

# QUESTION 7.



6 A queue Abstract Data Type (ADT) has these associated operations:

- create queue
- add item to queue
- remove item from queue

The queue ADT is to be implemented as a linked list of nodes.

Each node consists of data and a pointer to the next node.

(a) The following operations are carried out:

```
CreateQueue  
AddName ("Ali")  
AddName ("Jack")  
AddName ("Ben")  
AddName ("Ahmed")  
RemoveName  
AddName ("Jatinder")  
RemoveName
```

Add appropriate labels to the diagram to show the final state of the queue. Use the space on the left as a workspace. Show your final answer in the node shapes on the right:





(b) Using pseudocode, a record type, `Node`, is declared as follows:

```

TYPE Node
  DECLARE Name      : STRING
  DECLARE Pointer   : INTEGER
ENDTYPE

```

The statement

```

DECLARE Queue : ARRAY[1:10] OF Node

```

reserves space for 10 nodes in array `Queue`.

(i) The `CreateQueue` operation links all nodes and initialises the three pointers that need to be used: `HeadPointer`, `TailPointer` and `FreePointer`.

Complete the diagram to show the value of all pointers after `CreateQueue` has been executed.

Queue		
	Name	Pointer
HeadPointer	[1]	
	[2]	
TailPointer	[3]	
	[4]	
	[5]	
FreePointer	[6]	
	[7]	
	[8]	
	[9]	
	[10]	

[4]



- (ii) The algorithm for adding a name to the queue is written, using ps. procedure with the header:

```
PROCEDURE AddName (NewName)
```

where *NewName* is the new name to be added to the queue.

The procedure uses the variables as shown in the identifier table.

Identifier	Data type	Description
Queue	Array[1:10] OF Node	Array to store node data
NewName	STRING	Name to be added
FreePointer	INTEGER	Pointer to next free node in array
HeadPointer	INTEGER	Pointer to first node in queue
TailPointer	INTEGER	Pointer to last node in queue
CurrentPointer	INTEGER	Pointer to current node

```
PROCEDURE AddName (BYVALUE NewName : STRING)
  // Report error if no free nodes remaining
  IF FreePointer = 0
    THEN
      Report Error
    ELSE
      // new name placed in node at head of free list
      CurrentPointer ← FreePointer
      Queue[CurrentPointer].Name ← NewName
      // adjust free pointer
      FreePointer ← Queue[CurrentPointer].Pointer
      // if first name in queue then adjust head pointer
      IF HeadPointer = 0
        THEN
          HeadPointer ← CurrentPointer
        ENDIF
      // current node is new end of queue
      Queue[CurrentPointer].Pointer ← 0
      TailPointer ← CurrentPointer
    ENDIF
  ENDPROCEDURE
```

## QUESTION 8.

10



5 A stack Abstract Data Type (ADT) has these associated operations:

- create stack
- add item to stack (push)
- remove item from stack (pop)

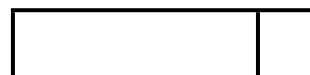
The stack ADT is to be implemented as a linked list of nodes.

Each node consists of data and a pointer to the next node.

(a) There is one pointer: the top of stack pointer, which points to the last item added to the stack. Draw a diagram to show the final state of the stack after the following operations are carried out.

```
CreateStack
Push("Ali")
Push("Jack")
Pop
Push("Ben")
Push("Ahmed")
Pop
Push("Jatinder")
```

Add appropriate labels to the diagram to show the final state of the stack. Use the space on the left as a workspace. Show your final answer in the node shapes on the right:



[3]



(b) Using pseudocode, a record type, Node, is declared as follows:

```

TYPE Node
  DECLARE Name : STRING
  DECLARE Pointer : INTEGER
ENDTYPE
    
```

The statement

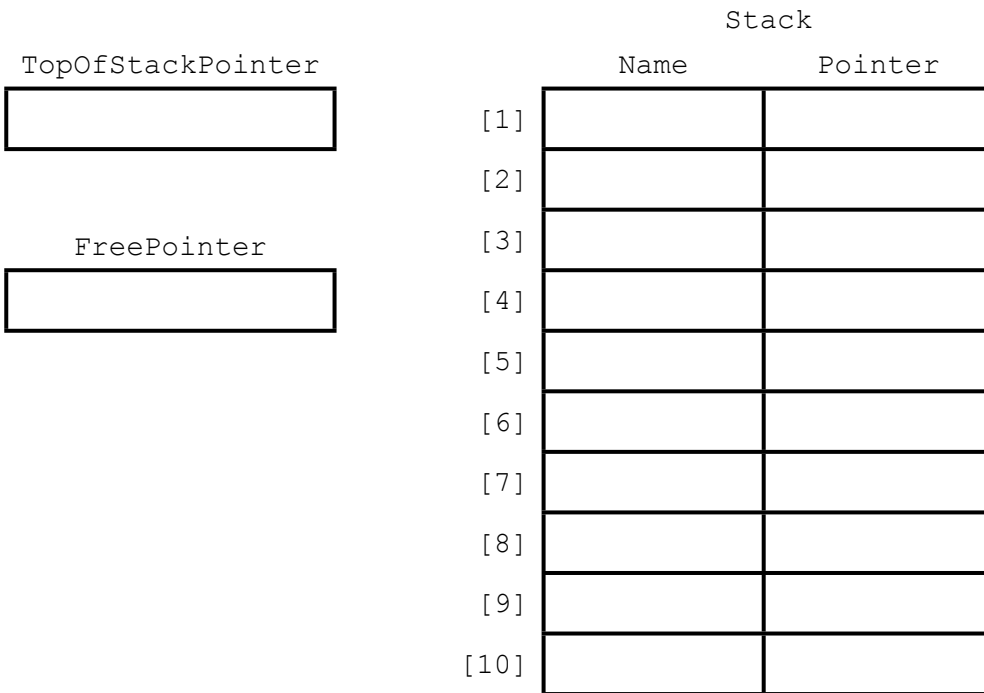
```

DECLARE Stack : ARRAY[1:10] OF Node
    
```

reserves space for 10 nodes in array Stack.

(i) The CreateStack operation links all nodes and initialises the TopOfStackPointer and FreePointer.

Complete the diagram to show the value of all pointers after CreateStack has been executed.



[4]

- (ii) The algorithm for adding a name to the stack is written, using pseudo-code, as a procedure with the header

```
PROCEDURE Push (NewName)
```

Where `NewName` is the new name to be added to the stack. The procedure uses the variables as shown in the identifier table.

Identifier	Data type	Description
Stack	Array[1:10] OF Node	
NewName	STRING	Name to be added
FreePointer	INTEGER	Pointer to next free node in array
TopOfStackPointer	INTEGER	Pointer to first node in stack
TempPointer	INTEGER	Temporary store for copy of FreePointer

```
PROCEDURE Push(BYVALUE NewName : STRING)
  // Report error if no free nodes remaining
  IF FreePointer = 0
    THEN
      Report Error
    ELSE
      // new name placed in node at head of free list
      Stack[FreePointer].Name ← NewName
      // take a temporary copy and
      // then adjust free pointer
      TempPointer ← FreePointer
      FreePointer ← Stack[FreePointer].Pointer
      // link current node to previous top of stack
      Stack[TempPointer].Pointer ← TopOfStackPointer
      // adjust TopOfStackPointer to current node
      TopOfStackPointer ← TempPointer
    ENDIF
  ENDPROCEDURE
```



Complete the **pseudocode** for the procedure Pop. Use the variables listed in the identifier.

```
PROCEDURE Pop()
```

```
    // Report error if Stack is empty
```

.....

.....

.....

.....

```
    OUTPUT Stack [.....].Name
```

```
    // take a copy of the current top of stack pointer
```

.....

```
    // update the top of stack pointer
```

.....

```
    // link released node to free list
```

.....

.....

.....

```
ENDPROCEDURE
```

[5]

## QUESTION 9.

10



4 A binary tree Abstract Data Type (ADT) has these associated operations:

- create the tree (`CreateTree`)
- add an item to tree (`Add`)
- output items in ascending order (`TraverseTree`)

(a) Show the final state of the binary tree after the following operations are carried out.

```
CreateTree
Add("Dodi")
Add("Farai")
Add("Elli")
Add("George")
Add("Ben")
Add("Celine")
Add("Ali")
```





- (b) The binary tree ADT is to be implemented as an array of nodes. Each node and two pointers.

Using pseudocode, a record type, `Node`, is declared as follows:

```

TYPE Node
  DECLARE Name : STRING
  DECLARE LeftPointer : INTEGER
  DECLARE RightPointer : INTEGER
ENDTYPE

```

The statement

```

DECLARE Tree : ARRAY[1:10] OF Node

```

reserves space for 10 nodes in array `Tree`.

The `CreateTree` operation links all nodes into a linked list of free nodes. It also initialises the `RootPointer` and `FreePointer`.

Show the contents of the `Tree` array and the values of the two pointers, `RootPointer` and `FreePointer`, after the operations given in **part (a)** have been carried out.

		Tree		
RootPointer		Name	LeftPointer	RightPointer
<input type="text"/>	[1]			
	[2]			
FreePointer	[3]			
<input type="text"/>	[4]			
	[5]			
	[6]			
	[7]			
	[8]			
	[9]			
	[10]			

[7]



(c) A programmer needs an algorithm for outputting items in ascending order. To do this, the programmer writes a recursive procedure in pseudocode.

(i) Complete the pseudocode:

```

01 PROCEDURE TraverseTree (BYVALUE Root: INTEGER)
02     IF Tree[Root].LeftPointer .....
03         THEN
04             TraverseTree (.....)
05     ENDIF
06     OUTPUT ..... .Name
07     IF ..... <> 0
08         THEN
09             TraverseTree (.....)
10     ENDIF
11 ENDPROCEDURE
    
```

[5]

(ii) Explain what is meant by a recursive procedure. Give a line number from the code above that shows procedure `TraverseTree` is recursive.

.....

.....

.....

Line number ..... [2]

(iii) Write the pseudocode call required to output all names stored in `Tree`.

.....

..... [1]



**Question 5 begins on page 14.**

# QUESTION 10.



1 A linked list abstract data type (ADT) is to be used to store and organise surnames.

This will be implemented with a 1D array and a start pointer. Elements of the array are of a user-defined type. The user-defined type consists of a data value and a link pointer.

Identifier	Data type	Description
LinkedList	RECORD	User-defined type
Surname	STRING	Surname string
Ptr	INTEGER	Link pointers for the linked list

(a) (i) Write **pseudocode** to declare the type `LinkedList`.

.....

.....

.....

.....[3]

(ii) The 1D array is implemented with an array `SurnameList` of type `LinkedList`.

Write the **pseudocode** declaration statement for `SurnameList`. The lower and upper bounds of the array are 1 and 5000 respectively.

.....[2]

(b) The following surnames are organised as a linked list with a start pointer `StartPtr`.

`StartPtr: 3`

	1	2	3	4	5	6	...	5000
<b>Surname</b>	Liu	Yang	Chan	Wu	Zhao	Huang	...	
<b>Ptr</b>	4	5	6	2	0	1	...	

State the value of the following:

(i) `SurnameList[4].Surname` .....[1]

(ii) `SurnameList[StartPtr].Ptr` .....[1]

(c) Pseudocode is to be written to search the linked list for a surname input by the user.



Identifier	Data type	Description
ThisSurname	STRING	The surname to search for
Current	INTEGER	Index to array SurnameList
StartPtr	INTEGER	Index to array SurnameList. Points to the element at the start of the linked list

(i) Study the pseudocode in **part (c)(ii)**.

Complete the table above by adding the missing identifier details.

[2]

(ii) Complete the pseudocode.

```

01 Current ← .....
02 IF Current = 0
03     THEN
04         OUTPUT .....
05     ELSE
06         IsFound ← .....
07         INPUT ThisSurname
08         REPEAT
09             IF ..... = ThisSurname
10                 THEN
11                     IsFound ← TRUE
12                     OUTPUT "Surname found at position ", Current
13                 ELSE
14                     // move to the next list item
15                     .....
16             ENDIF
17         UNTIL IsFound = TRUE OR .....
18         IF IsFound = FALSE
19             THEN
20                 OUTPUT "Not Found"
21             ENDIF
22 ENDIF

```

[6]

## QUESTION 11.



4 An ordered linked list Abstract Data Type (ADT) has these associated operations.

- create list
- add item to list
- output list to console

The ADT is to be implemented using object-oriented programming as a linked list of nodes.

Each node consists of data and a pointer.

(a) There are two classes, `LinkedList` and `Node`.

(i) State the term used to describe the relationship between these classes.

.....[1]

(ii) Draw the appropriate diagram to represent this relationship. Do not list the attributes and methods of the classes.

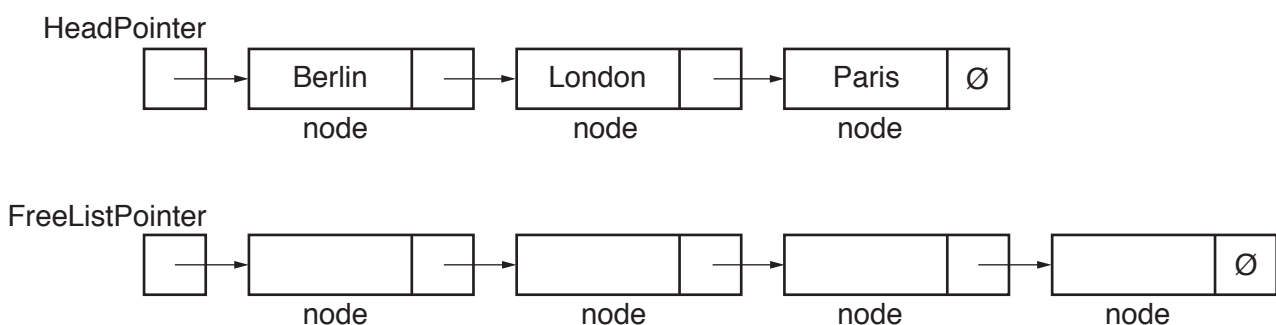




(c) The identifier table for the `LinkedList` class is:

Identifier	Data type	Description
<code>HeadPointer</code>	INTEGER	Pointer to the first node in the ordered list.
<code>FreeListPointer</code>	INTEGER	Pointer to the first node in the free list.
<code>NodeArray</code>	ARRAY[0 : 7] OF Node	1D array stores the nodes that make the ordered linked list. The unused nodes are linked together into a free list.
<code>Constructor()</code>		Constructor instantiates an object of <code>LinkedList</code> class, initialises <code>HeadPointer</code> to be a null pointer and links all nodes to form the free list.
<code>FindInsertionPoint()</code>		Procedure that takes the new data item as the parameter <code>NewData</code> and returns two parameters: <ul style="list-style-type: none"> <li>• <code>PreviousPointer</code>, whose value is:               <ul style="list-style-type: none"> <li>◦ either pointer to node before the insertion point</li> <li>◦ or the null pointer if the new node is to be inserted at the beginning of the list.</li> </ul> </li> <li>• <code>NextPointer</code>, whose value is a pointer to node after the insertion point.</li> </ul>
<code>AddToList(NewString)</code>		Procedure that takes as a parameter a unique string and links it into the correct position in the ordered list.
<code>OutputListToConsole()</code>		Procedure to output all the data from the list pointed to by <code>HeadPointer</code> .

The following diagram shows an example of a linked list object. This example list consists of three nodes, linked in alphabetical order of the data strings. The unused nodes are linked to form a free list.



The symbol  $\emptyset$  represents a null pointer.

(i) Explain the meaning of the term **null pointer**.

.....









**Question 4 continues on page 14.**



**(vi)** The structured English for the `AddToList(NewString)` method is as follows:

```

Make a copy of the value of free list pointer, name it NewNodePointer
Store new data item in free node pointed to by NewNodePointer
Adjust free list pointer to point to next free node
IF linked list is currently empty
    THEN
        Make this node the first node
        Set pointer of this node to null pointer
    ELSE
        Find insertion point using the FindInsertionPoint method
        // FindInsertionPoint provides
        // pointer to previous node and pointer to next node
        IF previous pointer is null pointer
            THEN
                Link this node to front of list
            ELSE
                Link this node between previous node and next node

```

The `FindInsertionPoint` method receives the new data item as the parameter `NewString`. It returns two parameters:

- `PreviousPointer`, whose value is:
  - either the pointer to the node before the insertion point
  - or the null pointer, if the new node is to be inserted at the beginning of the list.
- `NextPointer`, whose value is the pointer to the node after the insertion point.



## QUESTION 12.



2 An ordered binary tree Abstract Data Type (ADT) has these associated operations:

- create tree
- add new item to tree
- traverse tree

The binary tree ADT is to be implemented as a linked list of nodes.

Each node consists of data, a left pointer and a right pointer.

(a) A null pointer is shown as  $\emptyset$ .

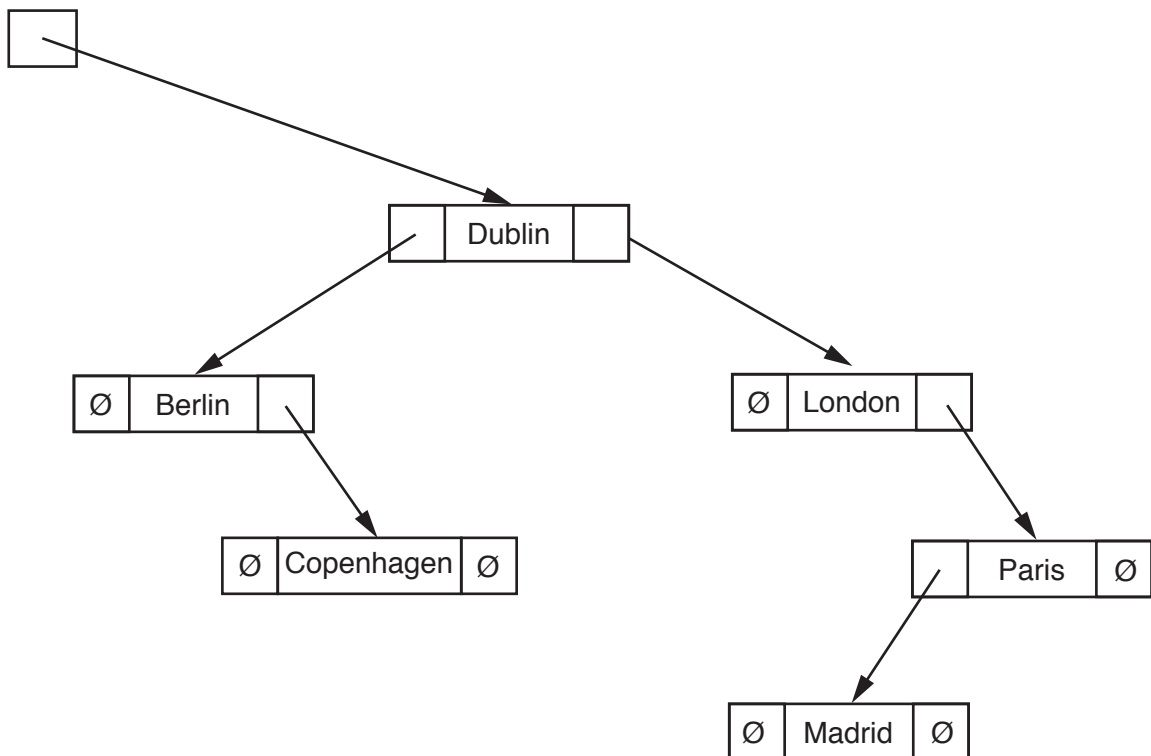
Explain the meaning of the term **null pointer**.

.....  
.....[1]

(b) The following diagram shows an ordered binary tree after the following data have been added:

Dublin, London, Berlin, Paris, Madrid, Copenhagen

RootPointer



Another data item to be added is Athens.

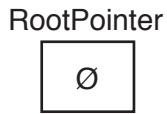
Make the required changes to the diagram when this data item is added.

[2]

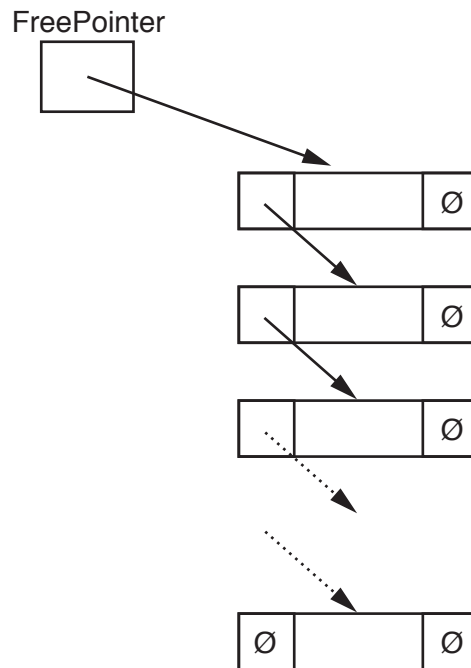
5



(c) A tree without any nodes is represented as:



Unused nodes are linked together as shown:



The following diagram shows an array of records that stores the tree shown in **part (b)**.

(i) Add the relevant pointer values to complete the diagram.

RootPointer		LeftPointer	Tree data	RightPointer
0	[0]		Dublin	
	[1]		London	
	[2]		Berlin	
	[3]		Paris	
	[4]		Madrid	
FreePointer	[5]		Copenhagen	
	[6]		Athens	
	[7]			
	[8]			
	[9]			

[5]



- (ii) Give an appropriate numerical value to represent the null pointer for the  
your answer.

.....

.....

.....

..... [2]

- (d) A program is to be written to implement the tree ADT. The variables and procedures to be used are listed below:

Identifier	Data type	Description
Node	RECORD	Data structure to store node data and associated pointers.
LeftPointer	INTEGER	Stores index of start of left subtree.
RightPointer	INTEGER	Stores index of start of right subtree.
Data	STRING	Data item stored in node.
Tree	ARRAY	Array to store nodes.
NewDataItem	STRING	Stores data to be added.
FreePointer	INTEGER	Stores index of start of free list.
RootPointer	INTEGER	Stores index of root node.
NewNodePointer	INTEGER	Stores index of node to be added.
CreateTree ()		Procedure initialises the root pointer and free pointer and links all nodes together into the free list.
AddToTree ()		Procedure to add a new data item in the correct position in the binary tree.
FindInsertionPoint ()		Procedure that finds the node where a new node is to be added. Procedure takes the parameter <code>NewDataItem</code> and returns two parameters: <ul style="list-style-type: none"> <li>• <code>Index</code>, whose value is the index of the node where the new node is to be added</li> <li>• <code>Direction</code>, whose value is the direction of the pointer ("Left" or "Right").</li> </ul>





(i) Complete the pseudocode to create an empty tree.

TYPE Node

.....  
 .....  
 .....

ENDTYPE

DECLARE Tree : ARRAY[0 : 9] .....

DECLARE FreePointer : INTEGER

DECLARE RootPointer : INTEGER

PROCEDURE CreateTree()

    DECLARE Index : INTEGER

.....  
 .....

    FOR Index ← 0 TO 9   // link nodes

.....  
 .....

    ENDFOR

.....

ENDPROCEDURE

[7]



(ii) Complete the pseudocode to add a data item to the tree.

```

PROCEDURE AddToTree(BYVALUE NewDataItem : STRING)
// if no free node report an error
  IF FreePointer .....
    THEN
      OUTPUT("No free space left")
    ELSE // add new data item to first node in the free list
      NewNodePointer ← FreePointer
      .....
      // adjust free pointer
      FreePointer ← .....
      // clear left pointer
      Tree[NewNodePointer].LeftPointer ← .....
      // is tree currently empty ?
      IF .....
        THEN // make new node the root node
          .....
        ELSE // find position where new node is to be added
          Index ← RootPointer
          CALL FindInsertionPoint(NewDataItem, Index, Direction)
          IF Direction = "Left"
            THEN // add new node on left
              .....
            ELSE // add new node on right
              .....
          ENDIF
        ENDIF
      ENDIF
    ENDPROCEDURE
  
```



- (e) The traverse tree operation outputs the data items in alphabetical order. This operation can be implemented as a recursive solution.

Complete the pseudocode for the recursive procedure `TraverseTree`.

```
PROCEDURE TraverseTree (BYVALUE Pointer : INTEGER)
```

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.....

.....

```
ENDPROCEDURE
```

[5]





(b) The records are stored in a random access file.

The function, `Hash()`, takes as a parameter the ISBN and returns the hash value.

The disk address of the record in the hash table is calculated as: ISBN modulus 2000 p

Write **program code** for the function `Hash()`.

Programming language .....

Program code .....

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[4]





# QUESTION 14.



6 A linked list abstract data type (ADT) is created. This is implemented as an array, records are of type `ListElement`.

An example of a record of `ListElement` is shown in the following table.

Data Item	Value
Country	"Scotland"
Pointer	1

(a) (i) Use **pseudocode** to write a definition for the record type, `ListElement`.

.....

.....

.....

.....

..... [3]

(ii) Use **pseudocode** to write an array declaration to reserve space for only 15 nodes of type `ListElement` in an array, `CountryList`. The lower bound element is 1.

..... [2]

(b) The program stores the position of the last node in the linked list in `LastNode`. The last node always has a `Pointer` value of `-1`. The position of the node at the head of the list is stored in `ListHead`.

After some processing, the array and variables are in the following state.

<b>ListHead</b>
1
<b>LastNode</b>
3

CountryList		
	Country	Pointer
1	"Wales"	2
2	"Scotland"	4
3		-1
4	"England"	5
5	"Brazil"	6
6	"Canada"	7
7	"Mexico"	8
8	"Peru"	9
9	"China"	10
10		11
11		12
12		13
13		14
14		15
15		3





A **recursive** algorithm searches the list for a value, deletes that value, and updates the required pointers. When a node value is deleted, it is set to empty "" and the pointer is moved to the end of the list.

A node value is deleted using the pseudocode statement

```
CALL DeleteNode("England", 1, 0)
```

Complete the following **pseudocode** to implement the DeleteNode procedure.

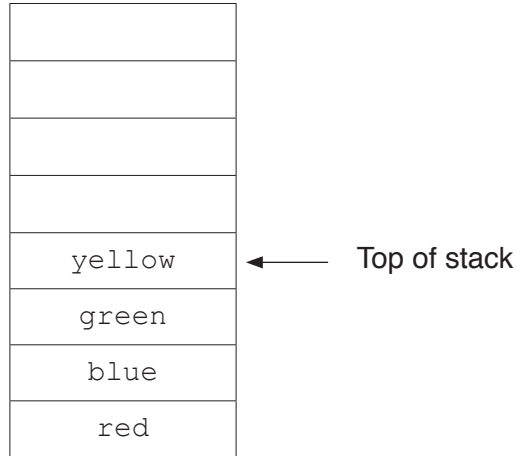
```
PROCEDURE DeleteNode(NodeValue: STRING, ThisPointer : INTEGER,
                    PreviousPointer : INTEGER)

IF CountryList[ThisPointer].Value = NodeValue
THEN
    CountryList[ThisPointer].Value ← ""
    IF ListHead = .....
    THEN
        ListHead ← .....
    ELSE
        CountryList[PreviousPointer].Pointer ← CountryList[ThisPointer].Pointer
    ENDIF
    CountryList[LastNode].Pointer ← .....
    LastNode ← ThisPointer
    .....
ELSE
    IF CountryList[ThisPointer].Pointer <> -1
    THEN
        CALL DeleteNode(NodeValue, .....,
                        ThisPointer)
    ELSE
        OUTPUT "DOES NOT EXIST"
    ENDIF
ENDIF
ENDIF
ENDPROCEDURE
```

## QUESTION 15.



- 1 (a) A stack contains the values 'red', 'blue', 'green' and 'yellow'.



- (i) Show the contents of the stack in **part(a)** after the following operations.

POP ()

PUSH ('purple')

PUSH ('orange')



[1]



(ii) Show the contents of the stack from **part(a)(i)** after these further operations.

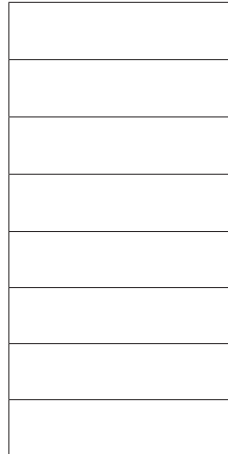
POP ()

POP ()

PUSH ('brown')

POP ()

PUSH ('black')



[1]

(b) A queue is an alternative Abstract Data Type (ADT).

Describe a **queue**.

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[3]

## QUESTION 16.



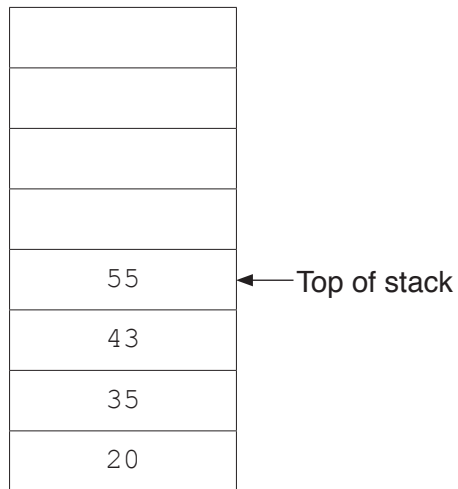
2 A stack is an Abstract Data Type (ADT).

(a) Tick (✓) **one** box to show the statement that describes a stack data structure.

Statement	Tick (✓)
Last in first out	
First in first out	
Last in last out	

[1]

(b) A stack contains the values 20, 35, 43, 55.



(i) Show the contents of the stack in **part (b)** after the following operations.

POP ()

POP ()

PUSH (10)



[1]



(ii) Show the contents of the stack from **part (b)(i)** after these further operations.

POP ()

PUSH (50)

PUSH (55)

POP ()

PUSH (65)


[1]



## QUESTION 17.



- 2 The number of cars that cross a bridge is recorded each hour. This number is placed in a circular queue before being processed.
- (a) The queue is stored as an array, `NumberQueue`, with eight elements. The function `AddToQueue` adds a number to the queue. `EndPoint` and `StartPointer` are global variables.

Complete the following **pseudocode** algorithm for the function `AddToQueue`.

```
FUNCTION AddToQueue (Number : INTEGER) RETURNS BOOLEAN

    DECLARE TempPointer : INTEGER

    CONSTANT FirstIndex = 0

    CONSTANT LastIndex = .....

    TempPointer ← EndPointer + 1

    IF ..... > LastIndex

        THEN

            TempPointer ← .....

        ENDIF

    IF TempPointer = StartPointer

        THEN

            RETURN .....

        ELSE

            EndPointer ← TempPointer

            NumberQueue[EndPointer] ← .....

            RETURN TRUE

        ENDIF

    ENDFUNCTION
```



(b) Describe how a number is removed from the circular queue to be processed.

.....

.....

.....

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.....

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.....

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.....

..... [4]

(c) A queue is one example of an Abstract Data Type (ADT).

Identify **three other** Abstract Data Types.

1 .....

2 .....

3 ..... [3]