# Level 3 Certificate MATHEMATICAL STUDIES <br> 1350/2B 

Paper 2B Critical path and risk analysis

Mark scheme

June 2019
Version: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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| $\mathbf{Q}$ | Answer | Mark | Comments |
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| $\mathbf{1 ( b )}$ | $\begin{array}{l}\text { No labels on the (horizontal) } x \text { axis } \\ \text { Wrong units used (kg used instead of g) } \\ \text { One of the bars is incorrect (brand C's } \\ \text { ready salted) } \\ \text { No title for the graph } \\ \text { The scale labelled incorrectly as 9 } \\ \text { instead of 0.009 etc } \\ \text { Has/should not have a broken axis or } \\ \text { does not start at zero }\end{array}$ | E2 | $\begin{array}{l}\text { oe } \\ \text { E1 for each valid error } \\ \text { eondone improvements which imply }\end{array}$ |
| :---: | :--- | :---: | :--- |
|  | Additional Guidance a title |  |  |$]$


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| 1 (c) | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $230 \div 10$ | M1 | or indicates there are 23 lots of 10 p <br> Can be implied by 69 (not 69.12) or their $69.12 \div 23$ or their $69.12 \div 230 \div$ 10 or 3.(...) |
|  | $160 \div 25 \times 10.8$ or 69.12 | M1 | Condone 9.6 instead of 10.8 |
|  | their $69.12 \div 23$ or 3 .(...) or $3 \times 23 \text { or } 69$ <br> or <br> their $69.12 \div 3$ | M1 |  |
|  | 3.(...) or $3.005(217 \ldots)$ or 3.01 and Yes or <br> 69.12 and 69 and Yes <br> or <br> 23.04 and 23 and Yes | A1 | Allow 3 with method |
|  | Alternative method 2 |  |  |
|  | $230 \div 10$ | M1 | or indicates there are 23 lots of 10 p Can be implied by $6.95(\ldots$ ) or 6.96 or 7 |
|  | $160 \div 23$ or 6.95(...) or 6.96 or 7 | M1 | g per 10p <br> 6.96 or 7 implies M2 |
|  | $10.8 \div 25 \times \text { their } 6.95(\ldots)$ <br> or $0.432 \times \text { their } 6.95(\ldots)$ | M1 | Condone 9.6 instead of 10.8 |
|  | $3 .(\ldots)$ or 3.005(217 ...) or 3.01 and Yes | A1 | Allow 3 with method |


| $\mathbf{Q}$ | Answer | Mark | Comments |
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| $\mathbf{Q}$ | Answer | Mark | Comments |
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## Main article

Give information about what the scores represent
Keep information nearer the graph it refers to

Show all data in a table format for ease of comparison

Show data/values for years between 2006 and 2012

State what OECD is
Write down the scores from previous PISA rather than saying gone up/down from previous

## Graphs

2 (a) Add a vertical axis
Add overall average PISA/OECD scores to graph(s)
Add a broken axis
Correct the title of each graph so it says 'score' not 'ranking'

Label or add units to the $x / y /$ both axes Line up the scores precisely with the horizontal lines

State what NI is
Start the vertical scales at the same point
Show the UK line in each graph for ease of comparison

Use common vertical scales (i.e. 460 to 520) or increase height of vertical axis

Use scales/grid line so can easily read the values for each year

E1 for each valid improvement

Ignore any additional but incorrect suggestions

SC1 two errors identified but no suggestions for improvement

SC2 three errors identified but no suggestions for improvement
e.g. data is not shown in table format no details for years before 2006

| $\mathbf{Q}$ | Answer | Mark | Comments |
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| 2 (b) | makes one or more statements implying critical analysis <br> and <br> gives 3.24(...)\% or 3.25\% as final answer with all errors corrected or any correct method shown <br> statements of critical analysis <br> 1. makes reference to the denominator, e.g. should be $\div 493$ (not 509) oe <br> 2. recognises that the $\%$ sign is placed incorrectly, e.g. <br> should multiply 0.0314 by 100(\%) or should not put \% sign after 0.0314 oe or allow $\times 100$ seen | B3 | B2 makes two statements implying <br> critical analysis <br> and <br> gives no or incorrect final answer or <br> B2 gives 3.24(...)\% or 3.25\% as final answer with all errors corrected or any correct method shown <br> and <br> makes no statement implying critical analysis <br> or <br> B1 makes one statement implying critical analysis <br> and <br> gives no or incorrect final answer or <br> B1 gives 3.24(...)\% or 3.25\% as final answer with no working and no statement implying critical analysis |
| :---: | :---: | :---: | :---: |
|  | Additional Guidance |  |  |
|  | No critical analysis can score maximum B2 |  |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
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| 2 (c) (i) | Alternative method 1 (Simon) |  |  |
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|  | 493 and 478 seen or $493-478 \text { or } 15$ | M1 |  |
|  | 15 and Yes | A1 |  |
|  | Alternative method 2 (Simon) |  |  |
|  | [492, 495] and $[476,479]$ seen or $[492,495]-[476,479](=[13,19])$ | M1 | Two chosen numbers must be within the given range |
|  | [13, 19] and Yes | A1 |  |
|  | Alternative method 3 (Simon) |  |  |
|  | Wales is below 480 <br> and <br> all the others/England are above 490 <br> and <br> Yes | B2 | B1 Wales is below 480 and all the others/England are above 490 |
|  | Additional Guidance |  |  |
|  | Right answer from wrong method scores MO AO eg $509-492=17$ and Yes. 509 is outside [492, 495] and 492 is outside [476, 479] |  |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
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| 2 (c) (ii) | Alternative method 1 (Rukshana) |  |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 493 \div 506(\times 100) \text { or }[0.97,0.9744] \text { or } \\ & {[97,97.44]} \\ & \text { or } \\ & 13 \div 506(\times 100) \text { or }[0.0256,0.03] \text { or } \\ & {[2.56,2.57]} \end{aligned}$ | M1 | oe |
|  | their [0.97, 0.9744] $\times 493$ <br> or $493 \text { - their }[0.0256,0.03] \times 493$ | M1 | oe |
|  | $\begin{aligned} & {[0.97,0.9744] \times 493=[478,481]} \\ & \text { and Yes } \\ & \text { or } \\ & 493-[0.0256,0.03] \times 493 \\ & =[478,481] \text { and Yes } \end{aligned}$ | A1 |  |
|  | Alternative method 2 (Rukshana) |  |  |
|  | $\begin{aligned} & {[492,495] \div[505,508](\times 100) \text { or }} \\ & {[0.968,0.98] \text { or }[96.8,98]} \\ & \text { or } \\ & {[10,16] \div[505,508](\times 100) \text { or }} \\ & {[0.0196,0.0317] \text { or }[1.96,3.17]} \end{aligned}$ | M1 | oe |
|  | ```their [0.968, 0.98] \times [492, 495] or [492, 495] - their [0.0196, 0.0317] * [492, 495]``` | M1 | oe |
|  | $\begin{aligned} & {[0.968,0.98] \times[492,495]=[476,485)} \\ & \text { and Yes } \\ & \text { or } \\ & {[492,495]-[0.0196,0.0317]} \\ & \times[492,495]=[485,485.2] \text { and No } \end{aligned}$ | A1 |  |
|  |  | nal | uidan |
|  | $[476,485) \rightarrow 476 \leq$ value $<485$ |  |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
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| 3 (a) | $\frac{28}{41}$ or $0.68(\ldots)$ or $68 .(\ldots) \%$ | B 1 | oe |
|  |  |  |  |


| Q | Answer | Mark | Comments |
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| 3 (b) | Alternative method 1 |  |  |
|  | $\frac{65}{41} \text { or } \frac{5.4}{41} \text { or } 65 \times 5.4$ | M1 | For dividing 65 or 5.4 by 41 or Multiplying 65 by 5.4 |
|  | $\frac{65}{41} \times 5.4$ | M1 | oe |
|  | 8560976 <br> or <br> 8.6 million | A1 | awrt 8.6 million |
|  | Alternative method 2 |  |  |
|  | $\frac{28+13}{491}\left(=\frac{41}{491}\right)$ | M1 |  |
|  | $5.4 \text { million } \div \frac{\text { their } 41}{491}(=64.7 \text { million })$ <br> and $\frac{13+52}{491} \times 64.7 \text { million }$ | M1 |  |
|  | 8560976 <br> or <br> 8.6 million | A1 | awrt 8.6 million |
|  | Additional Guidance |  |  |
|  | awrt 8.5 million scores M2A1 if supported by correct working |  |  |


| Q | Answer | Mark | Comments |
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|  | The survey asked adults: the rate in the <br> whole population (including children) <br> may be different <br> The rate in the population may be <br> different than the rate in the sample <br> The sample was relatively small <br> compared to the size of the population | E1 | E1 for any reasonable statement |
| 3 (c) | The survey data may be out of date <br> and so not representative of the current <br> population | Additional Guidance |  |
|  | 'survey is biased' scores E0 unless supported with a reason or reference to the population. <br> 'sample is small' or 'needs a bigger sample' scores E0 unless reference is made to the size of <br> the population (possibly implied) <br> 'some people may not be aware they have asthma' or 'misdiagnosis' scores E0 |  |  |




| Q | Answer | Mark | Comments |
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| 4 (c) (i) | 1 | B1 |  |


| Q | Answer | Mark | Comments |
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| $\mathbf{4}$ (c) (ii) | $0.35+0.30+0.06$ or <br> $1-0.08-0.21$ | M1 | P(delay of more than 1 day) |
|  | 0.71 | A1 | oe |



| Q | Answer | Mark | Comments |
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| $\mathbf{5}(\mathbf{b})$ | 4800 | B1 | ft from 5 (a) or correct |


| Q | Answer | Mark | Comments |
| :---: | :--- | :--- | :--- |
| 5 | $\frac{\text { their } 5800+\text { their } 1200}{10800}$ or $\frac{7000}{10800}$ | M1 | ft their 5 (a) for the numerator <br> Denominator must be 10800 |
|  | $\frac{35}{54}$ | A1ft | Final answer must be a fraction in its <br> lowest terms |
|  | Additional Guidance |  |  |
|  | $0.648(\ldots)$ or 0.65 implies M1A0 |  |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 5 (d) | $2 \times \frac{\text { their total in set } C}{20000} \times \frac{\text { remainder }}{19999}$ <br> or $2 \times \frac{4400}{20000} \times \frac{15600}{19999}$ <br> or $0.343(2 \ldots)$ | M1 | oe <br> Condone omission of $2 \times$ <br> Condone both denominators 20000 <br> Allow (for example) $2 \times \frac{44}{200} \times \frac{156}{200}$ |
|  | 0.34 | A1ft | ft |
|  | Additional Guidance |  |  |
|  | 0.17(16...) implies M1A0 |  |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 6 (a) | Alternative method 1 |  |  |
|  | 1-0.4 or 0.6 | M1 | Probability that whales do not appear in the 1st week (or any given week) |
|  | $0.6 \times 0.4$ or $1-0.4-0.36$ or 0.24 | M1 | Probability that whales appear in the 2nd week but not the 1st <br> Can be awarded if a quantity is multiplied by 0.6 and then by 0.4 oe |
|  | $0.6 \times 0.6$ or $1-0.4-0.24$ or 0.36 | M1 | Probability that whales do not appear in either week <br> Can be awarded if a quantity is multiplied by 0.6 and then by 0.6 oe |
|  | Option B $0.4 \times(80-200)$ or $32(-) 80$ or -48 | M1 | Contribution to expected costs if whales appear <br> Do not accept -48 from $0.24 \times-200$ |
|  | $\begin{aligned} & \text { their } 0.6 \times 50 \\ & \text { or } \\ & 30 \end{aligned}$ | M1 | Contribution to expected costs if whales do not appear <br> (in thousands or otherwise throughout) |
|  | $\begin{aligned} & \text { their }-48+30 \\ & \text { or } \\ & -18 \end{aligned}$ | M1 | Calculates expected cost of Option B by adding their two contributions <br> Do not accept -18 from $0.6 \times-30$ |


| Q | Answer | Mark | Comments |
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| 6 (a) <br> Cont. | Option C <br> their $0.24 \times(130-200)$ <br> or $31.2 \text { (-) } 48$ <br> or $\mid-16.8$ | M1 | Contribution to expected cost if whales appear in 2nd week |
|  | their $0.36 \times 100$ or 36 | M1 | Contribution to expected cost if whales do not appear in either week |
|  | their $-48+$ their $-16.8+$ their 36 or -28.8 | M1 | Calculates expected cost of Option C by adding their three contributions <br> Or: expected profit from Option $\mathrm{C}=$ expected profit from Option B + expected profit from staying an extra week if necessary $=18+0.6 \times 18$ |
|  | (Option A) £0 <br> and <br> (Option B) £18 000 <br> and <br> (Option C) £28 800 | A1 | Expected gains for all three options |
|  | Recommends Option C | E1ft | ft their gains if all three are stated |


| Q | Answer | Mark | Comments |
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| 6 (a) <br> Cont. | Alternative method 2 |  |  |
|  | $1-0.4$ or 0.6 | M1 | Probability that whales do not appear in the 1st week (or any given week) |
|  | $0.6 \times 0.4$ or $1-0.4-0.36$ or 0.24 | M1 | Probability that whales appear in the 2nd week but not the 1st <br> Can be awarded if a quantity is multiplied by 0.6 and then by 0.4 oe |
|  | $0.6 \times 0.6$ or $1-0.4-0.24$ or 0.36 | M1 | Probability that whales do not appear in either week <br> Can be awarded if a quantity is multiplied by 0.6 and then by 0.6 oe |
|  | Option B $\begin{aligned} & 0.4 \times 50+0.4 \times 30+0.6 \times 50 \\ & \text { or } \\ & 20+12+30 \end{aligned}$ <br> or $62$ | M1 | Expected cost <br> (in thousands or otherwise throughout) |
|  | $0.4 \times 200$ or 80 | M1 | Expected profit |
|  | their 80 - their 62 or 18 | M1 | Expected gain |


| Q | Answer | Mark | Comments |
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| 6 (a) <br> Cont. | Option C $\begin{aligned} & 0.4 \times 50+0.4 \times 30+\text { their } 0.24 \times 100+ \\ & \text { their } 0.24 \times 30+0.36 \times 100 \\ & \text { or } \\ & 20+12+24+7.2+36 \end{aligned}$ <br> or <br> 99.2 | M1 | Expected cost |
|  | $0.4 \times 200+$ their $0.24 \times 200$ or 128 | M1 | Expected profit |
|  | their 128 - their 99.2 or 28.8 | M1 | Expected gain |
|  | (Option A) £0 <br> and <br> (Option B) £18 000 <br> and <br> (Option C) £28 800 | A1 | Expected gains for all three options |
|  | Recommends Option C | E1ft | ft their gains if all three are stated |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 6 (a) <br> Cont. | Alternative method 3 |  |  |
|  | $1-0.4$ or 0.6 | M1 | Probability that whales do not appear in the 1st week (or any given week) |
|  | $0.6 \times 0.4$ or $1-0.4-0.36$ or 0.24 | M1 | Probability that whales appear in the 2nd week but not the 1st <br> Can be awarded if a quantity is multiplied by 0.6 and then by 0.4 oe |
|  | $0.6 \times 0.6$ or $1-0.4-0.24$ or 0.36 | M1 | Probability that whales do not appear in either week <br> Can be awarded if a quantity is multiplied by 0.6 and then by 0.6 oe |
|  | Option B $0.4 \times(200-30) \text { or } 68$ | M2 | Expected profit from seeing whales in the 1st week, not including fixed costs <br> M1 for either $0.4 \times 200$ or $0.4 \times(-) 30$ |
|  | their 68-50 or 18 | M1 | Expected gain <br> (Expected profit subtract fixed costs) |


| Q | Answer | Mark | Comments |
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| 6 (a) <br> Cont. | $\frac{\text { Option C }}{0.24 \times 170 \text { or } 40.8}$ | M1 | Expected profit from seeing whales in the 2nd week, not including fixed costs |
|  | $\begin{aligned} & 0.4 \times 50 \text { or } 20 \\ & \text { or } \\ & 0.6 \times 100 \text { or } 60 \end{aligned}$ | M1 | Expected fixed cost of staying for one week <br> Expected fixed cost of staying for two weeks |
|  | their 68 + their 40.8 - their 20 - their 60 or $28.8$ | M1 | Expected gain <br> (Expected profit from seeing whales in 1st week or 2nd week subtract expected fixed costs of staying for 1 or 2 weeks) |
|  | (Option A) £0 <br> and <br> (Option B) £18 000 <br> and <br> (Option C) £28 800 | A1 | Expected gains for all three options |
|  | Recommends Option C | E1ft | ft their gains if all three are stated |
|  | Additional Guidance |  |  |
|  | Accept working where signs are reversed consistently throughout (stating expected gains rather than costs, for example). |  |  |
|  | Probabilities may be seen in tree diagrams. |  |  |


| Q | Answer | Mark | Comments |
| :---: | :--- | :--- | :--- |
|  | don't want to risk losing $£ 100$ 000 <br> cannot afford to pay the upfront costs <br> want to get home <br> the choice may be incompatible with <br> deadlines <br> they may not have enough resources <br> to stay <br> they may want to go to another site <br> with a higher probability of whales <br> changing conditions <br> more up-to-date information becomes <br> available <br> the producer doubts the validity of the <br> estimates or expected costs <br> another benefit (e.g. accolade, lower <br> risk of loss) might become available if <br> the producer makes a different choice | E1ft | E1 for any valid reason <br> ft their answer to 6 (a) |

