A

## AQA $=$

Surname

Other Names

Centre Number
Candidate Number $\qquad$
Candidate Signature
GCSE
MATHEMATICS
Higher Tier Paper 1 Non-Calculator

## 8300/1H

Tuesday 21 May 2019 Morning
Time allowed: 1 hour 30 minutes
For this paper you must have:

- mathematical instruments

You must NOT use a calculator.


At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.
[Turn over]


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## INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.


## ADVICE

In all calculations, show clearly how you work out your answer.

## DO NOT TURN OVER UNTIL TOLD TO DO SO

Answer ALL questions in the spaces provided.

1 Here are two right-angled triangles.
They are not drawn accurately.


Circle the value of $y$. [1 mark]
11
7.5
9
Work out the value of $\left(1 \frac{2}{3}\right)^{2}$

4

2

Circle your answer. [1 mark]
$1 \frac{4}{9}$
$3 \frac{1}{3}$
$2 \frac{4}{9}$
$2 \frac{7}{9}$

3 Work out the arc length, in metres, of a semicircle of radius 6 metres.

Circle your answer. [1 mark]
$3 \pi$
$6 \pi$
$12 \pi$
$18 \pi$
$4 \quad$ Circle the fraction that is equivalent to $\mathbf{4 . 6 2 5}$ [1 mark]
$\frac{39}{8}$
$\frac{37}{8}$
$\frac{185}{4}$
$\frac{17}{4}$
[Turn over]

# 5 (a) Write 0.00097 in standard form. [1 mark] 

## Answer

$\qquad$

5 (b) Work out $\frac{3 \times 10^{5}}{4 \times 10^{3}}$
Give your answer as an ordinary number. [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

## BLANK PAGE

[Turn over]


6 Anna plays a game with an ordinary, fair dice.
If she rolls 1 she wins.
If she rolls $\mathbf{2}$ or $\mathbf{3}$ she loses.
If she rolls $\mathbf{4 , 5}$ or $\mathbf{6}$ she rolls again.
When she has to roll again,
if she rolls an odd number she wins
if she rolls an even number she loses.

6 (a) Complete the tree diagram on the opposite page with the four missing probabilities. [2 marks]

First roll

> Second roll

[Turn over]


## BLANK PAGE

6 (b) Is Anna more likely to win or to lose?
You MUST work out the probability that she wins. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
[Turn over]
$7 \quad$ Three friends arrive at a party.
Their arrival increases the number of people at the party by $20 \%$

In total, how many people are now at the party?
[2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

8 Work out the value of $\left(3^{12} \div 3^{5}\right) \div\left(3^{2} \times 3\right)$ [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
[Turn over]

9 A shaded semicircle is inside a circle as shown.
It is not drawn accurately.


The RADIUS of the circle is 10 cm
The DIAMETER of the semicircle is $\mathbf{8 ~ c m}$
How many times bigger is the unshaded area than the shaded area? [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

[Turn over]
$\square$

10 The number of items, $n$, made in 1 hour by a machine is given by
$n=\frac{60}{t}$
$t$ is the time in minutes the machine takes to make one item.

The value of $\boldsymbol{t}$ changes for different types of item.

10 (a) On the grid opposite, draw the graph of $n=\frac{60}{t}$ for values of $t$ from 1 to 4
[2 marks]

Number of items, $n$, made in 1 hour


10 (b) The machine takes 3 minutes 30 seconds to make one item.

USE YOUR GRAPH to estimate the value of $n$. [2 marks]

## Answer

$\qquad$
[Turn over]

11 Ed and Fay shared $£ 330$ in the ratio $7: 4$
Ed gives Fay some of his money.
Fay now has the same amount as Ed. How much does Ed give Fay? [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer £ $\qquad$

The next term of a sequence is made by adding the previous two terms.

Which of these sequences follows this rule?
Circle your answer. [1 mark]

$$
\begin{array}{lllllllllll}
-9 & 2 & -7 & -5 & -12 & -3 & 5 & -2 & 3 & 1 & \\
0 & -3 & -3 & 0 & -3 & -1 & -1 & -2 & -3 & 1
\end{array}
$$

[Turn over]


13 The triangular cross section of a prism is an isosceles right-angled triangle.


The volume of the prism is $102 \mathrm{~cm}^{3}$
Use approximations to estimate the value of $x$.
You MUST show your working. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

[Turn over]


14 Here is a quadrilateral.
It is not drawn accurately.

$\qquad$
$\qquad$

## [Turn over]

15 Here is some information about the test marks of 120 students.

| Mark, $m$ | $0<m \leqslant 10$ | $10<m \leqslant 20$ | $20<m \leqslant 30$ | $30<m \leqslant 40$ | $40<m \leqslant 50$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 20 | 28 | 40 | 20 | 12 |

15 (a) Complete the cumulative frequency table. [1 mark]

| Mark, $m$ | $m \leqslant 10$ | $m \leqslant 20$ | $m \leqslant 30$ | $m \leqslant 40$ | $m \leqslant 50$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Cumulative <br> frequency | 20 | 48 |  |  |  |

15 (b) Draw a cumulative frequency graph. [2 marks]

[Turn over]


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15 (c) Students who scored 15 marks or fewer take another test.

Use your graph to estimate how many students take another test. [2 marks]
$\qquad$
$\qquad$
$\qquad$
Answer
[Turn over]

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16 Simplify fully $\frac{4 x-8 x^{2}}{12 x-6}$
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

## [Turn over]

17 Toby is forming and solving equations.

17 (a) The product of half of a number and three more than the number is the same as
the square of the number

Toby uses $\boldsymbol{y}$ to represent the number.
Write an equation that Toby could form.
[2 marks]

Answer $\qquad$

17 (b) Toby forms another equation.

$$
x=\frac{9}{8 x}
$$

He wants to work out the values of $x$.
Here is his working.

$$
\begin{aligned}
& x=\frac{9}{8 x} \\
& 8 x^{2}=9 \\
& 8 x=3 \text { or } 8 x=-3 \\
& x=\frac{3}{8} \text { or } x=-\frac{3}{8}
\end{aligned}
$$

What error has he made in his working? [1 mark]
[Turn over]

18 Here is an identity.

$$
x^{2}-y^{2} \equiv(x+y)(x-y)
$$

18 (a) Use the identity to work out the value of 193 ${ }^{2}$ - $7^{2}$
You MUST show your working. [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

18 (b) Factorise $100 a^{2}-81 b^{2}$
[1 mark]
Answer $\qquad$

Circle the fraction that is equivalent to 0.1
[1 mark]

| $\frac{1}{9}$ | $\frac{1}{99}$ | $\frac{1}{10}$ | $\frac{11}{100}$ |
| :--- | :--- | :--- | :--- |

[Turn over]
$20 \quad A, B$ and $C$ are points on a circle.
$C D$ is a tangent.
The diagram is not drawn accurately.


20 (a) Assume that triangle $A B C$ is isosceles with $A C=B C$

Prove that $A B$ is parallel to $D C$. [4 marks]
$\qquad$
$\qquad$

20 (b) In fact, triangle $A B C$ is equilateral.
Tick the TWO boxes for the statements that MUST be correct. [1 mark]

$A B$ is parallel to $D C$

$A C$ bisects angle $B C D$

$A C$ bisects angle $B A D$
[Turn over]

21
Solve the simultaneous equations
$2 x+3 y=5 p$
$y=2 x+p$
where $\boldsymbol{p}$ is a constant.
Give your answers in terms of $p$ in their simplest form. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

[Turn over]
$22 \quad A B C$ and $A C D$ are triangles.
$k$ is a constant.
The diagram is not drawn accurately.


22 (a) Show that $\overrightarrow{C D}=6 a+4.5 b$
[1 mark]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

22 (b) $B C D$ is a straight line.
Work out the value of $\boldsymbol{k}$.
You must show your working. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
Answer
[Turn over]
$\qquad$

Simplify $8^{4} \div 32^{\frac{2}{5}}$

Give your answer in the form $2^{m}$ where $m$ is an integer. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

$$
f(x)=\sin \left(x-90^{\circ}\right)
$$

Circle the value of $f\left(0^{\circ}\right)$
[1 mark]
$1 \begin{array}{llll}0 & -\frac{1}{2} & -1\end{array}$
$\square$
[Turn over]
$25 \quad P(4,8)$ is a point on a circle, centre $O$.

## The tangent at $P$ intersects the axes at points $A$ and $B$.

The diagram is not drawn accurately.


## 43

25 (a) Show that the gradient of the tangent is $-\frac{1}{2}$ [2 marks]

## [Turn over]

25 (b) Work out the length $A B$.
Give your answer in the form $a \sqrt{5}$ where $a$ is an integer.

You MUST show your working. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

 units26 The turning point of the graph $y=(x+a)^{2}+b$ has $x$-coordinate -2
$(3,1)$ is another point on the graph.
Work out the $y$-coordinate of the turning point. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

27 Angle $x$ is acute. $\cos x=\sin 60^{\circ} \times \tan 30^{\circ}$

Work out the size of angle $x$.
You MUST show your working. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
degrees
END OF QUESTIONS

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| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $4-6$ |  |
| $8-11$ |  |
| $12-15$ |  |
| $16-19$ |  |
| $20-23$ |  |
| $24-29$ |  |
| $30-33$ |  |
| $34-37$ |  |
| $38-41$ |  |
| $42-45$ |  |
| $46-47$ |  |
| TOTAL |  |

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