

Cambridge International AS & A Level

MATHEMATICS
Paper 1 Pure Mathematics
MARK SCHEME
Maximum Mark: 75

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Ma	Mathematics-Specific Marking Principles				
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.				
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.				
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.				
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).				
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.				
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.				

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- DM or DB When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

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Abbreviations

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only

ISW Ignore Subsequent Working

SOI Seen Or Implied

SC Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the

light of a particular circumstance)

WWW Without Wrong Working

AWRT Answer Which Rounds To

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Question	Answer	Marks	Guidance
1	$f'(x) = [-(3x+2)^{-2}] \times [3] + [2x]$	B2, 1, 0	
	< 0 hence decreasing	B1	Dependent on at least B1 for $f'(x)$ and must include < 0 or '(always) neg'
		3	

Question	Answer	Marks	Guidance
2	[Stretch] [factor 2, x direction (or y-axis invariant)]	*B1 DB1	
	[Translation or Shift] [1 unit in y direction] or [Translation/Shift] $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$	B1B1	Accept transformations in either order. Allow (0, 1) for the vector
		4	

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Question	Answer	Marks	Guidance
3	$(\pi)\int (y-1)dy$	*M1	SOI Attempt to integrate x^2 or $(y-1)$
	$(\pi)\left[\frac{y^2}{2}-y\right]$	A1	
	$(\pi) \left[\left(\frac{25}{2} - 5 \right) - \left(\frac{1}{2} - 1 \right) \right]$	DM1	Apply limits $1 \rightarrow 5$ to an integrated expression
	8π or AWRT 25.1	A1	
		4	

Question	Answer	Marks	Guidance
4	$\frac{\mathrm{d}y}{\mathrm{d}x} = 2x - 2$	B1	
	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{4}{6}$	B1	OE, SOI
	$their(2x-2) = their\frac{4}{6}$	M1	LHS and RHS must be their $\frac{dy}{dx}$ expression and value
	$x = \frac{4}{3}$ oe	A1	
		4	

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Question	Answer	Marks	Guidance
5	$2\tan\theta - 6\sin\theta + 2 = \tan\theta + 3\sin\theta + 2 \rightarrow \tan\theta - 9\sin\theta \ (=0)$	M1	Multiply by denominator and simplify
	$\sin\theta - 9\sin\theta\cos\theta \ (=0)$	M1	Multiply by $\cos \theta$
	$\sin \theta (1 - 9\cos \theta) (= 0) \rightarrow \sin \theta = 0, \cos \theta = \frac{1}{9}$	M1	Factorise and attempt to solve at least one of the factors = 0
	$\theta = 0$ or 83.6° (only answers in the given range)	A1A1	
		5	

Question	Answer	Marks	Guidance
6(a)	$5C2 \left[2(x)\right]^3 \left[\frac{a}{(x^2)}\right]^2$	B1	SOI Can include correct x's
	$10 \times 8 \times a^2 \left(\frac{x^3}{x^4}\right) = 720 \left(\frac{1}{x}\right)$	B1	SOI Can include correct x's
	$a = \pm 3$	B1	
		3	
6(b)	$5C4 \left[2(x)\right] \left[\frac{their a}{(x^2)}\right]^4$	B1	SOI <i>Their a</i> can be just <u>one</u> of their values (e.g. just 3). Can gain mark from within an expansion but must use <i>their</i> value of <i>a</i>
	810 identified	B1	Allow with x^{-7}
		2	

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Question	Answer	Marks	Guidance
7	$OC = 6\cos 0.8 = 4.18(0)$	M1A1	SOI
	Area sector $OCD = \frac{1}{2} (their 4.18)^2 \times 0.8$	*M1	OE
	$\Delta OCA = \frac{1}{2} \times 6 \times their 4.18 \times \sin 0.8$	M1	OE
	Required area = their $\triangle OCA$ – their sector OCD	DM1	SOI. If not seen <i>their</i> areas of sector and triangle must be seen
	2.01	A1	CWO. Allow or better e.g. 2.0064
		6	

Question	Answer	Marks	Guidance
8(a)	2%	B1	
		1	
8(b)	Bonus = $600 + 23 \times 100 = 2900$	B1	
	Salary = 30000×1.03^{23}	M1	Allow 30000×1.03 ²⁴ (60984)
	= 59207.60	A1	Allow answers of 3significant figure accuracy or better
	their 2900 their 59200	M1	SOI
	4.9(0)%	A1	
		5	

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Question	Answer	Marks	Guidance
9(a)	$\left[2(x+3)^2\right][-7]$	B1B1	Stating $a = 3, b = -7$ gets B1B1
		2	
9(b)	$y = 2(x+3)^2 - 7 \rightarrow 2(x+3)^2 = y+7 \rightarrow (x+3)^2 = \frac{y+7}{2}$	M1	First 2 operations correct. Condone sign error or with x/y interchange
	$x+3=(\pm)\sqrt{\frac{y+7}{2}} \rightarrow x=(\pm)\sqrt{\frac{y+7}{2}}-3 \rightarrow f^{-1}(x)=-\sqrt{\frac{x+7}{2}}-3$	A1FT	FT on their a and b . Allow $y =$
	Domain: $x \geqslant -5$ or $\geqslant -5$ or $[-5, \infty)$	B1	Do not accept $y =, f(x) =, f^{-1}(x) =$
		3	
9(c)	$fg(x) = 8x^2 - 7$	B1FT	SOI. FT on their –7 from part (a)
	$8x^2 - 7 = 193 \rightarrow x^2 = 25 \rightarrow x = -5$ only	B1	
	Alternative method for question 9(c)		
	$g(x) = f^{-1}(193) \rightarrow 2x - 3 = -\sqrt{100} - 3$	M1	FT on their $f^{-1}(x)$
	x = -5 only	A1	
		2	
9(d)	(Largest k is) $-\frac{1}{2}$	B1	Accept $-\frac{1}{2}$ or $k \leqslant -\frac{1}{2}$
		1	

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Question	Answer	Marks	Guidance
10(a)	$2(a+3)^{\frac{1}{2}} - a = 0$	M1	SOI. Set $\frac{dy}{dx} = 0$ when $x = a$. Can be implied by an answer in terms of a
	$4(a+3) = a^2 \to a^2 - 4a - 12 = 0$	M1	Take <i>a</i> to RHS and square. Form 3-term quadratic
	$(a-6)(a+2) \to a=6$	A1	Must show factors, or formula or completing square. Ignore $a = -2$ SC If a is never used maximum of M1A1 for $x = 6$, with visible solution
		3	
10(b)	$\frac{d^2 y}{dx^2} = (x+3)^{\frac{1}{2}} - 1$	B1	
	Sub their $a \to \frac{d^2 y}{dx^2} = \frac{1}{3} - 1 = -\frac{2}{3} \ (or < 0) \to MAX$	M1A1	A mark only if completely correct If the second differential is not $-\frac{2}{3}$ correct conclusion must be drawn to award the M1
		3	
10(c)	$(y=)\frac{2(x+3)^{\frac{3}{2}}}{\frac{3}{2}} - \frac{1}{2}x^2 (+c)$	B1B1	
	Sub $x = their \ a \text{ and } y = 14 \rightarrow 14 = \frac{4}{3}(9)^{\frac{3}{2}} - 18 + c$	M1	Substitute into an integrated expression. c must be present. Expect $c = -4$
	$y = \frac{4}{3}(x+3)^{\frac{3}{2}} - \frac{1}{2}x^2 - 4$	A1	Allow $f(x) = \dots$
		4	

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Question	Answer	Marks	Guidance
11(a)	$(\tan x - 2)(3\tan x + 1)$ (= 0). or formula or completing square	M1	Allow reversal of signs in the factors. Must see a method
	$\tan x = 2 \text{ or } -\frac{1}{3}$	A1	
	$x = 63.4^{\circ}$ (only value in range) or 161.6° (only value in range)	B1FT B1FT	
		4	
11(b)	Apply $b^2 - 4ac < 0$	M1	SOI. Expect $25-4(3)(k) < 0$, tan x must not be in coefficients
	$k > \frac{25}{12}$	A1	Allow $b^2 - 4ac = 0$ leading to correct $k > \frac{25}{12}$ for M1A1
		2	
11(c)	k = 0	M1	SOI
	$\tan x = 0 \text{ or } \frac{5}{3}$	A1	
	$x = 0^{\circ} \text{ or } 180^{\circ} \text{ or } 59.0^{\circ}$	A1	All three required
		3	

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Question	Answer	Marks	Guidance
12(a)	Centre = $(2, -1)$	B1	
	$r^2 = [2 - (-3)]^2 + [-1 - (-5)]^2$ or $[2 - 7]^2 + [-1 - 3]^2$ OE	M1	OR $\frac{1}{2} \left[\left(-3 - 7 \right)^2 + \left(-5 - 3 \right)^2 \right]$ OE
	$(x-2)^2 + (y+1)^2 = 41$	A1	Must not involve surd form SCB3 $(x+3)(x-7)+(y+5)(y-3)=0$
		3	
12(b)	Centre = their $(2, -1) + {8 \choose 4} = (10, 3)$	B1FT	SOI FT on their (2, -1)
	$(x-10)^2 + (y-3)^2 = their 41$	B1FT	FT on <i>their</i> 41 even if in surd form SCB2 $(x-5)(x-15)+(y+1)(y-7)=0$
		2	

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Question	Answer	Marks	Guidance
12(c)	Gradient <i>m</i> of line joining centres = $\frac{4}{8}$ OE	B1	
	Attempt to find mid-point of line.	M1	Expect (6, 1)
	Equation of RS is $y-1=-2(x-6)$	M1	Through <i>their</i> $(6, 1)$ with gradient $\frac{-1}{m}$
	y = -2x + 13	A1	AG
	Alternative method for question 12(c)		
	$(x-2)^2 + (y+1)^2 - 41 = (x-10)^2 + (y-3)^2 - 41 \text{ OE}$	M1	
	$x^2 - 4x + 4 + y^2 + 2y + 1 = x^2 - 20x + 100 + y^2 - 6y + 9$ OE	A1	Condone 1 error or errors caused by 1 error in the first line
	16x + 8y = 104	A1	
	y = -2x + 13	A1	AG
		4	
12(d)	$(x-10)^{2} + (-2x+13-3)^{2} = 41$	M1	Or eliminate y between C ₁ and C ₂
	$x^{2} - 20x + 100 + 4x^{2} - 40x + 100 = 41 \rightarrow 5x^{2} - 60x + 159 = 0$	A1	AG
		2	

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