AQA

GCSE
STATISTICS

H

Higher tier Paper 2

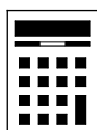Tuesday 18 June 2019   Morning   Time allowed: 1 hour 45 minutes

Materials

For this paper you must have:
- a calculator
- mathematical instruments
- a copy of the Data Sheet.

Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of the page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross out any work you do not want to be marked.

Information

- The marks for the questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper and graph paper. These must be tagged securely to this answer booklet.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
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9	
10	
11	
12	
13	
14	
15	
16	
TOTAL	

Do not write outside the box

Answer **all** questions in the spaces provided.

1 A set of data has

mean = 30

median = 25

standard deviation = 4

Circle the value of the skew for the data.

Use skew = $\dfrac{3\ (\text{mean} - \text{median})}{\text{standard deviation}}$

[1 mark]

−11.25   1.25   3.75   16.25

2 Here are some statements comparing the use of closed questions and open questions on a questionnaire.

A   Closed questions are generally quicker to answer than open questions.

B   The responses to closed questions are easier to analyse.

C   Closed questions allow respondents to give their true feelings more easily than open questions.

D   The response choices given for closed questions can help clarify the meaning of the question for respondents.

Circle the letter for the statement that is **false**.

[1 mark]

A   B   C   D

02

3 A gym has 800 members.

Lara asks a random sample of 40 members how many times they used the swimming pool last week.

Here are her results.

Number of times	0	1	2	3 or more
Frequency	21	10	5	4

Use Lara's results to estimate the total number of gym members who used the swimming pool **3 or more** times last week.

Circle your answer.

[1 mark]

4   80   160   200

1

4 Tina uses four online tests to measure her reaction time.

She measures her reaction times 20 times using each of the four tests.

The mean and standard deviation (s.d) of her results from each test are shown.

	Test A	**Test B**	**Test C**	**Test D**
mean (seconds)	0.415	0.583	0.379	0.375
s.d. (seconds)	0.025	0.054	0.104	0.075

Circle the test that appears to give the most **reliable** measure of Tina's reaction time.

[1 mark]

Test A   Test B   Test C   Test D

1

Turn over ▶

5 The spreadsheet shows the number of people attending Accident and Emergency (A&E) for major hospitals and for all A&E hospitals from 2008 to 2016.

| Year	Major hospitals	All A&E hospitals
2008	13 426 136	19 588 344
2009	13 618 300	20 511 908
2010	13 931 715	21 380 985
2011	14 013 922	21 481 402
2012	14 252 068	21 738 637
2013	14 213 148	21 778 657
2014	14 584 736	22 354 781
2015	14 960 805	22 920 435
2016	15 262 758	23 362 301

Source: www.england.nhs.uk

5 (a) Name the year when **Major hospitals** attendances fell.

[1 mark]

Answer _____

5 (b) Here is a partially completed time series graph showing the '**All A&E hospitals**' attendances.
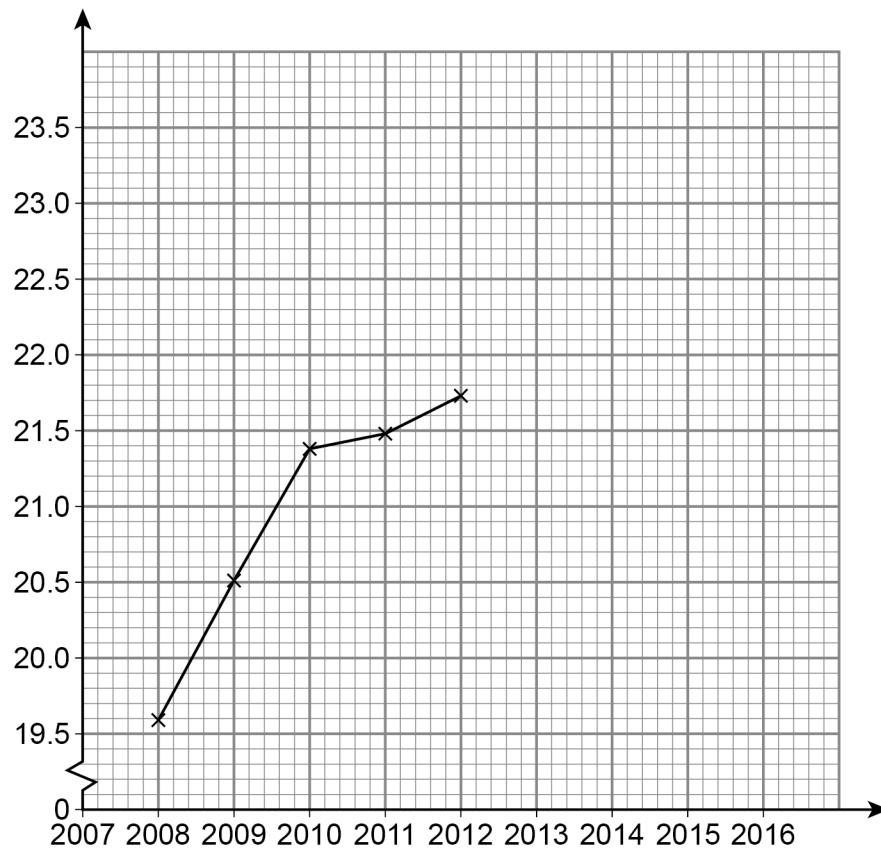
Complete the time series graph including labelling axes.

[4 marks]

5 (c) There is a break in the vertical axis in the time series graph.

Write down **one** positive reason and **one** negative reason for using this break.

[2 marks]

Positive

Negative

Question 5 continues on the next page

Turn over ▶

5 (d) Dan said,

"As there are more people going to A&E, you must have to wait longer."

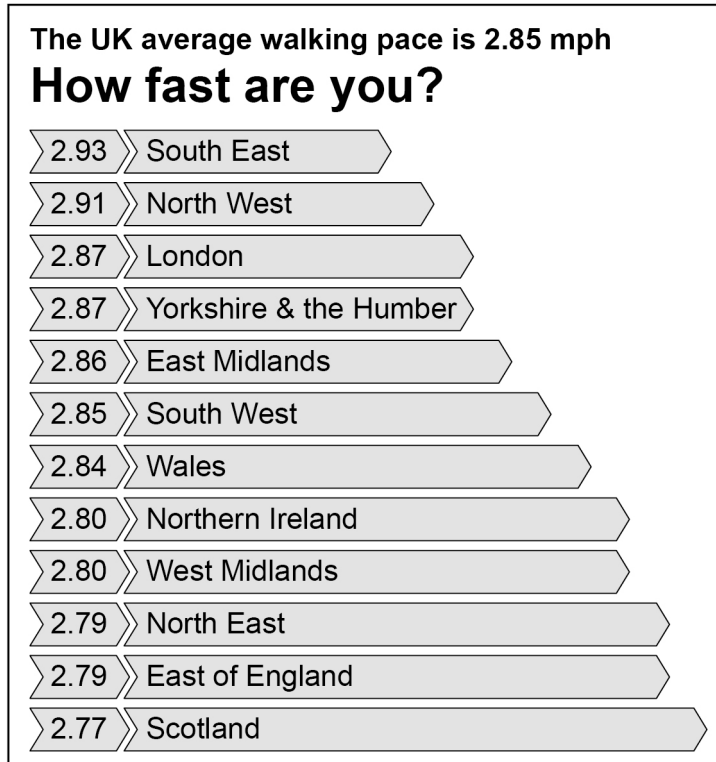Give a reason why Dan's statement may **not** be true.

[1 mark]

_____

_____

_____

8

5 (d) Dan said,

6 Samira records the average walking speed, in miles per hour (mph), of shoppers in different regions of the UK. The diagram shows her results.

The UK average walking pace is 2.85 mph
How fast are you?

2.93	South East
2.91	North West
2.87	London
2.87	Yorkshire & the Humber
2.86	East Midlands
2.85	South West
2.84	Wales
2.80	Northern Ireland
2.80	West Midlands
2.79	North East
2.79	East of England
2.77	Scotland

6 (a) List the regions in the UK where the walking speed is more than 0.05 mph faster than the **UK average**.

[1 mark]

Answer _____

_____

6 (b) Give **two** reasons why the diagram is misleading.

[2 marks]

Reason 1 _____

_____

_____

Reason 2 _____

_____

_____

Turn over ▶

6 (c) A manager in a shopping centre measures the walking speed (in mph) of a random sample of shoppers in June and a random sample of shoppers in December.

The walking speeds of 25 shoppers in June are shown in the stem-and-leaf diagram.

						June				December							
						9	8	**0**									
			7	7	6	4	2	**1**									
9	8	8	7	6	5	5	2	**2**									
		7	6	4	3	3	1	**3**									
			5	4	1	0		**4**									

Key: 8 │ 0 │ 7 represents a speed of 0.8 mph in June and a speed of 0.7 mph in December

6 (c) (i) The speeds (in mph) of 25 shoppers in December are,

1.2 3.4 0.9 1.9 2.4 2.7 1.6 3.2 2.1 0.7
1.0 2.2 2.5 1.8 4.1 1.7 2.6 1.8 3.2 1.3
2.5 0.7 3.1 2.2 1.4

Complete the back to back stem-and-leaf diagram above to show the speeds of shoppers in December.

[3 marks]

6 (c) (ii) Without further calculation, make a comparison of the average walking speeds of shoppers in June and December.

[1 mark]

_____

_____

6 (c) (iii) Give a possible reason to explain the difference in average walking speeds in June and December.

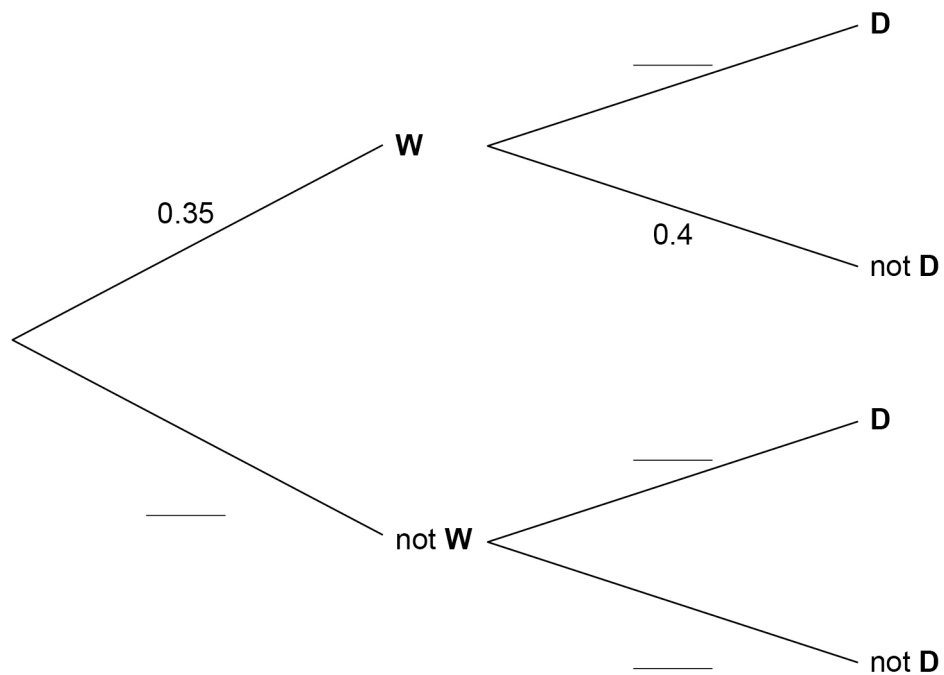**[1 mark]**

_____

_____

8

Turn over for the next question

Turn over ▶

7   Gareth has a washing machine and a dishwasher.

W is the event that his washing machine breaks down next year.

D is the event that his dishwasher breaks down next year.

Assume that the events **W** and **D** are independent.

7 (a)   The tree diagram shows some of the probabilities.

Complete the tree diagram.

[2 marks]

7 (b)   Find the probability that **at least one** of these machines breaks down next year.

[3 marks]

Answer _____

8 Maxine and Toby are investigating the amount of fat in supermarket ready meals.

8 (a) They each design a table for collecting the data.

Maxine

Fat (grams)	Tally	Frequency
4 – 8		
8 – 12		
12 – 16		
16 – 20		
20 – 24		
24 – 28		
28 – 32		
32 – 36		
Over 36		

Toby

Fat, x (grams)	Tally	Frequency
$0 \leqslant x < 5$		
$5 \leqslant x < 10$		
$10 \leqslant x < 15$		
$15 \leqslant x < 20$		
$20 \leqslant x < 25$		
$25 \leqslant x < 30$		
$30 \leqslant x < 35$		
$35 \leqslant x < 40$		
$x \geqslant 40$		

Give **two** different reasons why Toby's table is more suitable than Maxine's.

[2 marks]

Reason 1

Reason 2

Question 8 continues on the next page

Turn over ▶

8 (b)   Toby records the amount of fat in ready meals made for one person.

He collects this information from 60 ready meals sold at his local supermarket.

Fat, x (grams)	Cumulative frequency
$x < 5$	0
$x < 10$	8
$x < 15$	23
$x < 20$	34
$x < 25$	48
$x < 30$	54
$x < 35$	59
$x < 40$	60

8 (b) (i)   Draw a cumulative frequency graph to show Toby's results.

[3 marks]
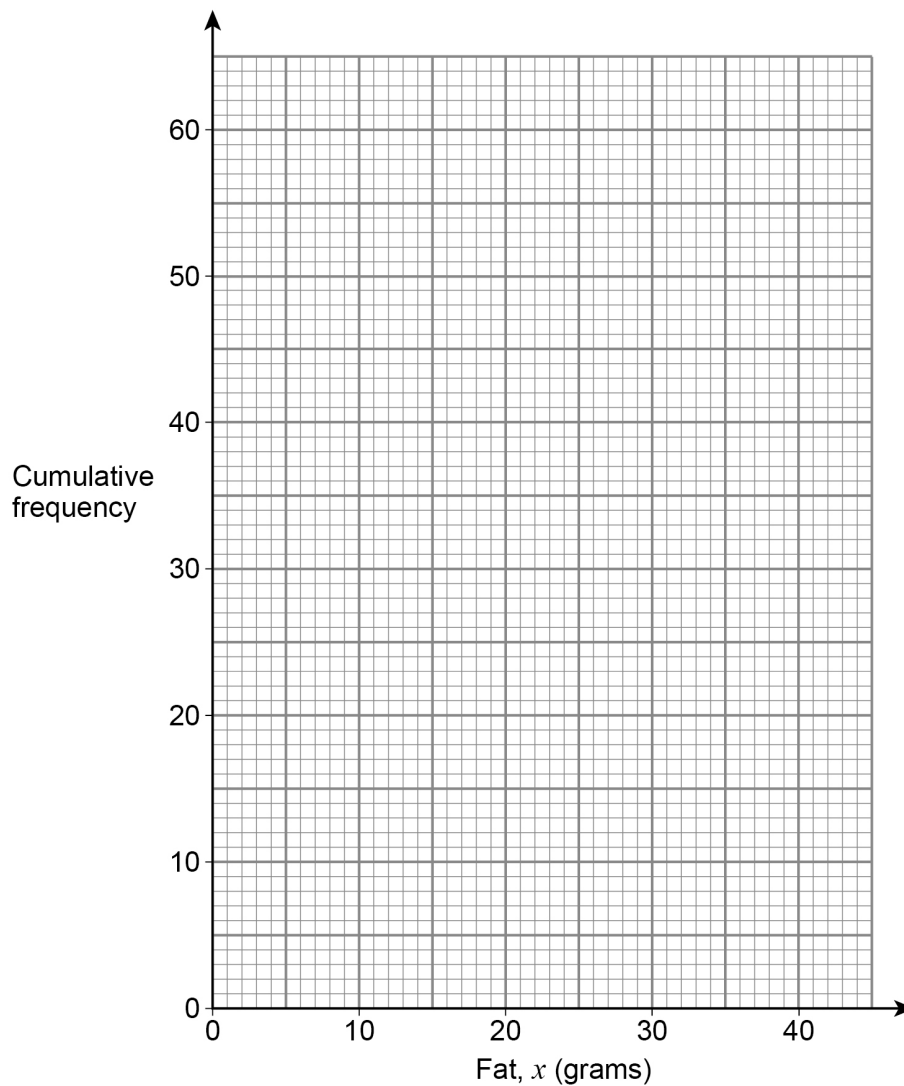
8 (b) (ii) Use your cumulative frequency graph to work out an estimate of the 70th percentile.

[2 marks]

Answer _____ grams

8 (b) (iii) Toby had previously carried out the same investigation 5 years ago.

He found then that 30% of ready meals contained more than 25 grams of fat.

Has there been a reduction in the percentage of ready meals containing more than 25 grams of fat?

Tick (✓) one box.

Yes ☐   No ☐

Give a reason for your answer.

[1 mark]

_____

_____

_____

_____

8

Turn over for the next question

Turn over ▶

9 (a) Laboratory experiments can be quicker and cheaper to perform than field experiments.

Give **one** other advantage of performing a laboratory experiment over a field experiment.

[1 mark]

_____

_____

_____

9 (b) Steve wants to investigate this hypothesis,

'Drinking a cup of coffee helps students to perform better in tests.'

He plans this laboratory experiment.

He chooses 80 Year 11 students.
He gives every student a computer-based intelligence test.
He then divides all the students into two groups.

- 40 of the students are randomly chosen to drink a cup of coffee.

- The rest are the control group and drink nothing.

Each student then takes a similar intelligence test.

---

9 (b) (i) Give a reason why Steve has used a control group.

[1 mark]

_____

_____

_____

9 (b) (ii) Here are Steve's results.

Coffee drinkers	Control group
Test results increase by an average of 6 marks	Test results increase by an average of 7 marks

Do these results support Steve's hypothesis?

Give a reason for your answer.

[1 mark]

_____
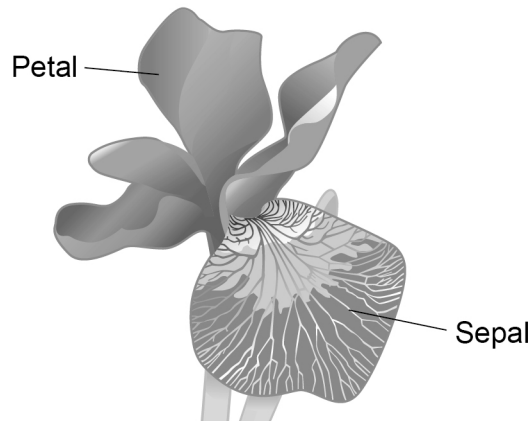
_____

_____

3

Turn over for the next question

Turn over ▶

10 An iris is a type of flowering plant.

The flower of the iris is made up from petals and sepals.

Petal

Sepal

A scientist collected the length and width of petals and of sepals from samples of iris flowers.

The scatter diagrams show sepal lengths (cm) plotted in turn against each of the other variables.

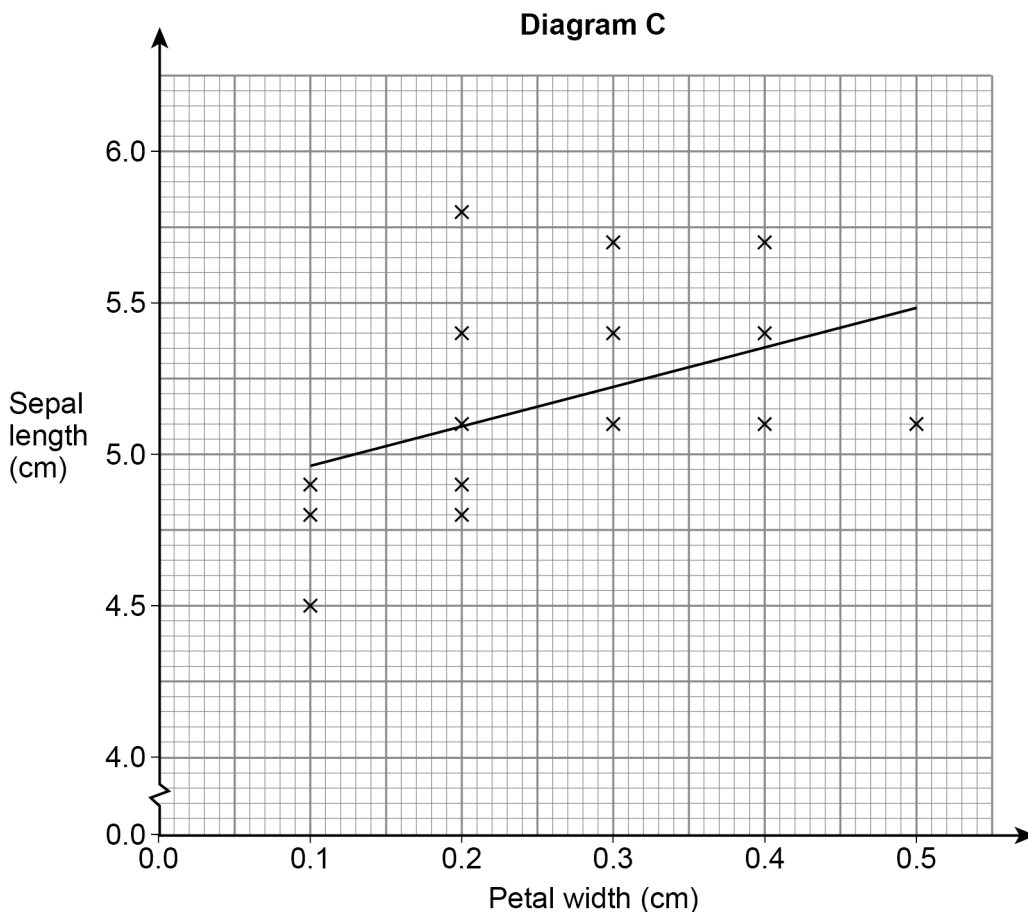The scientist's computer automatically draws a line of best fit on each diagram.

Diagram A

Sepal length (cm)

Sepal width (cm)

Diagram B

Sepal length (cm)
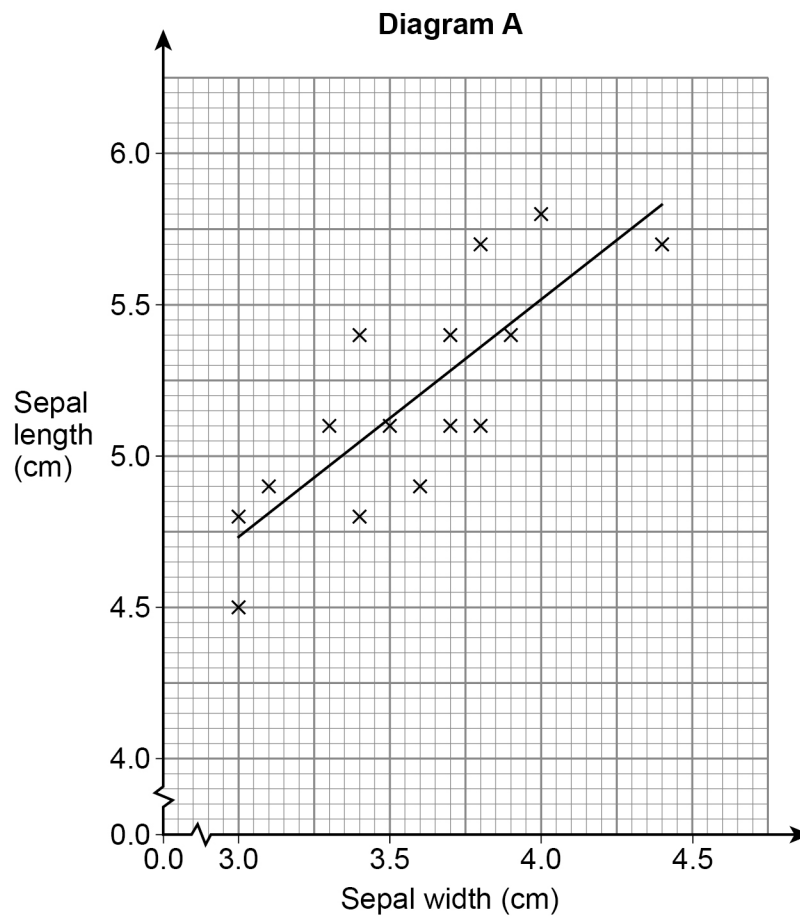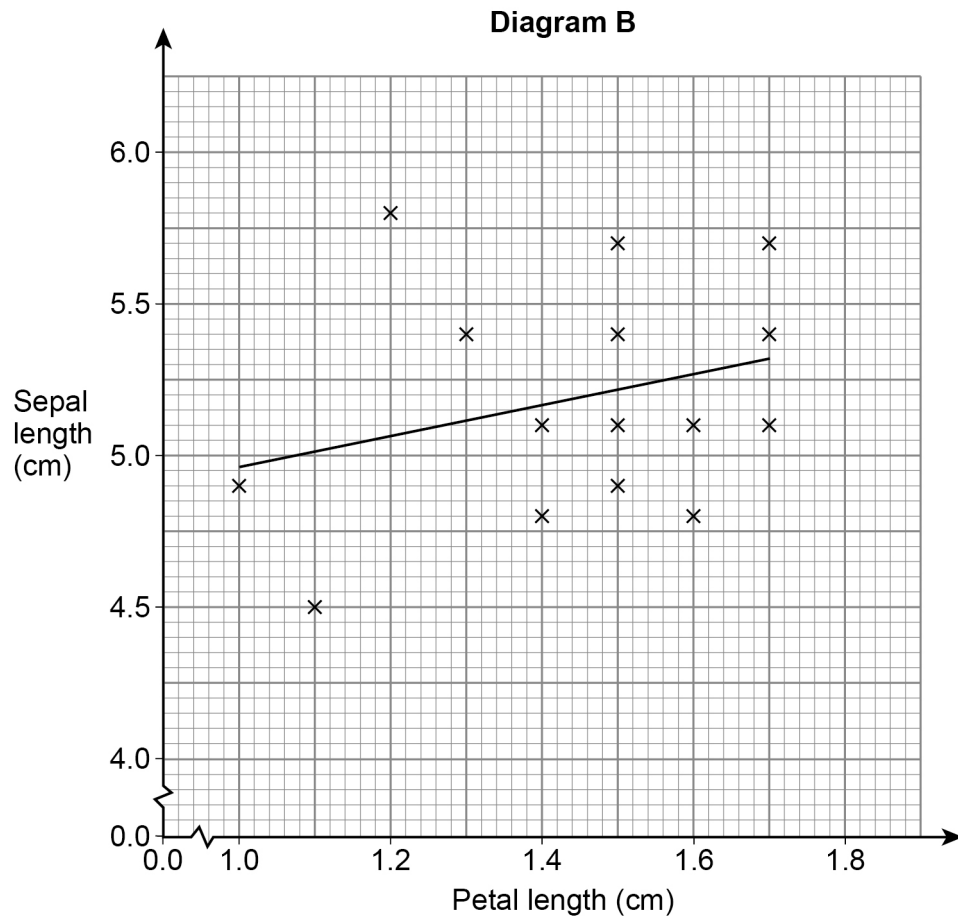
Petal length (cm)

Question 10 continues on the next page

Turn over ▶

Diagram C

Some of the measurements of another iris flower are,

Sepal width = 3.2 cm

Petal length = 1.2 cm

Petal width = 0.1 cm

Use **one** of the scatter diagrams to predict the **sepal length** of this flower.

You should state which diagram you chose to use and give a **statistical** reason for your choice.

[3 marks]

Scatter graph used _____

Reason for choice _____

_____

Sepal length _____ cm

Do not write outside the box

11 (a) Here are the volumes, in cm³, of 11 small containers.

15   16   19   21   25   26   28   29   31   34   37

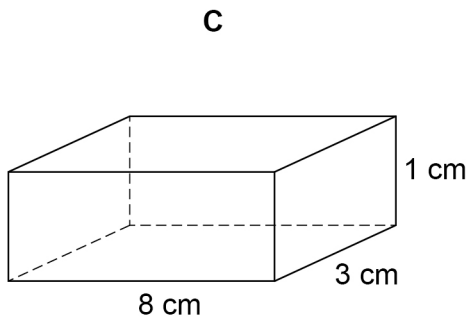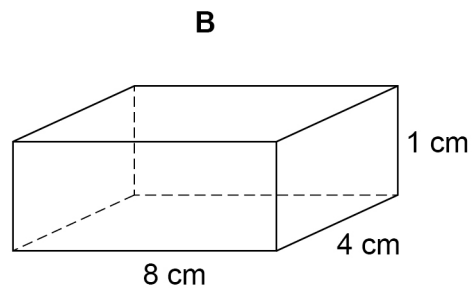Circle the value, in cm³, of the interquartile range.

[1 mark]

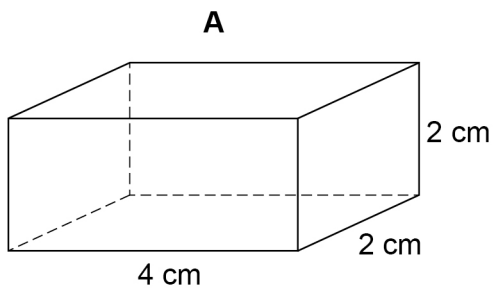6   12   22   25

11 (b) Here are four cuboids.

A

2 cm
2 cm
4 cm

B

1 cm
4 cm
8 cm

C

1 cm
3 cm
8 cm

D

8 cm
1 cm
8 cm
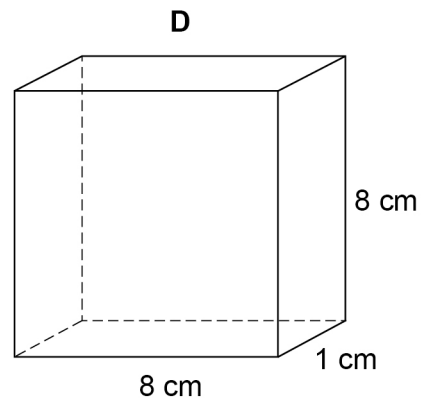
The geometric mean of the three side lengths of one of the cuboids is 4 cm

Circle the letter of this cuboid.

[1 mark]

A   B   C   D

Turn over ▶

2

12 Max, Natalie and Lottie work on a cruise ship.

They want to ask passengers staying in standard class accommodation what they think about their cabins.

There are 900 passengers in total on the cruise ship, of which 460 are staying in standard cabins.

Max, Natalie and Lottie each decide to collect information from a sample of 50 passengers.

12 (a) Max says that the population for the investigation is all passengers on the cruise ship.

Explain why he is wrong.

[1 mark]

12 (b) Natalie's calculator has a button marked Ran#.

This button generates a random number between 0 and 1

She uses her calculator to select 50 passengers from the population using the following method.

> Assign every passenger in the population a number.
>
> Generate random numbers from a calculator by typing Ran# × 100
>
> Select the passenger that matches the answer.

Natalie's method contains some errors.

Correct Natalie's method to show how she can use her Ran# button to choose a **random sample** from the population.

[3 marks]

12 (c) Lottie designs a questionnaire.

Here is part of her questionnaire.

> How would you rate the value for money and the quality of standard class cabins?
>
> Excellent ☐   Very good ☐   Good ☐   Fair ☐

Rewrite this part of Lottie's questionnaire so that she is more likely to obtain useful data.

[2 marks]

Turn over for the next question

6

Turn over ▶

13 Seb and Laura are studying for a gardening qualification.

Their overall mark is found as the **weighted average** of their marks in,

coursework	weight = 20%
a written examination	weight = 35%
a practical examination	weight = 45%

13 (a) Seb's marks are shown in the table.

Coursework	Written examination	Practical examination
85%	54%	70%

Calculate Seb's overall mark for the course.

[3 marks]

Answer _____ %

13 (b) Students need an overall mark of 60% to pass the qualification.

Laura scores,

40% in her coursework

32% in her written examination.

She has **not** yet taken the practical examination.

Can she still pass the qualification?

Tick (✓) one box.

Yes ☐   No ☐

You **must** show your working.

[3 marks]

_____

_____

_____

_____

_____

_____

6

Turn over for the next question

Turn over ▶

14 Carly has an activity tracker watch which tells her the distance she walks each day.

She sets herself the following target,

Target: Walk at least 6 km **every** day.

14 (a) She records the distance, x km, she walks on each of 24 different days.

Here is a summary of her results.

$$\sum x = 149.76 \qquad\qquad \sum x^2 = 968.72$$

14 (a) (i) Show that the mean distance she walks each day is 6.24 km

[1 mark]

14 (a) (ii) Show that the standard deviation is 1.2 km to 1 decimal place.

Use standard deviation = $\sqrt{\dfrac{\sum x^2}{n} - \left(\dfrac{\sum x}{n}\right)^2}$

[2 marks]

14 (a) (iii) Carly says that she has met her target.

Comment on Carly's claim.

Explain your answer.

[2 marks]

14 (b) Tomasz and Erika also have activity tracker watches.

The mean and the standard deviation for the distance they walk each day are shown in the table.

	Mean (km)	**Standard deviation (km)**
Tomasz	5.15	2.34
Erika	5.36	0.45

Compare statistically the distances walked by Tomasz and Erika.

[2 marks]

7

Turn over for the next question

Turn over ▶

15 A hotel has a choice of coffee or tea as the hot drink for breakfast.

The hotel finds that 18% of its customers have tea with their breakfast.

15 (a) Theo says,

"82% of customers at the hotel **must** have coffee with their breakfast."

Comment on Theo's statement.

[1 mark]

15 (b) The hotel selects a random sample of 5 customers.

Use the Binomial distribution to find the probability that **exactly one** of these customers has tea with their breakfast.

[3 marks]

Answer

15 (c)   A family of 3 people have breakfast at the hotel.

Explain why the number of people in the family having tea with their breakfast may **not** follow a Binomial distribution.

[1 mark]

_____

_____

_____

5

Turn over for the next question

Turn over ▶

16 University undergraduate degrees are graded as First Class, Upper Second Class, Lower Second Class, Third Class or Pass.

Luca wants to investigate how the number of degrees awarded in the UK in 2016 compares with the number awarded in the UK in 2008.

He also wants to see if there are any changes in the proportion of First Class degrees awarded.

He collects data about degree results from the website hesa.ac.uk.

The **Data Sheet** contains the data he collects for degrees awarded in the UK in 2016.

16 (a) Luca uses secondary data for his investigation.

Explain why it would **not** be sensible for him to collect primary data.

[1 mark]

He decides to use **comparative pie charts** to show the data.

He draws this pie chart to show the grades of degree awarded in 2008.

2008   **2016**
Number of degrees
308 395

Radius   3.0 cm
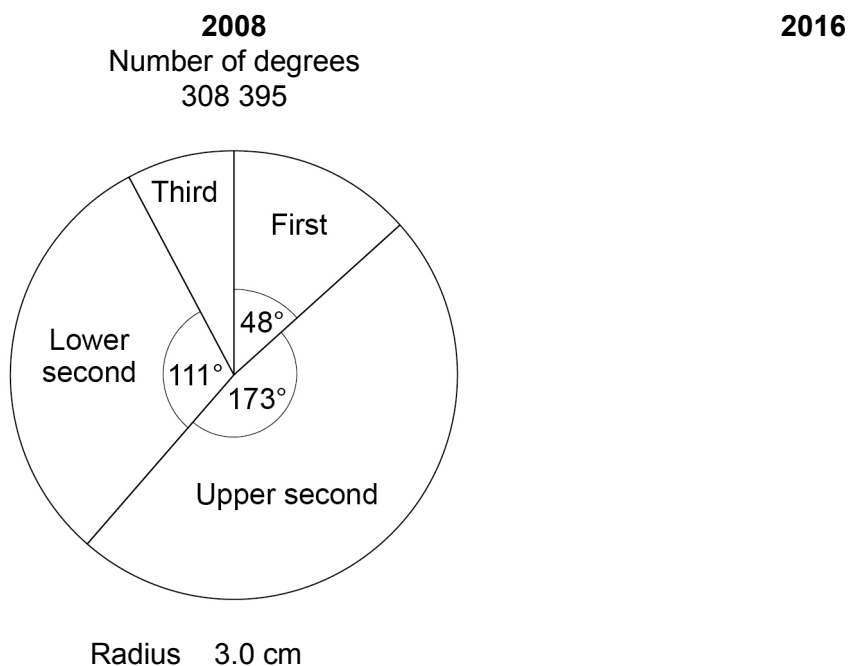
16 (b) Give **one** reason why comparative pie charts are a suitable way to show the data.

[1 mark]

_____

_____

16 (c) Draw the corresponding pie chart for 2016 next to the one for 2008.

Use the information from the 2008 pie chart and **TABLE 1** on the **Data Sheet**.

You **must** show your working.

[6 marks]

_____

_____

_____

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_____

16 (d) More **First Class** degrees were awarded in 2016 than in 2008.

How many more?

[3 marks]

_____

_____

_____

Answer _____

Question 16 continues on the next page

Turn over ▶

16 (e) Luca makes the following conclusion,

'It has become easier to get a First Class degree in the UK.'

Give **one** reason why Luca's conclusion may **not** be correct.

[1 mark]

16 (f) Luca extends his investigation by exploring the proportion of full-time students awarded a First Class degree compared to the proportion of part-time students awarded a First Class degree.

The data for 2016 are shown on the **Data Sheet** in **TABLE 2**.

Compare these proportions.

[3 marks]

15

END OF QUESTIONS

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