

**MARK SCHEME for the May/June 2010 question paper  
for the guidance of teachers**

**9709 MATHEMATICS**

**9709/12**

Paper 12, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

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### Mark Scheme Notes

Marks are of the following three types:

**M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

**A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

**B** Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol  $\surd$  implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.  
B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking  $g$  equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no “follow through” from a previous error is allowed)
CWO	Correct Working Only often written by a ‘fortuitous’ answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

### **Penalties**

MR –1	A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become “follow through $\checkmark$ ” marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR–2 penalty may be applied in particular cases if agreed at the coordination meeting.
PA –1	This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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<p><b>1 (i)</b> <math>3(2 \sin x - \cos x) = 2(\sin x - 3 \cos x)</math>  <math>\rightarrow 6s - 3c = 2s - 6c \rightarrow 4s = -3c</math>  <math>\rightarrow \tan x = -\frac{3}{4}</math></p> <p><b>(ii)</b> <math>x = 180 - 36.9 = 143.1^\circ</math> or  <math>x = 360 - 36.9 = 323.1^\circ</math></p>	<p>M1 A1 [2]</p> <p>B1 B1√ [2]</p>	<p>Expanding, collecting, use of <math>t = s \div c</math> Answer given. All correct.</p> <p>co For 180 + first answer.</p>
<p><b>2</b> <math>y = \frac{a}{x}</math></p> <p>Volume = <math>\pi \int \left( \frac{a^2}{x^2} \right) dx = (\pi) \left[ \frac{-a^2}{x} \right]</math></p> <p>Use of limits 1 to 3 <math>\rightarrow \frac{2\pi a^2}{3}</math></p> <p>Equates to <math>24\pi \rightarrow a = 6</math></p>	<p>M1 B1</p> <p>M1</p> <p>A1 [4]</p>	<p>For using correct formula with <math>\pi</math>. For correct integration of <math>x^{-2}</math> only</p> <p>Must be using <math>y^2</math> or <math>\pi y^2</math>.</p> <p>Co, allow <math>\pm 6</math>.</p>
<p><b>3</b> <math>f: x \mapsto 4x - 2x^2</math>,  <math>g: x \mapsto 5x + 3</math>.</p> <p><b>(i)</b> Turning point at <math>x = 1</math>. Range is <math>\leq 2</math>.</p> <p><b>(ii)</b> <math>gf(x) = 5(4x - 2x^2) + 3</math>  <math>= k</math> and use of <math>b^2 - 4ac</math>  <math>\rightarrow k = 13</math></p>	<p>M1 A1 [2]</p> <p>B1 M1 A1 [3]</p>	<p>Calculus or completing the square etc. Condone <math>&lt;</math> instead of <math>\leq</math>.</p> <p>For putting f into g. Setting to k, using <math>b^2 - 4ac</math> co</p>
<p><b>4</b> Gradient of <math>L_1</math> is <math>\frac{1}{3}</math>.</p> <p>Equation of <math>L_1</math> is <math>y - 3 = \frac{1}{3}(x + 1)</math></p> <p>Gradient of <math>AB</math> is <math>-\frac{1}{2}</math>. Perp = 2.</p> <p>Equation of <math>L_2</math> is <math>y - 1 = 2(x - 3)</math>.</p> <p>Sim eqns <math>3y = x + 10</math>, <math>y = 2x - 5</math>.  <math>\rightarrow (5, 5)</math></p>	<p>M1 A1</p> <p>M1</p> <p>A1</p> <p>M1 A1 [6]</p>	<p>M1 for equation for his <math>m</math>. A1 co.</p> <p>Use of <math>m_1 m_2 = -1</math></p> <p>co</p> <p>Method of solution co</p>

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<p>5 (i) <math>-8 + 3 + p = 0</math>  <math>\rightarrow p = 5.</math></p> <p>(ii) Vector <math>\overrightarrow{AB} = \mathbf{b} - \mathbf{a}</math>  <math>= 6\mathbf{i} - 2\mathbf{j} + (p - 1)\mathbf{k}</math></p> <p><math>36 + 4 + (p - 1)^2 = 49</math>  <math>\rightarrow p = 4</math> or <math>p = -2</math></p>	<p>M1 A1 [2]</p> <p>M1</p> <p>M1 A1 A1 [4]</p>	<p>Must be scalar. co.</p> <p>Must be <math>\mathbf{b} - \mathbf{a}</math> or <math>\mathbf{a} - \mathbf{b}</math></p> <p>Must be sum of 3 squares. A1 <math>\surd</math> lost. co.</p>
<p>6 (i) <math>1 + 5ax + 10a^2x^2</math></p> <p>(ii) <math>\times (1 - 2x) \rightarrow 5ax - 2x</math>  <math>\rightarrow a = \frac{2}{5}</math></p> <p>(iii) Coeff of <math>x^2</math> is <math>-10a + 10a^2</math>  <math>\rightarrow -4 + 1.6 = -2.4</math></p>	<p>B2,1 [2]</p> <p>M1 A1 [2]</p> <p>M1 A1 <math>\surd</math> A1 [3]</p>	<p>Loses 1 mark for each incorrect term.</p> <p>Needs to consider exactly 2 terms. co</p> <p>Needs to consider exactly 2 terms. co</p>
<p>7 (a) <math>a = 100, d = 5,</math>  <math>n = 41</math>  <math>\rightarrow S = 8200</math></p> <p>(b) (i) <math>a + ar + ar^2</math> or <math>a \frac{(1 - r^3)}{1 - r}</math>  <math>= 35 \rightarrow a = 45</math></p> <p>(ii) <math>S_{\infty} = \frac{a}{1 - r} = 27</math></p>	<p>B1 M1 A1 [3]</p> <p>B1</p> <p>M1 A1 [3]</p> <p>M1 A1 <math>\surd</math> [2]</p>	<p>co Use of correct sum formula. co</p> <p>co</p> <p>Solution of equation. co</p> <p>Correct use of formula. <math>\surd</math> for his <math>a</math>.</p>
<p>8 (i) <math>4xh + 2x^2 = 96</math>  <math>\rightarrow h = \frac{24}{x} - \frac{x}{2}</math></p> <p><math>V = x^2h \rightarrow V = 24x - \frac{x^3}{2}.</math></p> <p>(ii) <math>\frac{dV}{dx} = 24 - \frac{3x^2}{2}</math>  <math>= 0</math> when <math>x = 4</math>  <math>\rightarrow V = 64.</math></p> <p>(iii) <math>\frac{d^2V}{dx^2} = -3x \rightarrow \text{Max.}</math></p>	<p>M1 A1</p> <p>M1 [3]</p> <p>B1</p> <p>M1 A1 [3]</p> <p>M1 A1 <math>\surd</math> [2]</p>	<p>Needs to consider at least 5 areas. co</p> <p>for <math>V = x^2h</math> with <math>h</math> as <math>f(x)</math></p> <p>co</p> <p>Sets differential to 0 <b>and</b> solves. co</p> <p>Any valid method. co.</p>

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<p><b>9</b> <math>y = (x-2)^2</math> and <math>y + 2x = 7</math>  Elimination of <math>y \rightarrow x^2 - 2x - 3 = 0</math>  <math>\rightarrow A(-1, 9)</math> and <math>B(3, 1)</math></p> <p>Area under line = <math>\frac{1}{2} \times 4 \times 10</math>  or <math>\int [7x - x^2]</math> from <math>-1</math> to <math>3</math>.</p> <p>Area under curve = <math>\left[ \frac{(x-2)^3}{3} \right]</math></p> <p>or <math>\left[ \frac{x^3}{3} - 2x^2 + 4x \right]</math> from <math>-1</math> to <math>3</math>  <math>\rightarrow 10\frac{2}{3}</math>.  [ok to use <math>\int (y_1 - y_2) dx</math> – marks the same]</p>	<p>M1 DM1A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[8]</p>	<p><math>y</math> (or <math>x</math>) removed completely.  Soln of quadratic. Both points correct.</p> <p>Uses any valid method – integration or area of trapezium etc.</p> <p>Any attempt at integration.</p> <p>Correct integration in either form.</p> <p>Correct use of limits in an integral.</p> <p>co</p>
<p><b>10</b> <math>y = \frac{1}{6}(2x-3)^3 - 4x</math></p> <p>(i) <math>\frac{dy}{dx} = \frac{1}{6} \times 3 \times (2x-3)^2 \times 2 - 4</math></p> <p>(ii) <math>x = 0, y = -\frac{27}{6}</math>,  <math>y + \frac{27}{6} = 5x \rightarrow 2y + 9 = 10x</math></p> <p>(iii) <math>(2x-3)^2 - 4 (&gt; 0)</math>  <math>\rightarrow x = 2\frac{1}{2}</math> or <math>\frac{1}{2}</math>  <math>\rightarrow x &gt; 2\frac{1}{2}, x &lt; \frac{1}{2}</math>.</p>	<p>B2,1</p> <p>B1</p> <p>[3]</p> <p>B1</p> <p>M1 A1</p> <p>[3]</p> <p>M1</p> <p>DM1</p> <p>A1</p> <p>[3]</p>	<p>Everything but the “<math>\times 2</math>”</p> <p>For the “<math>\times 2</math>”, even if B0 given above.</p> <p>For correct <math>y</math> value</p> <p>Must be using calculus for <math>m</math>. co.  (ok unsimplified)</p> <p>Links <math>\frac{dy}{dx}</math> with 0</p> <p>Method for quadratic – lead to 2 answers  Correct set of values.</p>
<p><b>11</b> <math>f: x \mapsto 4 - 3\sin x</math></p> <p>(i) <math>4 - 3\sin x = 2 \rightarrow \sin x = \frac{2}{3}</math>  <math>\rightarrow x = 0.730</math> or <math>2.41</math></p> <p>(ii)</p> <p>(iii) <math>k &lt; 1, k &gt; 7</math>.</p> <p>(iv) <math>A = \frac{3\pi}{2}</math>.</p> <p>(v) <math>\sin x = \frac{1}{3}</math> – or using inverse  <math>g^{-1}(3) = 2.80</math></p>	<p>M1</p> <p>A1 A1√</p> <p>[3]</p> <p>B1</p> <p>B1</p> <p>[2]</p> <p>B1 B1</p> <p>[2]</p> <p>B1</p> <p>[1]</p> <p>M1A1</p> <p>[2]</p>	<p>Makes <math>\sin x</math> the subject + solution.  co. <math>\sqrt{\quad}</math> for <math>\pi</math> – first answer.</p> <p>Must be 1 complete oscillation.  Shape and position correct, in 1<sup>st</sup> quadrant,  curve not lines.</p> <p>B1 for <math>k = 1, 7</math>, B1 for answer  Or B1 for <math>k &lt; 1</math>, B1 for <math>k &gt; 7</math></p> <p>co</p> <p>M1 for soln of <math>3 = 4 - 3\sin x</math> or inverse.</p>