## AQA

Please write clearly in block capitals.

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## Level 3 Certificate MATHEMATICAL STUDIES

## Paper 2C Graphical Techniques

## Wednesday 24 May 2017

## Materials

For this paper you must have:

- a clean copy of the Preliminary Material and Formulae Sheet (enclosed)
- a scientific calculator or a graphics calculator
- a ruler.


## Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer questions in the space provided. Do not write outside the box around each page or on blank pages.
- Show all necessary working; otherwise, marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The final answer to questions should be given to an appropriate degree of accuracy.
- You may not refer to the copy of the Preliminary Material that was available prior to this examination. A clean copy is enclosed for your use.

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $2-3$ |  |
| $4-5$ |  |
| $6-7$ |  |
| $8-9$ |  |
| $10-11$ |  |
| $12-13$ |  |
| $14-15$ |  |
| $16-17$ |  |
| TOTAL |  |

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 60 .
- You may ask for more answer or graph paper, which must be tagged securely to this answer booklet.
- The paper reference for this paper is 1350/2C.

Answer all questions in the spaces provided.

1 Oliver is researching costs for a new smartphone he is planning to buy.
He collects information from five mobile network operators.
The network operators offer the phone on a rental contract or on pay-as-you-go.
Users must also make a one-off payment for the phone.
He produces the table below.

| Operator | One-off payment for the phone | Rental cost |
| :---: | :---: | :---: |
| A | $£ 189.99$ p | $£ 25$ |
| B | $£ 129.99$ p | $£ 36$ |
| C | $£ 99.99 p$ | $£ 49$ |
| D | $£ 9999 p$ | $£ 0$ (pay-as-you-go) |

1 (a) Analyse Oliver's table, identifying two errors.
Then suggest two improvements he could make to his table.

Error 1
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Error 2
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Improvement 1
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$\qquad$
$\qquad$
Improvement 2
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1 (b) Sam works for a different mobile network operator.
She can take out a 24 -month contract which costs, before staff discount,
$£ 109.99$ one-off payment for the phone $£ 37.49$ per month rental cost.

She receives a $30 \%$ staff discount on the monthly rental cost only.
Sam does not want to spend more than $£ 700$ on the phone over the 24 months.
Should she take out the contract?
You must show your working.
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2 Use Youth Unemployment from the Preliminary Material.
2 (a) Work out the decrease, between September-November 2014 and June-August 2015, in the number of people aged 16-24 who were unemployed.

Circle your answer.

2 (b) Two newsletters contained articles about the unemployment rate of the economically active population aged 16-24 in September-November 2015

Here are the two headlines.

Unemployment rate for 16-24 year olds declines by one fifth in one year!
Always Young newsletter

## For economically active 16-24 year olds, the ratio of men to women is about 11 : 10

Dynamic Youth newsletter

Using the data given, comment on the validity of these headlines.
Always Young
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Dynamic Youth
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Question 2 continues on the next page

2 (c) An independent body overseeing the quality of government reports suggested that the briefing paper could have been improved.

Suggest three improvements for future briefing papers.

Improvement 1
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Improvement 2
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Improvement 3
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DO NOT WRITE ON THIS PAGE ANSWER IN THE SPACES PROVIDED

Turn over for the next question

3 In 2009, Usain Bolt set a world record of 9.58 seconds for the 100-metre sprint.

3 (a) Calculate Bolt's average speed when he set this world record.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ $\mathrm{ms}^{-1}$

The graph below shows the speed, $v$, in metres per second, against time, $t$, in seconds, at 10 -metre intervals during this race.


The linear equation below models Bolt's speed, $v$, in metres per second, against time, $t$, in seconds, during the first 3 seconds of the race.

$$
v=3.62 t-0.663
$$

3 (b) Write down Bolt's average acceleration during this section of the race.

Answer $\qquad$ $\mathrm{ms}^{-2}$

3 (c) Describe how Bolt's acceleration varies during the rest of the race.
$\qquad$
$\qquad$
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$\qquad$

4 A sculptor is designing a large structure in the shape of an arch.
The arch will have the shape shown by the curve below.
The points $O$ and $G$ are at ground level.


The arch can be modelled by an equation of the form

$$
y=a x^{2}+x+c
$$

where $x$ metres and $y$ metres are the horizontal and vertical distances respectively from the point $O$, and $a$ and $c$ are constants.

The points $(0,4)$ and $(2,5)$ are on the arch as shown.

4 (a) Work out the values of $a$ and $c$
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$$
a=
$$

$\qquad$ $c=$ $\qquad$

4 (b) The arch meets the ground at the point $G$
Alex estimates that the distance $O G$ is 6.5 metres.
Is this an overestimate or an underestimate?
You must show your working.
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5 A balloon is being inflated for 5 seconds.
Assume that the balloon is a sphere.
Sam investigates how the radius of the balloon changes with time as the balloon is inflated.
He plots the points on the graph below.


5 (a) Use the graph to estimate the rate at which the radius is increasing when $t=2$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer $\qquad$ $\mathrm{cms}^{-1}$

5 (b) Describe how the rate of change of the radius varies during the first 5 seconds.
$\qquad$
$\qquad$
$\qquad$

Sam then makes a table to show the volume of the balloon for different radii.
The volume, $V$, of a sphere of radius, $r$, is given by $V=\frac{4}{3} \pi r^{3}$

| Time (seconds) | Radius (cm) | Volume (cm $\left.{ }^{\mathbf{3}}\right)$ |
| :---: | :---: | :---: |
| 0 | 0.98 | 4 |
| 2 | 2.19 |  |
| 4 | 2.72 |  |

5 (c) Complete the table, giving your answers to the nearest whole number.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

5 (d) Work out the rate at which the volume of the balloon is increasing.
State the units of your answer.
$\qquad$
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$\qquad$
Answer

5 (e) The initial volume of another balloon is $4 \mathrm{~cm}^{3}$
It starts to be inflated when $t=1$
Its volume increases at a constant rate of $30 \mathrm{~cm}^{3}$ each second.
Work out the non-zero time when the two balloons have the same volume.
You may use the grid on the opposite page if you wish.
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Answer seconds

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$6 \quad$ Capacitors are used in electronic circuits.
The charge on a capacitor can increase and decrease and is measured in coulombs. In a particular circuit, the charge on a capacitor increases for one millisecond and then decreases for one millisecond.
The charge, $Q$ coulombs, at time $t$ milliseconds after the capacitor starts to charge is given by

$$
\begin{aligned}
Q=6\left(1-\mathrm{e}^{-3 t}\right) & \text { for } 0 \leqslant t \leqslant 1 \\
\text { and } \quad Q=A \mathrm{e}^{-3(t-1)} & \text { for } 1 \leqslant t \leqslant 2
\end{aligned}
$$

6 (a) Work out the charge on the capacitor when $t=0$
$\qquad$
$\qquad$
Answer $\qquad$ coulombs

6 (b) Show that $A=5.70$ correct to three significant figures.
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6 (c) Sketch a graph to show how the charge on the capacitor varies during the two millisecond period.


6 (d) The circuit designer wants the charge to be less than 4 coulombs for at least $60 \%$ of the two millisecond period.

Does the circuit satisfy this requirement?
You must show your working.
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