AQA

## Surname

Other Names
Centre Number
Candidate Number
Candidate Signature
GCSE
MATHEMATICS
Higher Tier Paper 1 Non-Calculator 8300/1H

Tuesday 21 May 2019 Morning
Time allowed: 1 hour 30 minutes
At the top of the page, write your surname and other names, your centre number, your candidate number and add your signature.
[Turn over]

## 2

For this paper you must have:

- mathematical instruments

You must NOT use a calculator.


## INSTRUCTIONS

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer ALL questions.
- You must answer the questions in the spaces provided. Do not write on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## INFORMATION

- The marks for questions are shown in brackets.
- The maximum mark for this paper is $\mathbf{8 0}$.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

ADVICE
In all calculations, show clearly how you work out your answer.

DO NOT TURN OVER UNTIL TOLD TO DO SO

Answer ALL questions in the spaces provided.

1
Here are two right-angled triangles.
They are not drawn accurately.


15 cm

## 5

## Circle the value of $y$. [1 mark]

11
7.5
9
4

## 2

Work out the value of $\left(1 \frac{2}{3}\right)^{2}$
Circle your answer. [1 mark]
$1 \frac{4}{9}$
$3 \frac{1}{3}$
$2 \frac{4}{9}$
$2 \frac{7}{9}$

3
Work out the arc length, in metres, of a semicircle of radius 6 metres.

Circle your answer. [1 mark]
$3 \pi$
[Turn over]


6
4
Circle the fraction that is equivalent to 4.625
[1 mark]
$\frac{39}{8}$
$\frac{37}{8}$
$\frac{185}{4}$
$\frac{17}{4}$

5 (a)
Write 0.00097 in standard form.
[1 mark]

Answer

## 7

5 (b)
Work out $\frac{3 \times 10^{5}}{4 \times 10^{3}}$

Give your answer as an ordinary number. [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
[Turn over]
7

Anna plays a game with an ordinary, fair dice.

If she rolls 1 she wins.
If she rolls 2 or $\mathbf{3}$ she loses.
If she rolls 4,5 or $\mathbf{6}$ she rolls again.
When she has to roll again,
if she rolls an odd number she wins
if she rolls an even number she loses.

6 (a)
Complete the tree diagram on the opposite page with the four missing probabilities. [2 marks]

First roll

## Second roll



## [Turn over]

## BLANK PAGE

Is Anna more likely to win or to lose?
You MUST work out the probability that she wins. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
[Turn over]

## 7

Three friends arrive at a party.
Their arrival increases the number of people at the party by $20 \%$

In total, how many people are now at the party? [2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

8
Work out the value of $\left(3^{12} \div 3^{5}\right) \div\left(3^{2} \times 3\right)$ [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
[Turn over]

## 9

A shaded semicircle is inside a circle as shown.

It is not drawn accurately.


The RADIUS of the circle is $\mathbf{1 0 ~ c m}$
The DIAMETER of the semicircle is $\mathbf{8} \mathbf{c m}$

## How many times bigger is the unshaded area than the shaded area? [4 marks]

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

## [Turn over]

The number of items, $n$, made in 1 hour by a machine is given by
$n=\frac{60}{t}$
$t$ is the time in minutes the machine takes to make one item.

The value of $\boldsymbol{t}$ changes for different types of item.

10 (a)
On the grid opposite, draw the graph
of $n=\frac{60}{t}$ for values of $t$ from 1 to 4
[2 marks]

Number of items, $n$, made in 1 hour

[Turn over]

## BLANK PAGE

10 (b)
The machine takes 3 minutes 30 seconds to make one item.

USE YOUR GRAPH, on page 17, to estimate the value of $n$. [2 marks]

## Answer

[Turn over]

## 20

## 11

Ed and Fay shared $£ 330$ in the ratio $7: 4$
Ed gives Fay some of his money.
Fay now has the same amount as Ed. How much does Ed give Fay? [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer £

## 21

The next term of a sequence is made by adding the previous two terms.

Which of these sequences follows this rule?

Circle your answer. [1 mark]
$\begin{array}{llllllllll}-9 & 2 & -7 & -5 & -12 & -3 & 5 & -2 & 3 & 1\end{array}$
$\begin{array}{llllllllll}0 & -3 & -3 & 0 & -3 & -1 & -1 & -2 & -3 & 1\end{array}$
[Turn over]


The triangular cross section of a prism is an isosceles right-angled triangle.


The volume of the prism is $102 \mathrm{~cm}^{3}$

Use approximations to estimate the value of $x$.
You MUST show your working. [3 marks]

Answer
[Turn over]

24
14
Here is a quadrilateral.
It is not drawn accurately.


$$
x: y=1: 3
$$



25
Show that $\boldsymbol{b}=\boldsymbol{x}$
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## [Turn over]

## 26

15
Here is some information about the test marks of 120 students.

| Mark, $m$ | Frequency |
| :--- | :--- |
| $0<m \leqslant 10$ | 20 |
| $10<m \leqslant 20$ | 28 |
| $20<m \leqslant 30$ | 40 |
| $30<m \leqslant 40$ | 20 |
| $40<m \leqslant 50$ | 12 |

## 27

15 (a)
Complete the cumulative frequency table. [1 mark]

| Mark, $m$ | Cumulative <br> frequency |
| :--- | :--- |
| $m \leqslant 10$ | 20 |
| $m \leqslant 20$ | 48 |
| $m \leqslant 30$ |  |
| $m \leqslant 40$ |  |
| $m \leqslant 50$ |  |

15 (b)
Draw a cumulative frequency graph on page 29. [2 marks]
[Turn over]

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## Cumulative frequency



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15 (c)
Students who scored 15 marks or fewer take another test.
Use your graph, on page 29, to estimate how many students take another test. [2 marks]
$\qquad$
$\qquad$

Answer
[Turn over]

32

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Simplify fully $\frac{4 x-8 x^{2}}{12 x-6}$
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer
[Turn over]

## Toby is forming and solving equations.

17 (a)
The product of half of a number and three more than the number
is the same as
the square of the number

Toby uses $y$ to represent the number.
Write an equation that Toby could form. [2 marks]

## Answer

17 (b)
Toby forms another equation.
$x=\frac{9}{8 x}$
He wants to work out the values of $x$.
Here is his working.

$$
\begin{aligned}
& x=\frac{9}{8 x} \\
& 8 x^{2}=9 \\
& 8 x=3 \text { or } 8 x=-3 \\
& x=\frac{3}{8} \text { or } x=-\frac{3}{8}
\end{aligned}
$$

What error has he made in his working? [1 mark]

36
18
Here is an identity.
$x^{2}-y^{2} \equiv(x+y)(x-y)$
18 (a)
Use the identity to work out the value of 1932-72

You MUST show your working. [2 marks]

Answer

37
18 (b)
Factorise $\quad 100 a^{2}-81 b^{2}$
[1 mark]
Answer

19
Circle the fraction that is equivalent to 0.1 [1 mark]
$\begin{array}{llll}\frac{1}{9} & \frac{1}{99} & \frac{1}{10} & \frac{11}{100}\end{array}$
[Turn over]
7

20
$A, B$ and $C$ are points on a circle.
$C D$ is a tangent.
The diagram is not drawn accurately.


Assume that triangle $A B C$ is isosceles with $A C=B C$

Prove that $A B$ is parallel to $D C$. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
[Turn over]

20 (b)

## In fact, triangle $A B C$ is equilateral.

Tick the TWO boxes for the statements that MUST be correct. [1 mark]
$A B$ is parallel to $D C$
$A C$ bisects angle $B C D$
$A C$ bisects angle $B A D$

21
Solve the simultaneous equations
$2 x+3 y=5 p$
$y=2 x+p$
where $p$ is a constant.

## 41

Give your answers in terms of $p$ in their simplest form. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$ $x=\quad y=$

22
$A B C$ and $A C D$ are triangles.
$k$ is a constant.
The diagram is not drawn accurately.


22 (a)

## Show that $\overrightarrow{C D}=6 a+4.5 b$

[1 mark]
[Turn over]

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22 (b)
$B C D$ is a straight line.
Work out the value of $\boldsymbol{k}$.
You MUST show your working. [3 marks]

## $\stackrel{\rightharpoonup}{\mathcal{G}}$

Answer
[Turn over]
|||l|l||||||||

46
23
Simplify $8^{4} \div 32^{\frac{2}{5}}$

Give your answer in the form $2^{m}$ where $m$ is an integer. [3 marks]

Answer

## 47

24
$f(x)=\sin \left(x-90^{\circ}\right)$
Circle the value of $f\left(0^{\circ}\right)$
[1 mark]
1
$0 \quad-\frac{1}{2}$
-1

8

## [Turn over]

## 48

25
$P(4,8)$ is a point on a circle, centre $O$.
The tangent at $P$ intersects the axes at points $A$ and $B$.

The diagram is not drawn accurately.


49
25 (a)
Show that the gradient of the tangent is
$-\frac{1}{2}$
[2 marks]
[Turn over]

## Work out the length $A B$.

Give your answer in the form $a \sqrt{5}$ where $a$ is an integer.

You MUST show your working. [4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

51

Answer
units
$\square$
[Turn over]

52
26
The turning point of the graph $y=(x+a)^{2}+b$ has $x$-coordinate -2
$(3,1)$ is another point on the graph.
Work out the $y$-coordinate of the turning point. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$ Answer

53
27
Angle $x$ is acute.
$\cos x=\sin 60^{\circ} \times \tan 30^{\circ}$
Work out the size of angle $x$.
You MUST show your working. [3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## END OF QUESTIONS

## 54

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| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $4-7$ |  |
| $8-11$ |  |
| $12-15$ |  |
| $16-21$ |  |
| $22-25$ |  |
| $26-33$ |  |
| $34-37$ |  |
| $38-41$ |  |
| $42-47$ |  |
| $48-51$ |  |
| $52-53$ |  |
| TOTAL |  |

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