) | Use of $n=9$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $6 \times \frac{24.5}{720}(=0.2042)$ | M1ft |  |
|  | 1 - their 0.2042 | M1 |  |
|  | [0.7958, 0.8] | A1 | Answer only (achieved on calculator) to be awarded 4 marks |
|  | Additional Guidance |  |  |


| 9(b)(ii) | (High) positive <br> agreement/association between <br> number of pages and retail price | B1 | As the number of pages increase so <br> does the retail price of the book |  |
| :--- | :--- | :---: | :--- | :---: |
|  | Additional Guidance |  |  |  |
|  |  |  |  |  |


| 9(c)(i) | Each additional page increases the <br> price by 2 p | B2 | oe <br> Per page increase in price B1 |  |
| :--- | :--- | :---: | :--- | :---: |
|  | Additional Guidance |  |  |  |
|  |  |  |  |  |


| 9(c)(ii) | $y=0.02 \times 765+1.35$ or 16.65 <br> and their $16.65-10.30$ or 6.35 | M1 | $1^{\text {st }}$ mark |
| :---: | :--- | :---: | :--- |
|  | $x=$ their $\frac{6.35-1.35}{0.02}$ | M1dep | $2^{\text {nd }}$ mark |
|  | 250 | A1 | $3^{\text {rd }}$ mark |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 10(a) | The birth rate is higher than the <br> death rate (so more are being born <br> in the town than are dying in the <br> town) | B1 | oe |  |
| :--- | :--- | :--- | :--- | :--- |
|  | Additional Guidance |  |  |  |
|  |  |  |  |  |


| 10(b) | More people might have moved out <br> of the town (than the extra born) | B1 | oe |  |
| :--- | :--- | :--- | :--- | :--- |
|  | Additional Guidance |  |  |  |
|  |  |  |  |  |


| 11 | Attempt to find a median | M1 | May be on graph |
| :---: | :---: | :---: | :---: |
|  | Both medians correct | A1 | $\begin{aligned} & 9 \text { am median }[3.9,4.1] \\ & 2 \mathrm{pm} \text { median }[6.9,7.1] \end{aligned}$ |
|  | Attempt to find an IQR | M1 | May be on graph |
|  | Both IQRs correct | A1 | $\begin{aligned} & 9 \mathrm{am} \operatorname{IQR}[1.9,2.1] \\ & 2 \mathrm{pm} \operatorname{IQR}[3.8,4.0] \end{aligned}$ |
|  | Correct comparison of medians, e.g. the birds have a greater average mass at 2 pm than at 9 am | B1ft | In context <br> ft their medians |
|  | Correct comparison of IQRs eg the birds' masses are more widely spread at 2 pm than at 9 am | B1ft | In context <br> ft their IQRs |
|  | Additional Guidance |  |  |
|  | Beware - the 2pm IQR is approximately the same as the LQ |  |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 12(a) | $\left(\mathrm{r}^{2} / 4^{2}\right)=76468 / 54620$ | M1 | $\sqrt{76468 / 54620}$ |
|  | $\mathrm{r}^{2}=22.4$ | M1 | $r / 4=\sqrt{1.4}$ |
|  | $\mathrm{r}=4.7329$ | A1 |  |
|  | $r=4.73$ | B1 ft | Any value to 3 significant figures |
|  | Additional Guidance |  |  |


| 12(b) | $(126 / 360)$ | M1 |  |  |
| :--- | :--- | :---: | :--- | :--- |
|  | $\times 54620$ | M1 |  |  |
|  | 19117 | A1 |  |  |
|  | Additional Guidance |  |  |  |
|  |  |  |  |  |


| 13(a) | Attempt at bell-shaped curve | B1 | With approximate symmetry |
| :---: | :--- | :---: | :--- |
|  | Curve centred at $[33,37]$ | B1 |  |
|  | Curve shows knowledge of $+/-3$ <br> standard deviations | B1 | Curve goes from approximately <br> 5 to 65 |
|  | Additional Guidance |  |  |
|  |  |  |  |


| 13(b) | Mean (40) clearly to the right of the <br> middle of the area (median) under <br> the curve | B1 | Any general shape as long as meets <br> the criteria for positive skew |  |
| :--- | :--- | :---: | :---: | :---: |
|  | Long positive tail indicating skew ie <br> 40 to max at least 1.5 times min to <br> 40 | B1 |  |  |
|  | Additional Guidance |  |  |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 14(a) | Any valid hypothesis relating to the distance thrown | B1 | eg The competitors throw further in the 2008 qualifying round (than in the 2012 qualifying round). <br> eg The competitors throw further in the 2012 qualifying round (than in the 2008 qualifying round). <br> eg There is no difference between the distances thrown in 2008 and 2012, etc |
|  | Additional guidance |  |  |


| 14(b) | Data are continuous | B1 |  |
| :--- | :--- | :---: | :---: |
|  | Additional guidance |  |  |
|  |  |  |  |


| 14(c) | Any valid reason | B1 | eg Reduces the number of rectangles <br> where frequency densities are low. <br> eg Greater number of rectangles <br> where frequency densities are high <br> allowing more detail to be seen |
| :--- | :--- | :---: | :---: |
|  | Additional guidance |  |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 14(d) | Sensible unequal classes covering the full range | B2 | B1 Sensible unequal classes covering the whole range with one error (which may be repeated) |
| :---: | :---: | :---: | :---: |
|  | Justification for their choice of unequal classes | B1 | eg looking at close distribution of throws in the middle |
|  | Correct frequencies for their classes | B1 ft | ft their classes |
|  | Axes drawn with correct scales and labels | B1 |  |
|  | Frequency densities attempted for their classes and frequencies | M1 | Equal or unequal classes |
|  | All frequency densities correct for their frequencies and unequal classes | A1 ft | only if unequal classes |
|  | Rectangles all drawn accurately. | A1 ft | ft their frequency densities, unequal classes |
|  | Additional guidance |  |  |
|  | Note For equal classes, maximum score is B0 B0 B1ft B1 M1 A0 A0ft 3 marks out of 8 |  |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| Full interpretation of the two <br> histograms in context, both of which <br> are clearly linked to the hypothesis <br> in part (a) | B4 | B3Two features from the histogram <br> only one of which is linked to the <br> hypothesis. <br> B2One feature of the histogram <br> interpreted in context which is <br> clearly linked to the hypothesis. <br> B1One feature of the histogram <br> interpreted in context <br> or <br> A reference to the greatest distance <br> or least distance thrown which is <br> clearly linked to the hypothesis and <br> no other mark awarded. <br> or <br> A clear and correct comparison of <br> the two histograms in context <br> based on dispersion and no other <br> mark awarded |
| :--- | :--- | :--- | :--- |

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