

GCE A2

Mathematics

January 2010

Mark Schemes

Issued: April 2010

**NORTHERN IRELAND GENERAL CERTIFICATE OF SECONDARY EDUCATION (GCSE)
AND NORTHERN IRELAND GENERAL CERTIFICATE OF EDUCATION (GCE)**

MARK SCHEMES (2010)

Foreword

Introduction

Mark Schemes are published to assist teachers and students in their preparation for examinations. Through the mark schemes teachers and students will be able to see what examiners are looking for in response to questions and exactly where the marks have been awarded. The publishing of the mark schemes may help to show that examiners are not concerned about finding out what a student does not know but rather with rewarding students for what they do know.

The Purpose of Mark Schemes

Examination papers are set and revised by teams of examiners and revisers appointed by the Council. The teams of examiners and revisers include experienced teachers who are familiar with the level and standards expected of 16- and 18-year-old students in schools and colleges. The job of the examiners is to set the questions and the mark schemes; and the job of the revisers is to review the questions and mark schemes commenting on a large range of issues about which they must be satisfied before the question papers and mark schemes are finalised.

The questions and the mark schemes are developed in association with each other so that the issues of differentiation and positive achievement can be addressed right from the start. Mark schemes therefore are regarded as a part of an integral process which begins with the setting of questions and ends with the marking of the examination.

The main purpose of the mark scheme is to provide a uniform basis for the marking process so that all the markers are following exactly the same instructions and making the same judgements in so far as this is possible. Before marking begins a standardising meeting is held where all the markers are briefed using the mark scheme and samples of the students' work in the form of scripts. Consideration is also given at this stage to any comments on the operational papers received from teachers and their organisations. During this meeting, and up to and including the end of the marking, there is provision for amendments to be made to the mark scheme. What is published represents this final form of the mark scheme.

It is important to recognise that in some cases there may well be other correct responses which are equally acceptable to those published: the mark scheme can only cover those responses which emerged in the examination. There may also be instances where certain judgements may have to be left to the experience of the examiner, for example, where there is no absolute correct response – all teachers will be familiar with making such judgements.

The Council hopes that the mark schemes will be viewed and used in a constructive way as a further support to the teaching and learning processes.

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Rewarding Learning

ADVANCED
General Certificate of Education
January 2010

Mathematics

Assessment Unit C3

assessing

Module C3: Core Mathematics 3

[AMC31]

FRIDAY 15 JANUARY, AFTERNOON

MARK SCHEME

1 (a) $\frac{x^2 + x - 12}{x^2 - 16} \times \frac{x^2 - 4x}{x - 3}$
 $= \frac{(x+4)(x-3)}{(x+4)(x-4)} \times \frac{x(x-4)}{x-3}$
 $= x$

M1

AVAILABLE
MARKS

M1W1W1

MW1

(b) $\frac{3x+3}{(x-1)(x+2)} = \frac{A}{x-1} + \frac{B}{x+2}$
 $3x+3 = A(x+2) + B(x-1)$

M1W1

MW1

Let $x = -2$ $-3 = -3B$

M1

$B = 1$

W1

Let $x = 1$ $6 = 3A$

$A = 2$

MW1

11

$\frac{3x+3}{(x-1)(x+2)} = \frac{2}{x-1} + \frac{1}{x+2}$

2 $h = 1$

MW1

x	y
0	1
1	0.5
2	0.111111
3	0.0357143
4	0.0153846

W1

W2

$\int \approx \frac{1}{3}h[y_0 + 4(y_1 + y_3) + 2y_2 + y_4]$
 $= \frac{1}{3}[1 + 2.142857 + 0.222222 + 0.0153846]$
 $= 1.1268 = 1.13$ (3 s.f.)

M1

W1

6

3 (a) $= (1 - x^2)^{\frac{1}{2}}$

$= 1 + \left(\frac{1}{2}\right)(-x^2) + \frac{\frac{1}{2}\left(-\frac{1}{2}\right)}{1.2} (-x^2)^2 + \dots$

$= 1 - \frac{1}{2}x^2 - \frac{1}{8}x^4 + \dots$

MW1

MW4

W1

(b) $|\ln x| = 3$

$\ln x = 3$ or $\ln x = -3$

$x = e^3$ or $x = e^{-3}$

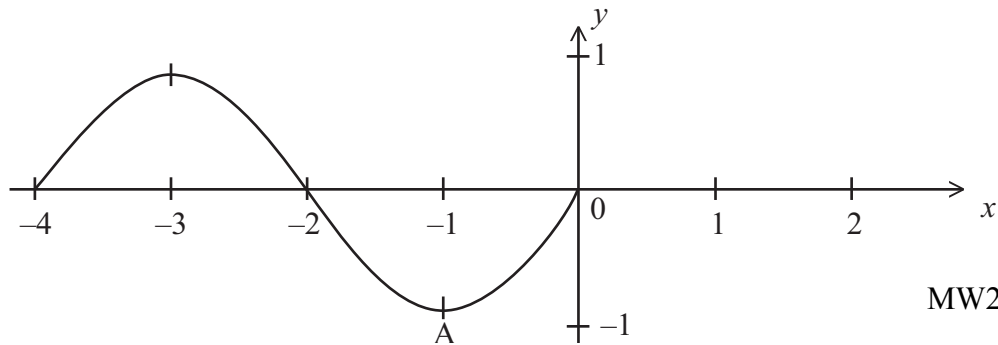
M1W2

MW2

AVAILABLE
MARKS

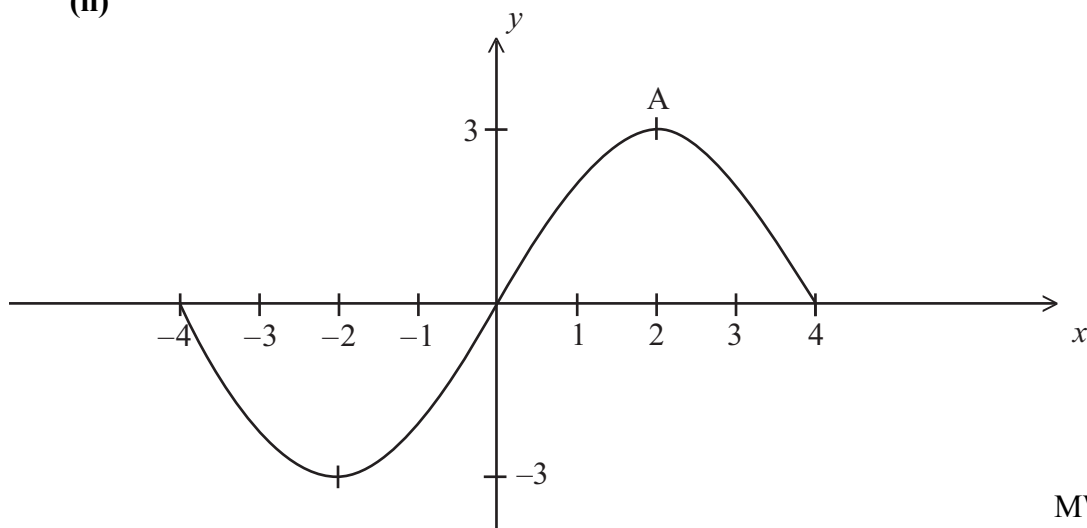
11

4 (i)



MW2

(ii)



MW2

4

			AVAILABLE MARKS
5 (a) (i)	$y = (3x^2 - 4)^6$ $\frac{dy}{dx} = 6(3x^2 - 4)^5(6x)$ $= 36x(3x^2 - 4)^5$	MW3	
(ii)	$u = \ln x \quad \frac{du}{dx} = \frac{1}{x}$ $v = x^2 - 1 \quad \frac{dv}{dx} = 2x$ $\frac{dy}{dx} = \frac{\frac{1}{x}(x^2 - 1) - 2x \ln x}{(x^2 - 1)^2}$ $= \frac{x^2 - 1 - 2x^2 \ln x}{x(x^2 - 1)^2}$	MW1 MW1 M1 W1	
ALTERNATIVE SOLUTION			
	$u = \ln x \quad \frac{du}{dx} = \frac{1}{x}$ $v = (x^2 - 1)^{-1} \quad \frac{dv}{dx} = -(x^2 - 1)^{-2}(2x)$ $\frac{dy}{dx} = -2x(x^2 - 1)^{-2} \ln x + \frac{1}{x}(x^2 - 1)^{-1}$ $= \frac{-2x^2 \ln x + x^2 - 1}{x(x^2 - 1)^2}$	MW1 MW1 M1 W1	
(b)	$\int \left(\frac{5}{x} - \cos 2x + \operatorname{cosec}^2 x - 2x \right) dx$ $5 \ln x - \frac{1}{2} \sin 2x - \cot x - x^2 + c$	MW5	12
6 (i)	$H = 10 + 60e^0 = 70^\circ$	M1W1	
(ii)	$20 = 10 + 60e^{-30k}$ $e^{-30k} = \frac{1}{6}$ $k = -\frac{1}{30} \ln \frac{1}{6}$ $k = 0.0597253$ $= 0.0597$	MW1 M1W1 W1	
(iii)	$\frac{dH}{dt} = -60ke^{-kt}$ $t = 60 \quad \frac{dH}{dt} = -0.099542^\circ \text{ s}^{-1}$ $= -0.0995^\circ \text{ s}^{-1}$	M1W1 M1 W1	10

		AVAILABLE MARKS
7	<p>(a) $\text{LHS} = \text{cosec}^2 \theta + \sec^2 \theta$</p> $= \frac{1}{\sin^2 \theta} + \frac{1}{\cos^2 \theta}$ $= \frac{\cos^2 \theta + \sin^2 \theta}{\sin^2 \theta \cos^2 \theta}$ $= \frac{1}{\sin^2 \theta \cos^2 \theta}$ $= \text{cosec}^2 \theta \sec^2 \theta \equiv \text{RHS}$	M1W1 M1W1 MW1 W1
	<p>(b) $3 \tan^2 x - 5 \sec x + 1 = 0$</p> $3(\sec^2 x - 1) - 5 \sec x + 1 = 0$ $3 \sec^2 x - 5 \sec x - 2 = 0$ $(3 \sec x + 1)(\sec x - 2) = 0$ $\sec x = -\frac{1}{3} \text{ or } \sec x = 2$ $\cos x = -3 \text{ or } \cos x = \frac{1}{2}$ $\text{No solution } x = \pm \frac{\pi}{3}$	M1W1 M1 W1 M1 MW2
8	<p>(i) $\frac{1}{\sin \theta} = 3 - x \quad \sin \theta = \frac{1}{3 - x}$</p> $\cos \theta = \frac{y}{2}$ $\sin^2 \theta + \cos^2 \theta = 1$ $\frac{1}{(3 - x)^2} + \frac{y^2}{4} = 1$	M1W1 M1W1
	<p>(ii) $y = 0 \Rightarrow \cos \theta = 0 \Rightarrow \theta = \pm \frac{\pi}{2}$</p> $x = 3 - \frac{1}{\sin \theta} = 3 \pm 1 \therefore A(2, 0)$	M1W1 W1
	<p>ALTERNATIVE SOLUTION</p> $y = 0 \Rightarrow \frac{1}{(3 - x)^2} = 1 \Rightarrow x = 2, 4 \therefore A(2, 0)$ $-2 \leq 2 \cos \theta \leq 2$ $L : y = 2$	M1W2 MW1
	Total	8
		75



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Mathematics

Assessment Unit C4

assessing

Module C4: Core Mathematics 4

[AMC41]

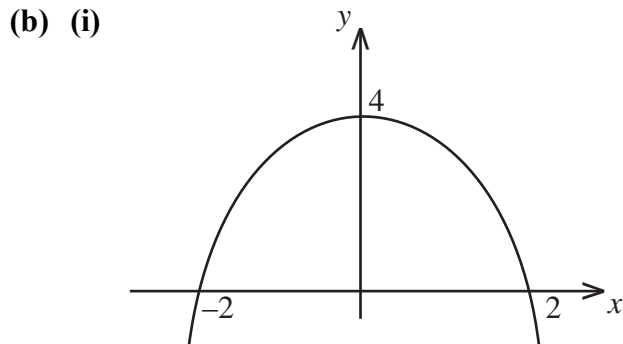
FRIDAY 29 JANUARY, MORNING

MARK SCHEME

- 1 (i) $\overrightarrow{AC} = \overrightarrow{AO} + \overrightarrow{OC}$ M1
 $\overrightarrow{AC} = -6\mathbf{i} + 2\mathbf{j} + \mathbf{k}$ W1
 $\mathbf{r} = 2\mathbf{i} + 3\mathbf{j} + \mathbf{k} + \lambda(-6\mathbf{i} + 2\mathbf{j} + \mathbf{k})$ M1W1
- (ii) $\overrightarrow{OB} = \overrightarrow{OA} + \overrightarrow{AB} = \overrightarrow{OA} + \overrightarrow{OC}$ M1
 $\overrightarrow{OB} = -2\mathbf{i} + 8\mathbf{j} + 3\mathbf{k}$ W1
- (iii) $\overrightarrow{OB} \cdot \overrightarrow{AC} = |\overrightarrow{OB}| \times |\overrightarrow{AC}| \times \cos \theta$ M1M1
 $12 + 16 + 3 = \sqrt{77} \times \sqrt{41} \times \cos \theta$ MW2
 $\theta = 56.5^\circ$ W1

11

- 2 (a) $g(x)$ is a function MW1
 $h(x)$ is a 1 – many mapping MW1
 $h(2) = 8$ or $h(2) = 9$



M1W1

- (ii) $f(x) \leq 4$ MW1

- (iii) $a(x) = 4 - x$ $x \in \mathbb{R}$ M1
 $b(x) = x^2$ $x \in \mathbb{R}$ W2

8

- 3 (i) $R \sin(\theta + \alpha) = R(\sin \theta \cos \alpha + \cos \theta \sin \alpha) = 8 \sin \theta + 6 \cos \theta$ M1
 $R \cos \alpha = 8$ and $R \sin \alpha = 6$
 $\tan \alpha = 0.75$ $\alpha = 0.64350 \approx 0.644$ (3 s.f.) MW1
 $R = 10$ MW1

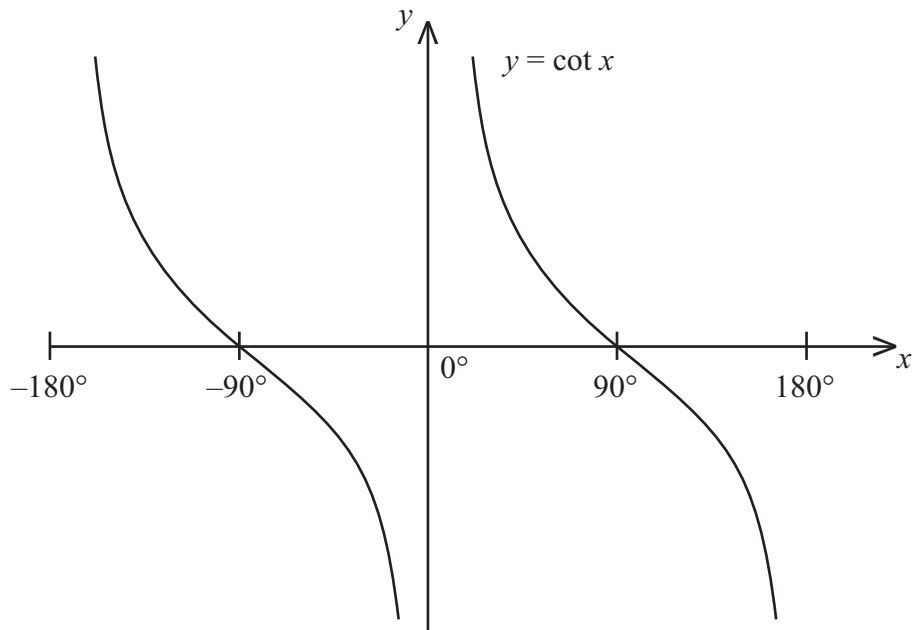
- (ii) Max value = 10 MW1
 Min value = -10 MW1

- (iii) $15 + 8 \sin 2t + 6 \cos 2t = 15 + 10 \sin(2t + 0.64350)$ M1
 Lowest point when $10 \sin(2t + 0.64350) = -10$ M1
 $(2t + 0.64350) = \frac{3\pi}{2}$ W1
 $t = 0.46365 \approx 0.464$ secs W1

9

<p>4 (i) $3x^2 - 3x^2 \frac{dy}{dx} - 6xy + 4y \frac{dy}{dx} = 0$ $\frac{dy}{dx} = \frac{6xy - 3x^2}{4y - 3x^2}$</p>	M2W3	
<p>(ii) At (1, 2) $m = \frac{12 - 3}{8 - 3} = \frac{9}{5}$ $(y - 2) = \frac{9}{5}(x - 1)$ $5y = 9x + 1$</p>	MW1 M1W1	8
<p>5 $\int x^2 dx = \frac{4}{\sin^2 \theta} d\theta$ $\int x^2 dx = \int 4 \operatorname{cosec}^2 \theta d\theta$ $\frac{1}{3} x^3 = -4 \cot \theta + c$ $x = 3, \theta = \frac{\pi}{4} \Rightarrow 9 = -4 + c$ $c = 13$ $x^3 = 39 - 12 \cot \theta$</p>	M2W1 MW2 M1	
<p>6 $V = \int_0^{\pi} \pi \sin^2 x dx$ $\sin^2 x = \frac{1}{2} (1 - \cos 2x)$ $V = \frac{\pi}{2} \int_0^{\pi} (1 - \cos 2x) dx$ $V = \frac{\pi}{2} \left[x - \frac{1}{2} \sin 2x \right]_0^{\pi}$ $V = \frac{\pi^2}{2}$</p>	M2W1 M1W1 MW2 M1W1	7 9

7 (a)



M1W1

(b) LHS = $\frac{1}{\sin 2\theta} + \frac{\cos 2\theta}{\sin 2\theta}$

MW1

$$\frac{1 + \cos 2\theta}{\sin 2\theta}$$

MW1

$$\frac{1 + 2 \cos^2 \theta - 1}{2 \sin \theta \cos \theta}$$

MW2

$$\frac{2 \cos^2 \theta}{2 \sin \theta \cos \theta}$$

W1

= $\cot \theta$ = R.H.S.

M1W1

9

<p>8 (a) $u = \ln 3x$ $\frac{dv}{dx} = 2x^4$</p> <p>$\frac{du}{dx} = \frac{1}{x}$ $v = \frac{2}{5}x^5$</p> <p>$= \frac{2}{5}x^5 \ln 3x - \int \frac{2}{5}x^4 dx$</p> <p>$= \frac{2}{5}x^5 \ln 3x - \frac{2}{25}x^5 + c$</p>	<p>M1</p> <p>W2</p> <p>M1W1</p> <p>MW1</p>
<p>(b) $\frac{x+9}{3-2x-x^2} = \frac{A}{3+x} + \frac{B}{1-x}$</p> <p>$x+9 = A(1-x) + B(x+3)$</p> <p>$x=1 \Rightarrow 10 = 4B \Rightarrow B = \frac{5}{2}$</p> <p>$x=-3 \quad 6 = 4A \quad A = \frac{3}{2}$</p> <p>$\int \frac{x+9}{3-2x-x^2} dx = \int \frac{3}{2(x+3)} dx + \int \frac{5}{2(1-x)} dx$</p> <p>$= \frac{3}{2} \ln(x+3) - \frac{5}{2} \ln(1-x) + c$</p>	<p>M1</p> <p>M1</p> <p>M1</p> <p>W1</p> <p>M1</p> <p>MW3</p>

Total

14

75



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Mathematics

Assessment Unit F2

assessing

Module FP2: Further Pure Mathematics 2

[AMF21]

WEDNESDAY 3 FEBRUARY, MORNING

**MARK
SCHEME**

GCE Advanced/Advanced Subsidiary (AS) Mathematics

Mark Schemes

Introduction

The mark scheme normally provides the most popular solution to each question. Other solutions given by candidates are evaluated and credit given as appropriate; these alternative methods are not usually illustrated in the published mark scheme.

The marks awarded for each question are shown in the right hand column and they are prefixed by the letters **M**, **W** and **MW** as appropriate. The key to the mark scheme is given below:

M indicates marks for correct method.

W indicates marks for correct working.

MW indicates marks for combined method and working.

The solution to a question gains marks for correct method and marks for an accurate working based on this method. Where the method is not correct no marks can be given.

A later part of a question may require a candidate to use an answer obtained from an earlier part of the same question. A candidate who gets the wrong answer to the earlier part and goes on to the later part is naturally unaware that the wrong data is being used and is actually undertaking the solution of a parallel problem from the point at which the error occurred. If such a candidate continues to apply correct method, then the candidate's individual working must be followed through from the error. If no further errors are made, then the candidate is penalised only for the initial error. Solutions containing two or more working or transcription errors are treated in the same way. This process is usually referred to as "follow-through marking" and allows a candidate to gain credit for that part of a solution which follows a working or transcription error.

Positive marking:

It is our intention to reward candidates for any demonstration of relevant knowledge, skills or understanding. For this reason we adopt a policy of **following through** their answers, that is, having penalised a candidate for an error, we mark the succeeding parts of the question using the candidates' value or answers and award marks accordingly.

Some common examples of this occur in the following cases:

- (a) a numerical error in one entry in a table of values might lead to several answers being incorrect, but these might not be essentially separate errors;
- (b) readings taken from candidates' inaccurate graphs may not agree with the answers expected but might be consistent with the graphs drawn.

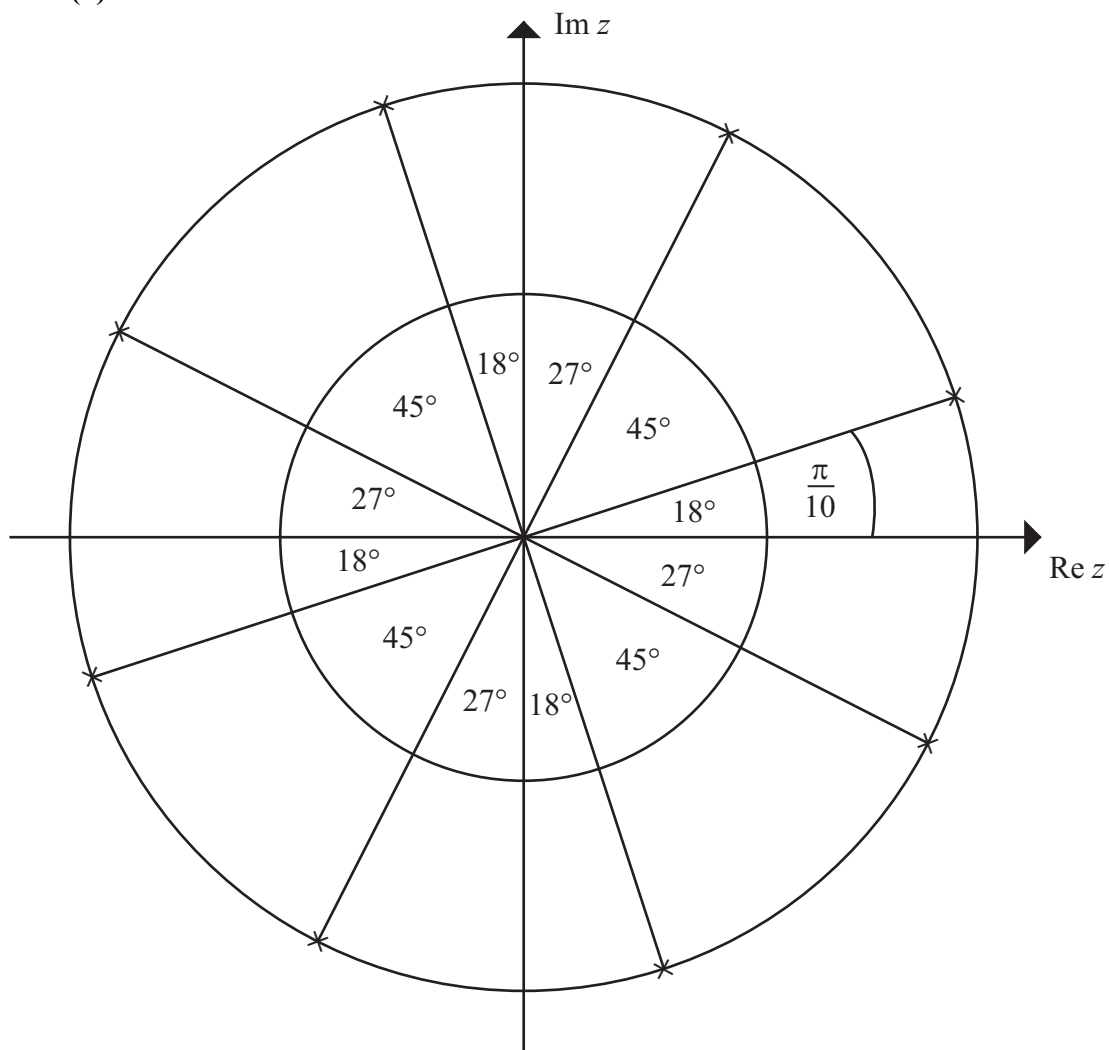
When the candidate misreads a question in such a way as to make the question easier only a proportion of the marks will be available (based on the professional judgement of the examining team).

		AVAILABLE MARKS
1	$(2 \sin x + 1)(2 \cos x - 1) = 0$ $\sin x = -\frac{1}{2}$ $x = n\pi + (-1)^n \left(-\frac{\pi}{6}\right)$ $\cos x = \frac{1}{2}$ $x = 2n\pi \pm \frac{\pi}{3}$	M1W1 M2W1 M1W1
2	Let $P(k) \equiv "1^3 + \dots + k^3 \equiv \frac{1}{4}k^2(k+1)^2"$ When $n = 1$ LHS = 1 RHS = $\frac{1}{4} \times 1 \times 2^2 = 1$ \therefore LHS = RHS and $P(1)$ true (*) Assume $P(k)$ true Consider $1^3 + \dots + k^3 + (k+1)^3$ $= \frac{1}{4}k^2(k+1)^2 + (k+1)^3$ by $P(k)$ $= (k+1)^2 \left[\frac{1}{4}k^2 + (k+1) \right]$ $= \frac{1}{4}(k+1)^2(k+2)^2$ $\therefore P(k+1)$ true so $P(k) \Rightarrow P(k+1)$ (†) (*) and (†) imply $P(n)$ true for all n where $n \geq 1$	M1 M1 MW1 M1 W1 MW1 M1
		7
		7

		AVAILABLE MARKS
3 (i)	$\frac{1+x}{(1+x^2)(1-x)} = \frac{Ax+B}{1+x^2} + \frac{C}{1-x}$ $1+x = (1-x)(Ax+B) + (1+x^2)C$ <p>Put $x = 1$: $2 = 2C \Rightarrow C = 1$</p> <p>Coeff of x^2: $0 = -A + C \Rightarrow A = 1$</p> <p>Coeff of x: $1 = A - B \Rightarrow B = 0$</p> $\frac{x}{1+x^2} + \frac{1}{1-x}$	M1W1 M1 M1 W2
(ii)	<p>IF $e^{\int \frac{-2x}{x^2+1} dx} = e^{-\ln(1+x^2)} = \frac{1}{1+x^2}$</p> $\frac{1}{1+x^2} \frac{dy}{dx} - \frac{2x}{(1+x^2)^2} y = \frac{1+x}{(1+x^2)(1-x)}$ $\frac{d}{dx} \left[\frac{1}{1+x^2} y \right] = \text{RHS}$ $\frac{y}{1+x^2} = \int \frac{1+x}{(1+x^2)(1-x)} dx$ $= \int \left[\frac{x}{1+x^2} + \frac{1}{1-x} \right] dx$ $= \frac{1}{2} \ln(1+x^2) - \ln 1-x + C$	M1W1 M1 MW1 M1 MW1 W2
(iii)	<p>Put $y = 3, x = 0$</p> $3 = \frac{1}{2} \ln 1 - \ln 1 + C$ $C = 3$ $y = (1+x^2) \left\{ \frac{1}{2} \ln(1+x^2) - \ln 1-x + 3 \right\}$ $y = (1+x^2) \left\{ \ln \frac{\sqrt{1+x^2}}{ 1-x } + 3 \right\}$	M1 MW1

16

4 (a)



$r = 3$

$\lambda = \frac{\pi}{10}$

equal spacing

M1

MW1

MW1

AVAILABLE MARKS

(b) (i) $z^{-1} = (\cos \theta + i \sin \theta)^{-1} = \cos \theta - i \sin \theta$ MW1

$\frac{1}{2}(z + z^{-1}) = \frac{1}{2}(2 \cos \theta + 0) = \cos \theta$ W1

(ii) $\cos^6 \theta = \frac{1}{2^6}(z + z^{-1})^6$ MW1

$= \frac{1}{64}(z^6 + 6z^5z^{-1} + 15z^4z^{-2} + 20z^3z^{-3} + 15z^2z^{-4} + 6zz^{-5} + z^{-6})$ MW1

$= \frac{1}{64}(z^6 + z^{-6}) + \frac{6}{64}(z^4 + z^{-4}) + \frac{15}{64}(z^2 + z^{-2}) + \frac{20}{64}$ MW1

Now $z^6 + z^{-6} = 2 \cos 6\theta$, $z^4 + z^{-4} = 2 \cos 4\theta$, etc MW1

So $\cos^6 \theta = \frac{1}{32}(\cos 6\theta + 6 \cos 4\theta + 15 \cos 2\theta + 10)$

$a = \frac{1}{32}$ $b = \frac{3}{16}$ $c = \frac{15}{32}$ $d = \frac{5}{16}$ W2

(iii) $\int \cos^6 \theta d\theta = \frac{1}{192} \sin 6\theta + \frac{3}{64} \sin 4\theta + \frac{15}{64} \sin 2\theta + \frac{5}{16} \theta + C$ MW2

13

5 (i) $f(x) = \cos(x)$ $f'(x) = -\sin x$ $f''(x) = -\cos x$ $f'''(x) = \sin x$ $f^{iv}(x) = \cos x$ M1W1

$f(0) = 1$ $f'(0) = 0$ $f''(0) = -1$ $f'''(0) = 0$ $f^{iv}(0) = 1$ MW1

$f(x) \approx f(0) + xf'(0) + \frac{x^2}{2}f''(0) + \dots$ M1

$\cos x \approx 1 - \frac{x^2}{2} + \frac{x^4}{24} + \dots$ W1

AVAILABLE MARKS

(ii) $\cos kx \doteq 1 - \frac{k^2}{2}x^2 + \frac{k^4 x^4}{24} + \dots$

M1W1

AVAILABLE
MARKS

$$(1-x^2)^{-\frac{1}{2}} \doteq 1 + \left(-\frac{1}{2}\right)(-x^2) + \frac{\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)}{2}(-x^2)^2 + \dots$$

MW1

$$= 1 + \frac{1}{2}x^2 + \frac{3}{8}x^4 + \dots$$

W2

$$\frac{\cos kx}{\sqrt{1-x^2}} \approx \left(1 - \frac{k^2}{2}x^2 + \frac{k^4 x^4}{24}\right) \left(1 + \frac{1}{2}x^2 + \frac{3}{8}x^4\right)$$

M1

$$= 1 + \left(\frac{1}{2} - \frac{k^2}{2}\right)x^2 + \left(\frac{k^4}{24} - \frac{k^2}{4} + \frac{3}{8}\right)x^4 + \dots$$

W2

(iii) Coeff $x^2 = 0 \Rightarrow k^2 = 1$

M1W1

$$\therefore p = \frac{1}{24} - \frac{1}{4} + \frac{3}{8} = \frac{1}{6}$$

W1

16

		AVAILABLE MARKS
6 (i)	$ae = 12 \quad \frac{a}{e} = \frac{169}{12}$	M2
	$a^2 = 169 \quad e^2 = \frac{144}{169}$	MW1
	$b^2 = a^2(1 - e^2) = 169 - 144 = 25$	MW1
	$\frac{x^2}{169} + \frac{y^2}{25} = 1$	MW1
(ii)	$\frac{2x}{169} + \frac{2y}{25} \frac{dy}{dx} = 0$	M1W1
	$\frac{dy}{dx} = -\frac{25x}{169y}$	W1
	$y = 3 \quad x^2 = 169 \left(1 - \frac{y^2}{25}\right) = \frac{169 \times 16}{25} \quad x = \frac{52}{5}$	M1W1
	$\frac{dy}{dx} = -\frac{25}{169} \times \frac{52}{5 \times 3} = -\frac{20}{39}$	W1
	$y - 3 = -\frac{20}{39} \left(x - \frac{52}{5}\right)$	M1
	$39y - 117 = -20x + 208$	
	$39y + 20x = 325$	W1
(iii)	In tangent $y = 0 \quad x = \frac{325}{20} = OT$	MW1
	$ON = \frac{52}{5}$	
	$ON \times OT = \frac{52}{5} \times \frac{325}{20} = 13^2$	MW1
	semi major axis = $a = 13$	MW1
	Total	16
		75



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January 2010**

Mathematics

Assessment Unit M2

assessing

Module M2: Mechanics 2

[AMM21]

MONDAY 1 FEBRUARY, AFTERNOON

**MARK
SCHEME**

GCE Advanced/Advanced Subsidiary (AS) Mathematics

Mark Schemes

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MW indicates marks for combined method and working.

The solution to a question gains marks for correct method and marks for an accurate working based on this method. Where the method is not correct no marks can be given.

A later part of a question may require a candidate to use an answer obtained from an earlier part of the same question. A candidate who gets the wrong answer to the earlier part and goes on to the later part is naturally unaware that the wrong data is being used and is actually undertaking the solution of a parallel problem from the point at which the error occurred. If such a candidate continues to apply correct method, then the candidate's individual working must be followed through from the error. If no further errors are made, then the candidate is penalised only for the initial error. Solutions containing two or more working or transcription errors are treated in the same way. This process is usually referred to as "follow-through marking" and allows a candidate to gain credit for that part of a solution which follows a working or transcription error.

Positive marking:

It is our intention to reward candidates for any demonstration of relevant knowledge, skills or understanding. For this reason we adopt a policy of **following through** their answers, that is, having penalised a candidate for an error, we mark the succeeding parts of the question using the candidate's value or answers and award marks accordingly.

Some common examples of this occur in the following cases:

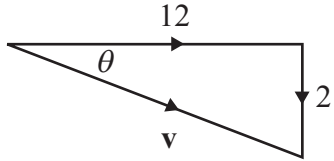
- (a) a numerical error in one entry in a table of values might lead to several answers being incorrect, but these might not be essentially separate errors;
- (b) readings taken from candidates' inaccurate graphs may not agree with the answers expected but might be consistent with the graphs drawn.

When the candidate misreads a question in such a way as to make the question easier only a proportion of the marks will be available (based on the professional judgement of the examining team).

1 (i) $\mathbf{u} = 2\mathbf{i}$
 $\mathbf{a} = 5\mathbf{i} - \mathbf{j}$
 $\mathbf{v} = ?$
 $t = 2$

$\mathbf{v} = \mathbf{u} + \mathbf{a}t$
 $\mathbf{v} = 2\mathbf{i} + (5\mathbf{i} - \mathbf{j})2$
 $\mathbf{v} = 12\mathbf{i} - 2\mathbf{j}$

M1
W2

(ii) 

$\tan \theta = \frac{2}{12}$

$\theta = \tan^{-1} \left(\frac{1}{6} \right)$

M1W1

$\theta = 9.46^\circ$ below + \mathbf{i} direction

W1W1

7

2 By Principle of Conservation of Mechanical Energy
 Total Energy at Start = Total Energy at End

M1

$Mgx + \frac{1}{2} Mu^2 = 0 + \frac{1}{2} M(3u)^2$

M2W3

$x = \frac{4u^2}{g}$

W1

7

3 (i) $\mathbf{r} = t^3\mathbf{i} + t\mathbf{j} + t\mathbf{k}$
 $\mathbf{v} = 3t^2\mathbf{i} + 2t\mathbf{j} + \mathbf{k}$
 At $t = 3$ $\mathbf{v} = 27\mathbf{i} + 6\mathbf{j} + \mathbf{k}$

M1W1
MW1

(ii) $|\mathbf{v}| = \sqrt{(27)^2 + (6)^2 + (1)^2} = 27.7 \text{ m s}^{-1}$

M1W1

(iii) $\mathbf{a} = 6t\mathbf{i} + 2\mathbf{j}$

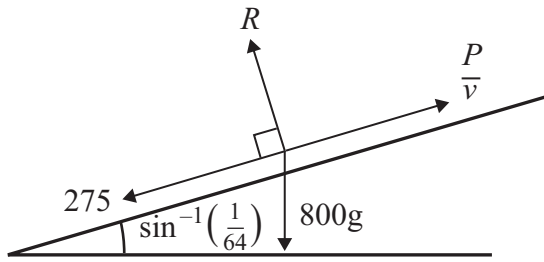
M1W1

(iv) acceleration is not constant as \mathbf{i} component includes t
 i.e. it varies with time

MW1

8

4 (i)



MW2

(ii) Using $F = ma$
At steady speed $a = 0$

M1

M1

$$\frac{P}{v} = 275 + 800g \left(\frac{1}{64} \right)$$

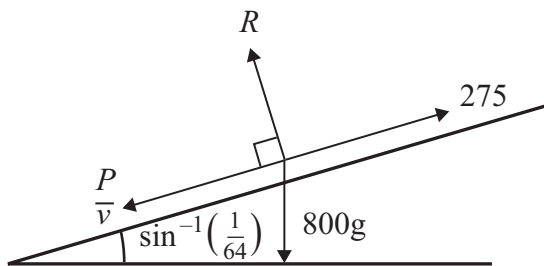
M1W2

$$\frac{P}{15} = 275 + \frac{8000}{64}$$

$$P = 6000 \text{ W} = 6 \text{ kW}$$

W1

(iii)



At max speed $a = 0$

M1

$$275 = \frac{6000}{v} + \frac{800g}{64}$$

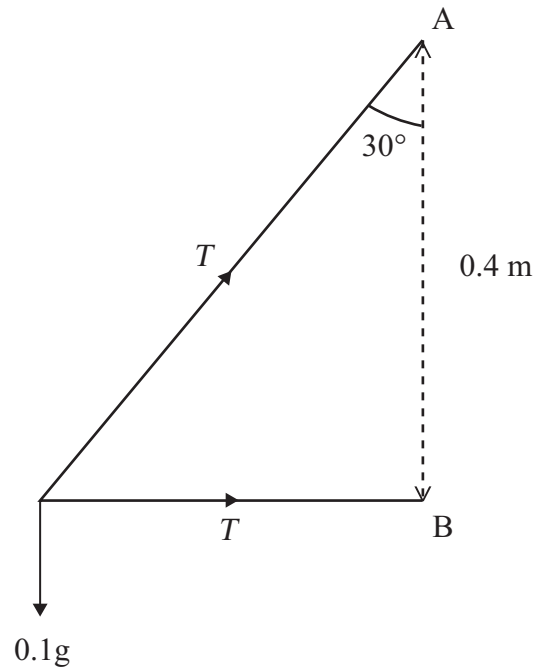
MW1W1

$$v = 40 \text{ ms}^{-1}$$

W1

12

5 (i)



MW2

(ii) \updownarrow $T \cos 30^\circ = 0.1g$

M1

$$T = \frac{0.1g}{\cos 30^\circ} = 1.13 \text{ N}$$

W1

(iii) \longleftrightarrow $T + T \sin 30^\circ = mr\omega^2$

M2W1

$$1.13 + 1.13(0.5) = (0.1)(0.4 \tan 30^\circ)\omega^2$$

MW1W2

$$\omega = 8.57 \text{ rad s}^{-1}$$

W1

(iv) Time to complete one circle = $\frac{2\pi}{\omega}$

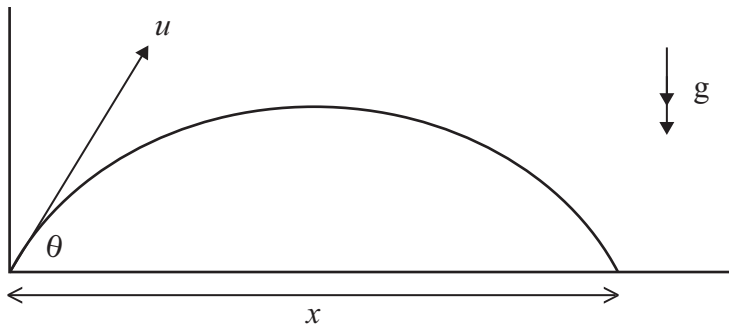
M1

$$= 0.733 \text{ s}$$

W1

13

6 (i)



$$\uparrow \quad u = u \sin \theta \quad v = u + at \quad \text{M1}$$

$$a = -g$$

$$v = 0$$

$$0 = u \sin \theta - gt$$

$$t = ?$$

$$t = \frac{u \sin \theta}{g} \quad \text{W1}$$

$$\text{Total time } t = \frac{2u \sin \theta}{g} \quad \text{MW1}$$

$$\rightarrow u = u \cos \theta$$

$$a = 0$$

$$t = \frac{2u \sin \theta}{g}$$

$$s = ut + \frac{1}{2}at^2 \quad \text{M1}$$

$$s = \frac{2u \sin \theta}{g} u \cos \theta \quad \text{W1}$$

$$s = \frac{2u^2 \sin \theta \cos \theta}{g} = \frac{u^2 \sin 2\theta}{g} \quad \text{W1}$$

Alternative Solution

$$\uparrow \quad u = u \sin \theta \quad s = ut + \frac{1}{2}at^2 \quad \text{MW1}$$

$$s = 0$$

$$0 = u \sin \theta t - \frac{1}{2}gt^2 \quad \text{M1}$$

$$t = ?$$

$$a = -g$$

$$t = \frac{2u \sin \theta}{g} \quad \text{W1}$$

$$\rightarrow u = u \cos \theta$$

$$a = 0$$

$$t = \frac{2u \sin \theta}{g}$$

$$s = ut + \frac{1}{2}at^2$$

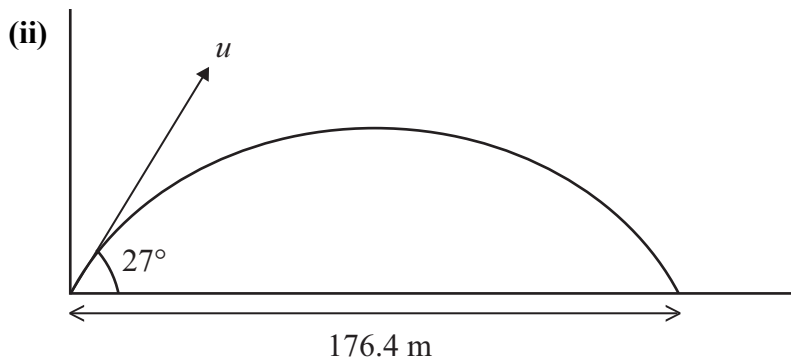
M1

$$s = \frac{2u \sin \theta}{g} u \cos \theta$$

W1

$$s = \frac{2u^2 \sin \theta \cos \theta}{g} = \frac{u^2 \sin 2\theta}{g}$$

W1



$$\frac{u^2 \sin 2\theta}{g} = 176.4$$

M1

$$u^2 = \frac{(176.4)(9.8)}{\sin 54^\circ}$$

W1

$$u = 46.2 \text{ m s}^{-1}$$

W1

(iii) At greatest height $v = 0$

M1

$$u = 46.2 (\sin 27^\circ)$$

$$v = 0$$

$$v^2 = u^2 + 2as$$

M1

$$s = ?$$

$$0 = (46.2 \sin 27^\circ)^2 - 19.6s$$

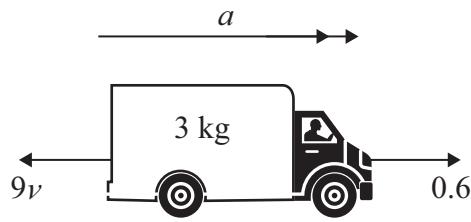
$$a = -9.8$$

$$s = 22.5 \text{ m}$$

W1

12

7 (i)



$F = ma$ M1

$0.6 - 9v = 3a$ W1

$a = 0.2 - 3v$

$\frac{dv}{dt} = 0.2 - 3v$ M1W1

(ii) $\frac{dv}{dt} = 0.2 - 3v$

$\int \frac{dv}{0.2 - 3v} = \int dt$ M2W1

$-\frac{1}{3} \ln |0.2 - 3v| = t + c$ MW2

At $t = 0, v = 0$ $c = -\frac{1}{3} \ln 0.2$ M1W1

$t = \frac{1}{3} \ln 0.2 - \frac{1}{3} \ln |0.2 - 3v|$

$t = \frac{1}{3} \ln \left| \frac{0.2}{0.2 - 3v} \right|$ MW1

(iii) $1 = \frac{1}{3} \ln \left| \frac{0.2}{0.2 - 3v} \right|$ M1

$v = 0.0633 \text{ m s}^{-1}$ M1W1

(iv) Treat truck as a particle MW1

Total

16

75

