

MATHEMATICS

Higher Tier Paper 1 Non-Calculator

8300/1H

Tuesday 21 May 2019 Morning

Time allowed: 1 hour 30 minutes

For this paper you must have:

• mathematical instruments



You must NOT use a calculator.

At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.



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INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

ADVICE

In all calculations, show clearly how you work out your answer.

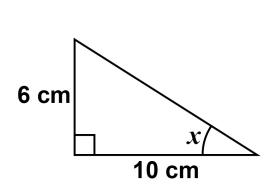
DO NOT TURN OVER UNTIL TOLD TO DO SO

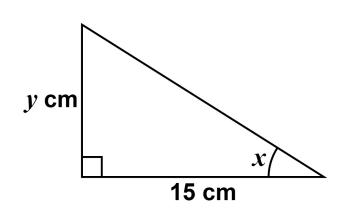


Answer ALL questions in the spaces provided.

1 Here are two right-angled triangles.

They are not drawn accurately.





Circle the value of y. [1 mark]

11

7.5

9

4

2 Work out the value of $\left(1\frac{2}{3}\right)^2$

Circle your answer. [1 mark]

$$1\frac{4}{9}$$

 $3\frac{1}{3}$

$$2\frac{4}{9}$$

 $2\frac{7}{9}$



Work out the arc length, in metres, of a semicircle of radius 6 metres.

Circle your answer. [1 mark]

 3π

 6π

 12π

 $18\,\pi$

4 Circle the fraction that is equivalent to 4.625 [1 mark]

 $\frac{39}{8}$

37 8 185 4

 $\frac{17}{4}$



5	(a)	Write	0.00097	in standard form.	[1	mark]
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	Answer
(b)	Work out $\frac{3 \times 10^5}{4 \times 10^3}$
	Give your answer as an ordinary number. [2 marks]
	Answer



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6 Anna plays a game with an ordinary, fair dice.

If she rolls 1 she wins.

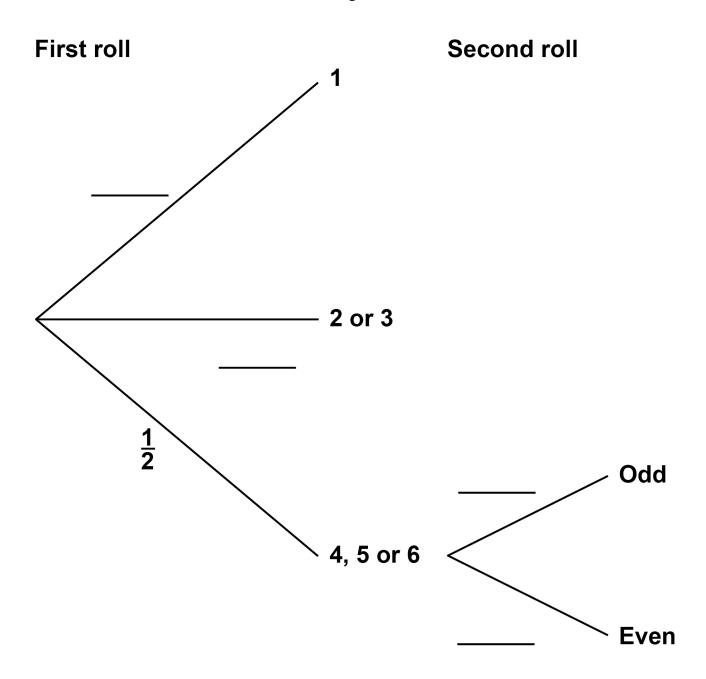
If she rolls 2 or 3 she loses.

If she rolls 4, 5 or 6 she rolls again.

When she has to roll again, if she rolls an odd number she wins if she rolls an even number she loses.

6 (a) Complete the tree diagram on the opposite page with the four missing probabilities. [2 marks]







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6 (b)	Is Anna more likely to win or to lose?
	You MUST work out the probability that she wins. [4 marks]
Turn	over]
i ui ii	6 6

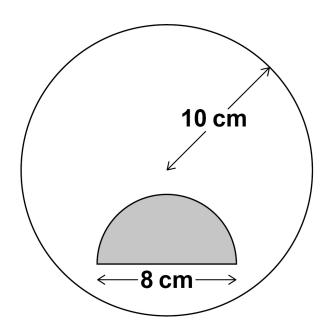


Thre	e friends arrive at a party.	
	r arrival increases the number of poarty by 20%	eople a
	tal, how many people are now at t arks]	he party





9 A shaded semicircle is inside a circle as shown.
It is not drawn accurately.



The RADIUS of the circle is 10 cm

The DIAMETER of the semicircle is 8 cm

How many times bigger is the unshaded area than the shaded area? [4 marks]





Answer	
nverl	9



The number of items, n, made in 1 hour by a machine is given by

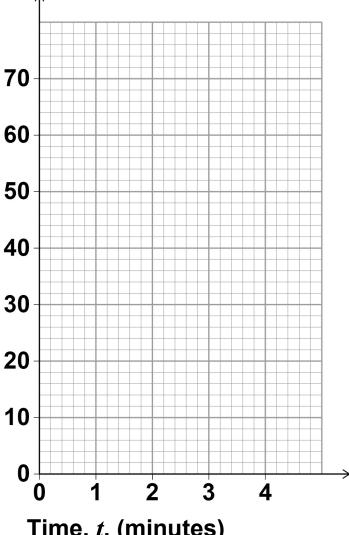
$$n=\frac{60}{t}$$

t is the time in minutes the machine takes to make one item.

The value of t changes for different types of item.

10 (a) On the grid opposite, draw the graph of $n = \frac{60}{t}$ for values of t from 1 to 4 [2 marks]

Number of items, n, made in 1 hour



Time, t, (minutes) to make one item

10 (b) The machine takes 3 minutes 30 seconds to make one item.

USE YOUR GRAPH to estimate the value of n. [2 marks]

Answer			
--------	--	--	--



Ed and Fay shared £330 in the ratio 7:4
Ed gives Fay some of his money.
Fay now has the same amount as Ed.
How much does Ed give Fay? [3 marks]



12 The next term of a sequence is made by adding the previous two terms.

Which of these sequences follows this rule?

Circle your answer. [1 mark]

-9 2 -7 -5 -12

-3 5 -2 3 1

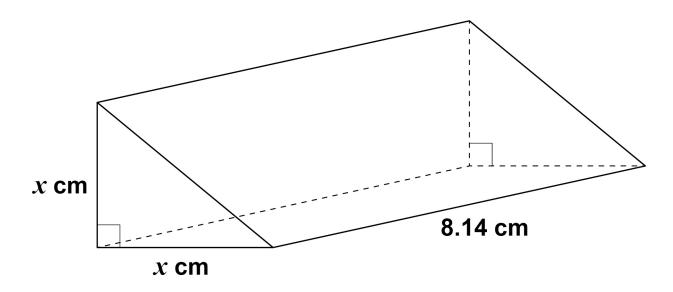
0 -3 -3 0 -3

-1 -1 -2 -3 1

8



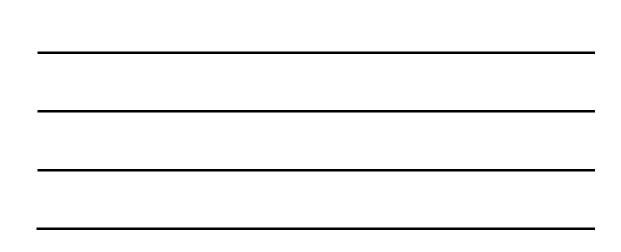
13 The triangular cross section of a prism is an isosceles right-angled triangle.



The volume of the prism is 102 cm³

Use approximations to estimate the value of x.

You MUST show your working. [3 marks]



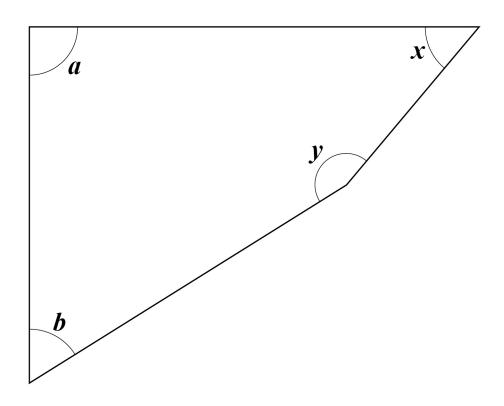


Answer		
		



14 Here is a quadrilateral.

It is not drawn accurately.



 $a = 90^{\circ}$ and a : b = 5 : 3

x: y = 1:3

Show that b = x

[3 marks]





15 Here is some information about the test marks of 120 students.

Mark, m	0 < <i>m</i> ≤ 10	10 < <i>m</i> ≤ 20	$20 < m \leqslant 30$	$30 < m \leqslant 40$	40 < <i>m</i> ≤ 50
Frequency	20	28	40	20	12

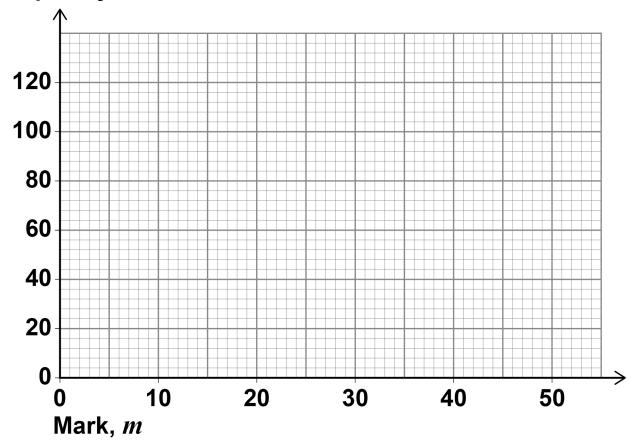
15 (a) Complete the cumulative frequency table. [1 mark]

Mark, m	<i>m</i> ≤ 10	<i>m</i> ≤ 20	<i>m</i> ≤ 30	<i>m</i> ≤ 40	<i>m</i> ≤ 50
Cumulative frequency	20	48			

24

15 (b) Draw a cumulative frequency graph. [2 marks]

Cumulative frequency





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15 (c)	Students who scored 15 marks or fewer take another test.				
	Use your graph to estimate how many students take another test. [2 marks]				

Answer ____



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[3 marks] Answer	5	Simplify fully $\frac{4x-8x^2}{12x-6}$	
Answer		[3 marks]	
Answer			
		Answer	
ırn over]			



17	Toby is forming and solving equations.
17 (a)	The product of half of a number and three more than the number
	is the same as
	the square of the number
	Toby uses y to represent the number.
	Write an equation that Toby could form. [2 marks]
	Answer



17 (b) Toby forms another equation.

$$x = \frac{9}{8x}$$

He wants to work out the values of x.

Here is his working.

$$x = \frac{9}{8x}$$

 $8x^2 = 9$
 $8x = 3 \text{ or } 8x = -3$
 $x = \frac{3}{8} \text{ or } x = -\frac{3}{8}$

What error has he made in his working? [1 mark]



18 Here is an identity.

$$x^2 - y^2 \equiv (x + y)(x - y)$$

18 (a) Use the identity to work out the value of $193^2 - 7^2$

You MUST show your working. [2 marks]

Answer			

18 (b) Factorise $100a^2 - 81b^2$ [1 mark]

Answer



19 Circle the fraction that is equivalent to 0.1 [1 mark]

9

10

100

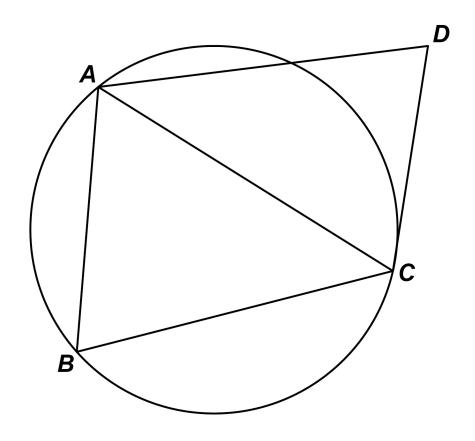
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20 A, B and C are points on a circle.

CD is a tangent.

The diagram is not drawn accurately.



20 (a) Assume that triangle ABC is isosceles with AC = BC

Prove that AB is parallel to DC. [4 marks]



20 (b)	In fact, triangle <i>ABC</i> is equilateral.
	Tick the TWO boxes for the statements that MUST be correct. [1 mark]
	AB is parallel to DC
	AC bisects angle BCD
	AC bisects angle BAD
Turn o	worl



21	Solve the simultaneous equations
	2x + 3y = 5p
	y = 2x + p
	where p is a constant.
	Give your answers in terms of p in their simplest form. [4 marks]



x = y =			
x = y =		 	
x = y =		 	
x = y =		 	
	x =	y =	

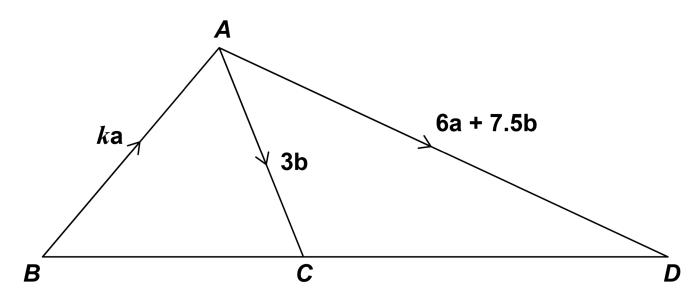




22 ABC and ACD are triangles.

k is a constant.

The diagram is not drawn accurately.



22 (a) Show that $\overrightarrow{CD} = 6a + 4.5b$ [1 mark]



22 (b)	BCD is a straight line.			
	Work out the value of k .			
	You must show your working. [3 marks]			
	A			
	Answer			

[Turn over]



23	Simplify	84 ÷	32

Give your answer in the form an integer. [3 marks]	m 2^m where m is	
Answer		



24
$$f(x) = \sin(x - 90^{\circ})$$

Circle the value of f(0°)

[1 mark]

1

0

 $-\frac{1}{2}$

–1

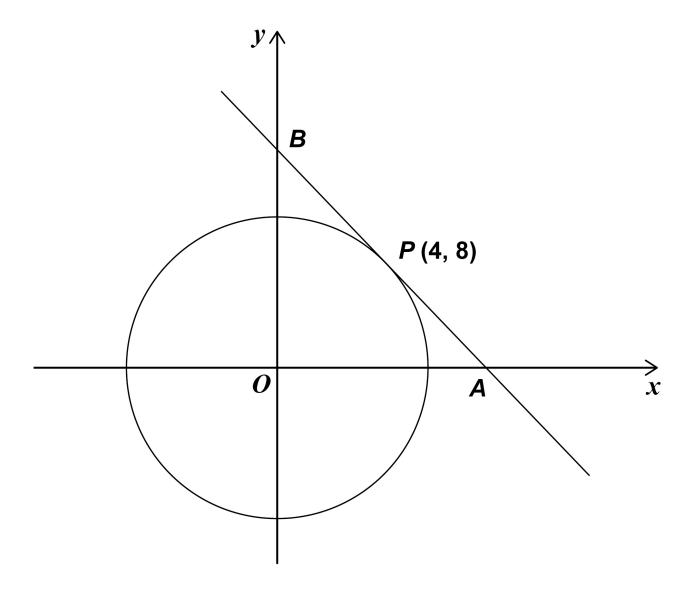
[Turn over]



25 P(4, 8) is a point on a circle, centre O.

The tangent at *P* intersects the axes at points *A* and *B*.

The diagram is not drawn accurately.





25 (a)	Show that the gradient of the tangent is $-\frac{1}{2}$ [2 marks]

[Turn over]



25 (b)	Work out the length <i>AB</i> .
	Give your answer in the form $a\sqrt{5}$ where a is an integer.
	You MUST show your working. [4 marks]



	Answer _			_ uni	ts
lTurn ov	erl				



The turning point of the graph $y = (x + a)^2 + b$ has x-coordinate -2
(3, 1) is another point on the graph.
Work out the y -coordinate of the turning point. [3 marks]
Answer



27	Angle x is acute.	
	$\cos x = \sin 60^{\circ} \times \tan 30^{\circ}$	
	Work out the size of angle x .	
	You MUST show your working. [3 marks]	
		_
		_
		_
		_
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		_
		_
	Answer degrees	
END O	QUESTIONS]
	6	



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For Examiner's Use		
Pages	Mark	
4–6		
8–11		
12–15		
16–19		
20–23		
24–29		
30–33		
34–37		
38–41		
42–45		
46–47		
TOTAL		

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