

**Q1.**

- 6 (i) Attempt to apply the chain or quotient rule M1  
 Obtain derivative of the form  $\frac{k \sec^2 x}{(1 + \tan x)^2}$  or equivalent A1  
 Obtain correct derivative  $-\frac{\sec^2 x}{(1 + \tan x)^2}$  or equivalent A1  
 Explain why derivative, and hence gradient of the curve, is always negative A1  
**[4]**
- (ii) State or imply correct ordinates: 1, 0.7071..., 0.5 B1  
 Use correct formula, or equivalent, with  $h = \frac{1}{8}\pi$  and three ordinates M1  
 Obtain answer  $0.57 (0.57220...) \pm 0.01$  (accept  $0.18\pi$ ) A1  
**[3]**

© University of Cambridge Local Examinations Syndicate 2003

Page 3	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – JUNE 2003	9709	2

- (iii) Justify the statement that the rule gives an over-estimate B1  
**[1]**

**Q2.**

- 5 (i) State derivative of the form  $(e^x \pm xe^x)$ . Allow  $xe^x \pm e^x$  {via quotient rule} M1  
 Obtain correct derivative of  $e^{2x} - xe^{-x}$  A1  
 Equate derivative to zero and solve for x M1  
 Obtain answer  $x = 1$  A1 **4**
- (ii) Show or imply correct ordinates 0, 0.367879..., 0.27067... B1  
 Use correct formula, or equivalent, with  $h = 1$  and three ordinates M1  
 Obtain answer 0.50 with no errors seen A1 **3**
- (iii) Justify statement that the rule gives an under-estimate B1 **1**

**Q3.**

6	(i) State coordinates (1, 0)	B1	1
	(ii) Use quotient or product rule	M1	
	Obtain correct derivative, e.g. $\frac{-\ln x}{x^2} + \frac{1}{x^2}$	A1	
	Equate derivative to zero and solve for $x$	M1	
	Obtain $x = e$	A1	
	Obtain $y = \frac{1}{e}$	A1	5
	(iii) Show or imply correct coordinates 0, 0.34657..., 0.36620..., 0.34657,,	B1	
	Use correct formula, or equivalent, with $h = 1$ and four ordinates	A1	
	Obtain answer 0.89 with no errors seen	A1	3
	(iv) Justify statement that the rule gives an under-estimate	B1	1

**Q4.**

7	(i) Obtain derivative of the form $\frac{k}{2x+3}$ , where $k = 2$ or $k = 1$	M1	
	Obtain correct derivative $\frac{2}{2x+3}$	A1	2
	(ii) State indefinite integral of the form $m \ln(2x+3)$	M1*	
	Use limits correctly	M1(dep*)	
	Obtain given answer	A1	3
	(iii) Carry out division method reaching a linear quotient and constant remainder	M1	
	Obtain quotient $2x + 1$	A1	
	Obtain remainder $-3$	A1	3
	(iv) Attempt integration of its integrand of the form $ax + b + \frac{c}{2x+3}$	M1	
	Obtain indefinite integral $x^2 + x - \frac{3}{2} \ln(2x+3)$	A1/2	
	Substitute limits and obtain given answer	A1	3
	[The f.f. mark is also available if the indefinite integral of the third term is omitted but its definite integral is stated to be $c \ln 3$ .]		

**Q5.**

7	(i) State coordinates (0, 1) for $A$	B1	[1]
	(ii) Differentiate using the product rule	M1*	
	Obtain derivative in any correct form	A1	
	Equate derivative to zero and solve for $x$	M1*	
	Obtain $x = \frac{1}{4}\pi$ or 0.785 (allow $45^\circ$ )	A1	[4]
	(iii) Show or imply correct ordinates 1, 1.4619..., 1.4248..., 0	B1	
	Use correct formula or equivalent with $h = \frac{1}{6}\pi$ and four ordinates	M1	
	Obtain correct answer 1.77 with no errors seen	A1	[3]
	(iv) Justify statement that the trapezium rule gives an underestimate	B1	[1]

## Q6.

- 8 (a) State derivative is  $k/(3x-2)$  where  $k=3$ , 1, or  $\frac{1}{3}$  M1  
State correct derivative  $3/(3x-2)$  A1  
Form the equation of the tangent at the point where  $x=1$  M1  
Obtain answer  $y=3x-3$ , or equivalent A1 [4]
- (b) (i) Carry out a complete method for finding  $A$  M1  
Obtain  $A=4$  A1 [2]
- (ii) Integrate and obtain term  $2x$  B1  
Obtain second term of the form  $a \ln(3x-2)$  M1  
Obtain second term  $\frac{4}{3} \ln(3x-2)$  A1√  
Substitute limits correctly M1  
Obtain given answer following full and correct working A1 [5]

## Q7.

- 8 (i) Use quotient rule M1  
Obtain correct derivative in any form A1  
Obtain given result correctly A1 [3]
- (ii) State  $\cot^2 x \equiv -1 + \operatorname{cosec}^2 x$ , or equivalent B1  
Obtain integral  $-x - \cot x$  (f.t. on signs in the identity) B1√  
Substitute correct limits correctly M1  
Obtain given answer A1 [4]
- (iii) Use trig formulae to convert integrand to  $\frac{1}{k \sin^2 x}$  where  $k = \pm 2$ , or  $\pm 1$  M1  
Obtain given answer  $\frac{1}{2} \operatorname{cosec}^2 x$  correctly A1  
Obtain answer  $-\frac{1}{2} \cot x + c$ , or equivalent B1 [3]

## Q8.

- 5 (i) Differentiate to obtain expression of form  $ke^{\frac{1}{2}x} + m$  M1  
Obtain correct  $2e^{\frac{1}{2}x} - 6$  A1  
Equate attempt at first derivative to zero and attempt solution DM1  
Obtain  $\frac{1}{2}x = \ln 3$  or equivalent A1  
Conclude  $x = \ln 9$  or  $a = 9$  A1 [5]
- (ii) Integrate to obtain expression of form  $ae^{\frac{1}{2}x} + bx^2 + cx$  M1  
Obtain correct  $8e^{\frac{1}{2}x} - 3x^2 + 3x$  A1  
Substitute correct limits and attempt simplification DM1  
Obtain  $8e - 14$  A1 [4]

## Q9.

- 7 (a) Obtain one term of form  $ke^{2x-1}$  with any non-zero  $k$  M1  
 Obtain correct integral  $x + \frac{1}{2}e^{2x-1}$  A1  
 Substitute limits, giving exact values M1  
 Correct answer  $\frac{1}{2}e^3 + 1$  A1 [4]
- (b) Use product or quotient rule M1\*  
 Obtain correct derivative in any form A1  
 Equate derivative to zero and solve for  $x$  M1\*  
 Obtain  $\tan 2x = 1$  dep  
 A1  
 Obtain  $x = \frac{\pi}{8}$  A1 [5]

## Q10.

- 7 (i) Attempt to differentiate using the quotient, product or chain rule M1  
 Obtain derivative in any correct form A1  
 Obtain the given answer correctly A1  
 [3]

© University of Cambridge Local Examinations Syndicate 2003

Page 3	Mark Scheme	Syllabus	Paper
	A AND AS LEVEL – NOVEMBER 2003	9709	2

- (ii) State or imply the indefinite integral is  $-\cot x$  B1  
 Substitute limits and obtain given answer correctly B1  
 [2]
- (iii) Use  $\cot^2 x = \operatorname{cosec}^2 x - 1$  and attempt to integrate both terms, or equivalent M1  
 Substitute limits where necessary and obtain a correct unsimplified answer A1  
 Obtain final answer  $\sqrt{3} - \frac{1}{3}\pi$  A1  
 [3]
- (iv) Use  $\cos 2A$  formula and reduce denominator to  $2\sin^2 x$  B1  
 Use given result and obtain answer of the form  $k\sqrt{3}$  M1  
 Obtain correct answer  $\frac{1}{2}\sqrt{3}$  A1  
 [3]

## Q11.

7 (i)	State coordinates (0, 5)	B1	1
(ii)	State first derivative of the form $k e^x + m e^{-2x}$ , where $km \neq 0$	M1	
	Obtain correct first derivative $2 e^x - 6 e^{-2x}$	A1	
	Substitute $x = 0$ , obtaining gradient of $-4$	A1✓	
	Form equation of line through A with this gradient (NOT the normal)	M1	
	Obtain equation in any correct form e.g. $y - 5 = -4x$	A1	
	Obtain coordinates (1.25, 0) or equivalent	A1	6
(iii)	Integrate and obtain $2 e^x - \frac{3}{2} e^{-2x}$ , or equivalent	B1 + B1	
	Use limits $x = 0$ and $x = 1$ correctly	M1	
	Obtain answer 4.7	A1	4

## Q12.

6.	(i) State $\frac{1}{2} e^{2x}$ as integral of $e^{2x}$	B1	
	State $y = \frac{1}{2} e^{2x} + 2e^{-x} + c$	B1	
	Evaluate $c$	M1	
	Obtain answer $y = \frac{1}{2} e^{2x} + 2e^{-x} - 1\frac{1}{2}$	A1	4
	[Condone omission of $c$ for the second B1.]		
	(ii) Equate derivative to zero	M1	
	<i>EITHER:</i> Obtain $e^{3x} = 2$	A1	
	Use logarithms and obtain a linear equation in $x$	M1	
	Obtain answer $x = 0.231$	A1	
	Show that the point is a minimum with no errors seen	A1	
	<i>OR:</i> Use logarithms and obtain a linear equation in $x$	M1	
	Obtain $2x = \ln 2 - x$	A1	
	Obtain answer $x = 0.231$	A1	
	Show that the point is a minimum with no errors seen	A1 ✓	5

## Q13.

7.	(i) Differentiate using the chain or product rule	M1	
	Obtain given answer correctly	A1	2
	(ii) Use correct method for solving $\sin 2x = 0.5$	M1	
	Obtain answer $x = \frac{1}{12} \pi$ (or 0.262 radians)	A1	
	Obtain answer $x = \frac{5}{12} \pi$ (or 1.31 radians) and no others in range	A1	3
	(iii) Replace integrand by $\frac{1}{2} - \frac{1}{2} \cos 2x$ , or equivalent	B1	
	Integrate and obtain $\frac{1}{2} x - \frac{1}{4} \sin 2x$ , or equivalent	B1✓ + B1✓	
	Use limits $x = 0$ and $x = \pi$ correctly	M1	
	Obtain final answer 1.57 (or $\frac{1}{2} \pi$ )	A1	5

## Q14.

6	(i) Use quotient or product rule	M1	
	Obtain derivative in any correct form, e.g. $e^{2x} \left( \frac{2}{x} - \frac{1}{x^2} \right)$	A1	
	Equate derivative to zero and solve for $x$	M1	
	Obtain $x = \frac{1}{2}$	A1	
	Obtain $y = 2e$ (or 5.44)	A1*	5
	(ii) Show or imply correct ordinates 7.389..., 13.390..., 27.299...	B1	
	Use correct formula, or equivalent, with $h = 0.5$ and three ordinates	M1	
	Obtain answer 15.4 with no errors seen	A1	3
	(iii) Justify the statement that the rule gives an over-estimate	B1	1

### Q15.

8	(i) Differentiate using product or quotient rule	M1	
	Obtain derivative in any correct form	A1	
	Equate derivative to zero and solve for $x$	M1	
	Obtain answer $x = 2$ correctly, with no other solution	A1	[4]
	(ii) Find the gradient of the curve when $x = 1$ , must be simplified, allow 0.368	B1	
	Form the equation of the tangent when $x = 1$	M1	
	Show that it passes through the origin	A1	[3]
	(iii) State or imply correct ordinates 0.36787..., 0.54134..., 0.44808...	B1	
	Use correct formula, or equivalent, correctly with $h = 1$ and three ordinates	M1	
	Obtain answer 0.95 with no errors seen	A1	[3]

### Q16.

8	(i) (a) Use trig formulae and justify given result	B1	
	(b) Use $1 - \sin^2 x = \cos^2 x$	M1	
	Obtain given result correctly	A1	[3]
	(ii) Use quotient or chain rule	M1	
	Obtain correct derivative in any form	A1	
	Obtain given result correctly	A1	[3]
	(iii) Obtain integral $\tan x + \sec x$	B1	
	Substitute limits correctly	M1	
	Obtain exact answer $\sqrt{2}$ , or equivalent	A1	[3]

### Q17.

- 8 (i) Use product rule M1  
 Obtain correct derivative in any form A1  
 Substitute  $x = \frac{1}{2}\pi$ , and obtain gradient of  $-1$  for normal A1✓  
 from  $y' = \sin x - x \cos x$  ONLY  
 Show that line through  $\left(\frac{1}{2}\pi, \frac{1}{2}\pi\right)$  with gradient  $-1$  passes through  $(\pi, 0)$  M1  
 A1 [5]
- (ii) Differentiate  $\sin x$  and use product rule to differentiate  $x \cos x$  M1  
 Obtain  $x \sin x$ , or equivalent A1 [2]
- (iii) State that integral is  $\sin x - x \cos x (+c)$  B1  
 Substitute limits  $0$  and  $\frac{\pi}{2}$  correctly M1  
 Obtain answer 1 A1 [3]  
 S. R. Feeding limits into original integrand, 0/3

### Q18.

- 7 (i) Use product or quotient rule M1\*  
 Obtain correct derivative in any form A1  
 Equate derivative to zero and solve for  $x$  M1\*(dep)  
 Obtain  $x = e^{0.5}$  or  $\sqrt{e}$  A1  
 Obtain  $\frac{1}{2e}$ , or equivalent A1 [5]
- (ii) State or imply correct ordinates  $0, 0.17328\dots, 0.12206\dots, 0.08664\dots$  B1  
 Use correct formula, or equivalent, correctly with  $h = 1$  and four ordinates M1  
 Obtain answer  $0.34$  with no errors seen A1 [3]

### Q19.

- 3 (i) Obtain correct derivative B1  
 Obtain  $x = 2$  only B1 [2]
- (ii) State or imply correct ordinates  $0.61370\dots, 0.80277\dots, 1.22741\dots, 1.78112\dots$  B1  
 Use correct formula, or equivalent, correctly with  $h = 1$  and four ordinates M1  
 Obtain answer  $3.23$  with no errors seen A1 [3]
- (iii) Justify statement that the trapezium rule gives an over-estimate B1 [1]

### Q20.

- 8 (i) Differentiate using chain or quotient rule M1  
 Obtain derivative in any correct form A1  
 Obtain given answer correctly A1 [3]
- (ii) Differentiate using product rule M1  
 State derivative of  $\tan \theta = \sec^2 \theta$  B1  
 Use trig identity  $1 + \tan^2 \theta = \sec^2 \theta$  correctly M1  
 Obtain  $2\sec^3 \theta - \sec \theta$  A1 [4]
- (iii) Use  $\tan^2 x = \sec^2 \theta - 1$  to integrate  $\tan^2 x$  M1  
 Obtain  $3\sec \theta$  from integration of  $3\sec \theta \tan \theta$  B1  
 Obtain  $\tan \theta - 3\sec \theta$  A1  
 Attempt to substitute limits, using exact values M1  
 Obtain answer  $4 - 3\sqrt{2}$  A1 [5]

## Q21.

- 5 (i) Differentiate to obtain  $-2 \sin x + 2 \sin 2x$  or equivalent B1  
 Use  $\sin 2x = 2 \sin x \cos x$  or equivalent B1  
 Equate first derivative to zero and solve for  $x$  M1  
 Obtain  $\frac{1}{3}\pi$  A1 [4]

© Cambridge International Examinations 2014

Page 5	Mark Scheme	Syllabus	Paper
	Cambridge International AS Level – October/November 2014	9709	22

- (ii) Integrate to obtain form  $k_1 \sin x + k_2 \sin 2x$  M1  
 Obtain correct  $2 \sin x - \frac{1}{2} \sin 2x$  A1  
 Apply limits 0 and their answer from part (i) M1  
 Obtain  $\frac{3}{4}\sqrt{3}$  or exact equivalent A1 [4]

## P3 (variant1 and 3)

### Q1.



- 5 (i) State derivative  $-e^{-x} - (-2)e^{-2x}$ , or equivalent B1 + B1  
 Equate derivative to zero and solve for  $x$  M1  
 Obtain  $p = \ln 2$ , or exact equivalent A1 [4]
- (ii) State indefinite integral  $-e^{-x} - (-\frac{1}{2})e^{-2x}$ , or equivalent B1 + B1  
 Substitute limits  $x = 0$  and  $x = p$  correctly M1  
 Obtain given answer following full and correct working A1 [4]

## Q2.

- 8 (i) Use product and chain rule M1  
 Obtain correct derivative in any form, e.g.  $15 \sin^2 x \cos^3 x - 10 \sin^4 x \cos x$  A1  
 Equate derivative to zero and obtain a relevant equation in one trigonometric function M1  
 Obtain  $2 \tan^2 x = 3$ ,  $5 \cos^2 x = 2$ , or  $5 \sin^2 x = 3$  A1  
 Obtain answer  $x = 0.886$  radians A1 [5]
- (ii) State or imply  $du = -\sin x dx$ , or  $\frac{du}{dx} = -\sin x$ , or equivalent B1  
 Express integral in terms of  $u$  and  $du$  M1  
 Obtain  $\pm \int 5(u^2 - u^4) du$ , or equivalent A1  
 Integrate and use limits  $u = 1$  and  $u = 0$  (or  $x = 0$  and  $x = \frac{1}{2}\pi$ ) M1  
 Obtain answer  $\frac{2}{3}$ , or equivalent, with no errors seen A1 [5]

## Q3.

- 5 (i) Differentiate to obtain  $4 \cos \frac{1}{2}x - \frac{1}{2} \sec^2 \frac{1}{2}x$  B1  
 Equate to zero and find value of  $\cos \frac{1}{2}x$  M1  
 Obtain  $\cos \frac{1}{2}x = \frac{1}{2}$  and confirm  $\alpha = \frac{2}{3}\pi$  A1 [3]
- (ii) Integrate to obtain  $-16 \cos \frac{1}{2}x \dots$  B1  
 $\dots + 2 \ln \cos \frac{1}{2}x$  or equivalent B1  
 Using limits 0 and  $\frac{2}{3}\pi$  in  $a \cos \frac{1}{2}x + b \ln \cos \frac{1}{2}x$  M1  
 Obtain  $8 + 2 \ln \frac{1}{2}$  or exact equivalent A1 [4]

## Q4.

- 9 (i) Use product rule M1  
 Obtain correct derivative in any form, e.g.  $4\sin 2x \cos 2x \cos x - \sin^2 2x \sin x$  A1  
 Equate derivative to zero and use a double angle formula M1\*  
 Reduce equation to one in a single trig function M1(dep\*)  
 Obtain a correct equation in any form, A1  
 e.g.  $10 \cos^3 x = 6 \cos x$ ,  $4 = 6 \tan^2 x$  or  $4 = 10 \sin^2 x$  A1  
 Solve and obtain  $x = 0.685$  A1 [6]
- (ii) Using  $du = \pm \cos x \, dx$ , or equivalent, express integral in terms of  $u$  and  $du$  M1  
 Obtain  $\int 4u^2(1-u^2) \, du$ , or equivalent A1  
 Use limits  $u = 0$  and  $u = 1$  in an integral of the form  $au^3 + bu^5$  M1  
 Obtain answer  $\frac{8}{15}$  (or 0.533) A1 [4]

## Q5.

- 9 (i) State coordinates (1, 0) B1 [1]
- (ii) Use correct quotient or product rule M1  
 Obtain derivative in any correct form A1  
 Equate derivative to zero and solve for  $x$  M1  
 Obtain  $x = e^2$  correctly A1 [4]

© UCLES 2009

Page 7	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE A/AS LEVEL – October/November 2009	9709	31

- (iii) Attempt integration by parts reaching  $a\sqrt{x} \ln x \pm a \int \sqrt{x} \frac{1}{x} \, dx$  M1\*  
 Obtain  $2\sqrt{x} \ln x - 2 \int \frac{1}{\sqrt{x}} \, dx$  A1  
 Integrate and obtain  $2\sqrt{x} \ln x - 4\sqrt{x}$  A1  
 Use limits  $x = 1$  and  $x = 4$  correctly, having integrated twice M1(dep\*)  
 Justify the given answer A1 [5]

## Q6.

- 9 (i) Use correct product rule M1  
 Obtain correct derivative in any form A1  
 Equate derivative to zero and find non-zero  $x$  M1  
 Obtain  $x = \exp(-\frac{1}{3})$ , or equivalent A1  
 Obtain  $y = -1/(3e)$ , or any ln-free equivalent A1 [5]

- (ii) Integrate and reach  $kx^4 \ln x + I \int x^4 \cdot \frac{1}{x} dx$  M1  
 Obtain  $\frac{1}{4}x^4 \ln x - \frac{1}{4} \int x^3 dx$  A1  
 Obtain integral  $\frac{1}{4}x^4 \ln x - \frac{1}{16}x^4$ , or equivalent A1  
 Use limits  $x = 1$  and  $x = 2$  correctly, having integrated twice M1  
 Obtain answer  $4 \ln 2 - \frac{15}{16}$ , or exact equivalent A1 [5]

## Q7.

- 4 (i) Obtain derivative of form  $k \cos 3x \sin 3x$ , any constant  $k$  M1  
 Obtain  $-24 \cos 3x \sin 3x$  or unsimplified equivalent A1  
 Obtain  $-6\sqrt{3}$  or exact equivalent A1 [3]
- (ii) Express integrand in the form  $a + b \cos 6x$ , where  $ab \neq 0$  M1  
 Obtain  $2 + 2 \cos 6x$  o.e. A1  
 Obtain  $2x + \frac{1}{3} \sin 6x$  or equivalent, condoning absence of  $+ c$ , ft on  $a, b$  A1√ [3]

## Q8.

- 9 (i) Use product rule M1  
 Obtain correct derivative in any form A1  
 Equate derivative to zero and solve for  $x$  M1  
 Obtain answer  $x = e^{-\frac{1}{2}}$ , or equivalent A1  
 Obtain answer  $y = -\frac{1}{2}e^{-1}$ , or equivalent A1 [5]
- (ii) Attempt integration by parts reaching  $kx^3 \ln x \pm k \int x^3 \cdot \frac{1}{x} dx$  M1\*  
 Obtain  $\frac{1}{3}x^3 \ln x - \frac{1}{3} \int x^2 dx$ , or equivalent A1  
 Integrate again and obtain  $\frac{1}{3}x^3 \ln x - \frac{1}{9}x^3$ , or equivalent A1  
 Use limits  $x = 1$  and  $x = e$ , having integrated twice M1(dep\*)  
 Obtain answer  $\frac{1}{9}(2e^3 + 1)$ , or exact equivalent A1 [5]
- [SR: An attempt reaching  $ax^2(x \ln x - x) + b \int 2x(x \ln x - x) dx$  scores M1. Then give the first A1 for  $I = x^2(x \ln x - x) - 2I + \int 2x^2 dx$ , or equivalent.]

## Q9.

- 5 (i) Use correct quotient or chain rule M1  
Obtain the given answer correctly having shown sufficient working A1 [2]
- (ii) Use a valid method, e.g. multiply numerator and denominator by  $\sec x + \tan x$ , and a version of Pythagoras to justify the given identity B1 [1]
- (iii) Substitute, expand  $(\sec x + \tan x)^2$  and use Pythagoras once M1  
Obtain given identity A1 [2]
- (iv) Obtain integral  $2 \tan x - x + 2 \sec x$  B1  
Use correct limits correctly in an expression of the form  $a \tan x + bx + c \sec x$ , or equivalent, where  $abc \neq 0$  M1  
Obtain the given answer correctly A1 [3]

## Q10.

- 5 (i) Either Use correct product rule M1  
Obtain  $3e^{-2x} - 6xe^{-2x}$  or equivalent A1  
Substitute  $-\frac{1}{2}$  and obtain  $6e$  A1
- Or / Take  $\ln$  of both sides and use implicit differentiation correctly M1  
Obtain  $\frac{dy}{dx} = y \left( \frac{1}{x} - 2 \right)$  or equivalent A1  
Substitute  $-\frac{1}{2}$  and obtain  $6e$  A1 [3]
- (ii) Use integration by parts to reach  $kxe^{-2x} \pm \int ke^{-2x} dx$  M1  
Obtain  $-\frac{3}{2}xe^{-2x} + \int \frac{3}{2}e^{-2x} dx$  or equivalent A1  
Obtain  $-\frac{3}{2}xe^{-2x} - \frac{3}{4}e^{-2x}$  or equivalent A1  
Substitute correct limits correctly DM1  
Obtain  $-\frac{3}{4}$  with no errors or inexact work seen A1 [5]

## Q11.

- 9 (i) Substitute for  $x$  and  $dx$  throughout using  $u = \sin x$  and  $du = \cos x \, dx$ , or equivalent M1  
 Obtain integrand  $e^{2u}$  A1  
 Obtain indefinite integral  $\frac{1}{2}e^{2u}$  A1  
 Use limits  $u = 0, u = 1$  correctly, or equivalent M1  
 Obtain answer  $\frac{1}{2}(e^2 - 1)$ , or exact equivalent A1 **5**

© Cambridge International Examinations 2014

---

Page 6	Mark Scheme	Syllabus	Paper
	GCE A LEVEL – May/June 2014	9709	33

- (ii) Use chain rule or product rule M1  
 Obtain correct terms of the derivative in any form, e.g.  $2\cos x e^{2\sin x} \cos x - e^{2\sin x} \sin x$  A1 + A1  
 Equate derivative to zero and obtain a quadratic equation in  $\sin x$  M1  
 Solve a 3-term quadratic and obtain a value of  $x$  M1  
 Obtain answer 0.896 A1 **6**

