

Q1.

<p>10 (i) $2(x-1)^2 - 1$ OR $a=2, b=-1, c=-1$ $A = (1, -1)$</p>	<p>B1, B1, B1 B1✓ [4]</p>	<p>Allow alt. method for final mark</p>
<p>(ii) $2x^2 - 5x - 3 = 0 \Rightarrow (2x+1)(x-3) = 0$ OE in y $x = -\frac{1}{2}, y = 3\frac{1}{2}$</p>	<p>M1, M1 A1 [3]</p>	<p>Complete elim & simplify, attempt soln. Additional (3, 7) not penalised</p>
<p>(iii) Mid-point of $AP = (2, 3)$ Gradient of line = $\frac{\frac{1}{2}}{\frac{-5}{2}} = -\frac{1}{5}$ Equation is $y - 3 = -\frac{1}{5}(x - 2)$ OE</p>	<p>B1✓ B1 B1 [3]</p>	<p>Follow through on <i>their A</i> Or $y - 3\frac{1}{2} = -\frac{1}{5(x + \frac{1}{2})}$</p>

Q2.

<p>2 $y = mx + 4$ $y = 3x^2 - 4x + 7$ Equate $\rightarrow 3x^2 - (4+m)x + 3 = 0$ Uses $b^2 - 4ac \rightarrow (4+m)^2 - 36$ Solution of quadratic $m = 2$ or -10 Set of values $m > 2$ or $m < -10$</p>	<p>M1 M1 DM1 A1 A1 [5]</p>	<p>Eliminates y (or x) completely Any use of $b^2 - 4ac$ Method shown. Correct end-values co</p>
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Q3.

<p>5 (i) $6x + 2 - 7\sqrt{x} \Rightarrow 6(\sqrt{x})^2 - 7\sqrt{x} + 2 = 0$ $(3\sqrt{x} - 2)(2\sqrt{x} - 1) = 0$ $\sqrt{x} = \frac{2}{3}$ or $\frac{1}{2}$ $x = \frac{4}{9}$ or $\frac{1}{4}$ (or 0.444, 0.25) OR $(6x + 2)^2 - 49x \rightarrow 36x^2 - 25x + 4 = 0$ $(9x - 4)(4x - 1) = 0$ $x = \frac{4}{9}$ or $\frac{1}{4}$ (or 0.444, 0.25) oe</p>	<p>M1 M1 A1 A1 M1A1 M1 A1 [4]</p>	<p>Expressing as a clear quadratic so oe e.g. $(3t - 2)(2t - 1) = 0$ 1 solution sufficient. Accept e.g. $t = 2/3$ Both solutions required cao Attempt to square both sides Attempt to solve (or formula etc.)</p>
<p>(ii) $7^2 - 4 \times 6 \times k = 0$ $k = \frac{49}{24}$ or 2.04 OR $\frac{d}{dx}(7x^2) = \frac{d}{dx}(6x + k) \rightarrow \frac{7}{2}x^2 = 6$ $x = \frac{49}{144}, y = \frac{49}{12} \rightarrow k = \frac{49}{24}$ or 2.04</p>	<p>M1 A1 M1 A1 [2]</p>	<p>Apply $b^2 - 4ac = 0$ Attempt to equate derivatives</p>

Q4.

10 $2y + x - k \quad xy - 6$ (i) $2y + x - 8 \rightarrow y(8 - 2y) - 6$ $2y^2 - 8y + 6 - 0$ or $x^2 - 8x + 12 = 0$ $\rightarrow (6, 1)$ and $(2, 3)$ Midpoint $M(4, 2)$ $m = -\frac{1}{2}$ Perpendicular $m = 2$ $\rightarrow y - 2 - 2(x - 4)$ (ii) $(k - 2y)y - 6$ $\rightarrow 2y^2 - ky + 6 - 0$ or $x^2 - kx + 12 = 0$ Uses $b^2 - 4ac = 0$ $\rightarrow k^2 > 48$ $\rightarrow k < -\sqrt{48}$ and $k > \sqrt{48}$	M1	Complete elimination of x (or y)
	DM1A1	DM1 soln of quadratic. co
	M1	for their 2 points
	M1 A1	Uses $m_1 m_2 = -1$ to find perp. gradient co unsimplified
	[6]	
	M1 A1 A1	Any use of $b^2 - 4ac$ on a quadratic = 0 For $\sqrt{48}$ on its own All correct.
	[3]	

Q5.

7 (i) $x^2 - 4x + 4 - x \Rightarrow x^2 - 5x + 4 - 0$ $(x - 1)(x - 4) - 0$ or other valid method $(1, 1), (4, 4)$ Mid-point = $(2\frac{1}{2}, 2\frac{1}{2})$	M1 M1 A1 A1 ✓	Eliminate y to reach 3-term quadratic Attempt solution
	[4]	ft dependent on 1 st M1
(ii) $x^2 - (4 + m)x + 4 - 0 \rightarrow (4 + m)^2 - 4(4) - 0$ $4 + m - \pm 4$ or $m(8 + m) - 0$ $m = -8$ $x^2 + 4x + 4 - 0$ $x = -2, y = 16$	M1 DM1 A1 M1 A1	Applying $b^2 - 4ac = 0$ Attempt solution Ignore $m = 0$ in addition Sub non-zero m and attempt to solve Ignore $(2, 0)$ solution from $m = 0$
	[5]	
Alt (ii) $2x - 4 = m$ $x^2 - 4x + 4 = (2x - 4)x$ $x = -2$ (ignore +2) $m = -8$ (ignore 0) $y = 16$	M1 DM1 A1 A1 A1	OR $2x - 4 = m$ Sub $x = \frac{m + 4}{2}, y = \frac{m(m + 4)}{2}$ into quad $m = -8$ from resulting quad $m(m + 8) = 0$ $x = -2$ $y = 16$

Q6.

2 $\frac{\partial y}{\partial x} = 9x^2 - 12x + 4$ $(3x - 2)^2 \geq 0$	M1A1	
	A1	[3]

Q7.

9	(i) $x^2 + 3x + 4 = 2x + 6 \Rightarrow x^2 + x - 2 (= 0)$ $(x - 1)(x + 2) - 0 \rightarrow (1, 8), (-2, 2)$ $AB = \sqrt{3^2 + 6^2} = 6.71 \text{ or } \sqrt{45} \text{ or } 3\sqrt{5}$ $\left(-\frac{1}{2}, 5\right)$	M1	[5]	3-term simplification DM1 for attempted solution for x cao ($\sqrt{45}$ from wrong points scores B0) Ft <i>their</i> coordinates
		DM1A1		
		B1		
		B1✓		

	(ii) $x^2 + (3 - k)x + 2k - 6 (= 0)$ $(3 - k)^2 - 4(2k - 6) = 0$ $(3 - k)(11 - k) - 0$ $k = 3 \text{ or } 11$	M1	[4]	Simplified to 3-term quadratic Apply $b^2 - 4ac = 0$ as function of k only Attempt factorisation or use formula Both correct NB Alternative methods for (ii) possible
		DM1		
		DM1		
		A1		

Q8.

3	(i) $2x^5 + 3x^2 = 2x \Rightarrow 2x^5 + 3x^2 - 2x = 0$ $[x(2x)^4 + 3x^2 - 2] = 0$ $2x^4 + 3x^2 - 2 = 0$	M1	[2]	First line essential AG Factorising needed for A1 Reasonable attempt at solving a quadratic in x^2 For a correct pair of solutions, either 2 x's or 1 x and 1 y SC ($\pm 0.707, \pm 1.41$) AWR T B1
		A1		
		M1		
	A1			
	A1			
	A1			
(ii) $(x^2 + 2)(2x^2 - 1) = 0$ $x = \pm \frac{1}{\sqrt{2}}$ only $\left(\frac{1}{\sqrt{2}}, \frac{2}{\sqrt{2}}\right), \left(\frac{-1}{\sqrt{2}}, \frac{-2}{\sqrt{2}}\right)$		[3]		

Q9.

<p>7 (i) $y = m(x-2)$ oe</p> <p>(ii) $x^2 - 4x + 5 = mx - 2m \Rightarrow x^2 - x(4+m) + 5 + 2m = 0$ $(4+m)^2 - 4(5+2m) = 0 \Rightarrow m^2 - 4 = 0$ $m = \pm 2$ $m = 2 \Rightarrow x^2 - 6x + 9 = 0 \Rightarrow x = 3$ $m = -2 \Rightarrow x^2 - 2x + 1 = 0 \Rightarrow x = 1$ $(3, 2), (1, 2)$</p> <p>OR $m = 2^x - 4$ $y = m^x - 2m, y = x^2 - 4x + 5$</p> <p>(iii) $(x-2)^2 + 1, (2, 1)$</p>	<p>B1 [1]</p> <p>M1 DM1 A1 DM1 A1 A1 [6]</p> <p>M1 M1</p> <p>M1 A1 A1 A1</p> <p>B1, B1 [2]</p>	<p>Accept $y = mx + c, c = -2m$</p> <p>Apply $b^2 - 4ac$</p> <p>Substitute their m and attempt to solve for x Allow for a pair of x values or 1 x and 1 y.</p> <p>Eliminating 2 variables from 3 equations. Obtaining a quadratic in x or y.</p> <p>Solving their quadratic correctly.</p> <p>A pair of x values or 1 x and 1 y..</p> <p>$m=2, -2$ also needed for final mark.</p>
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Q10.

<p>10 (i)</p> <p>(ii) $(6+k)^2(4)(2)(2+3k) = 0$</p> <p>$k = 2$ or 10</p> <p>(iii) or $(2, -2)$ $k = 10 \Rightarrow 2(x-4)^2 = 0$ $x = 4, y = 2$ or $(4, 2)$ AB:</p>	<p>B1 [1]</p> <p>M1 A1 A1 [3]</p> <p>M1 A1 M1 A1 M1 A1 [6]</p>	<p>AG</p> <p>Apply $b^2 - 4ac$</p> <p>cao</p> <p>$(y = 2x - 6)$</p>
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Q11.

<p>1 $(x+1)(x-2)$ or other valid method $-1, 2$ $x < -1, x > 2$</p>	<p>M1 A1 A1 [3]</p>	<p>Attempt soln of eqn or other method Penalise $<, >$</p>
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