## **Vectors - 2020 A2**

1. Nov/2020/Paper\_9709/31/No.11

Two lines have equations  $\mathbf{r} = \mathbf{i} + 2\mathbf{j} + \mathbf{k} + \lambda(a\mathbf{i} + 2\mathbf{j} - \mathbf{k})$  and  $\mathbf{r} = 2\mathbf{i} + \mathbf{j} - \mathbf{k} + \mu(2\mathbf{i} - \mathbf{j} + \mathbf{k})$ , where a is a constant.

(a) Given that the two lines intersect, find the value of a and the position vector of the point of intersection. [5]

Palpa Califild (1) (b) Given instead that the acute angle between the directions of the two lines is  $\cos^{-1}(\frac{1}{6})$ , find the two possible values of a.

## **2.** Nov/2020/Paper\_9709/32/No.8

With respect to the origin O, the position vectors of the points A, B, C and D are given by

$$\overrightarrow{OA} = \begin{pmatrix} 2 \\ 1 \\ 5 \end{pmatrix}, \quad \overrightarrow{OB} = \begin{pmatrix} 4 \\ -1 \\ 1 \end{pmatrix}, \quad \overrightarrow{OC} = \begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix} \quad \text{and} \quad \overrightarrow{OD} = \begin{pmatrix} 3 \\ 2 \\ 3 \end{pmatrix}.$$

(a) Show that AB = 2CD. [3]

- (b) Find the angle between the directions of  $\overrightarrow{AB}$  and  $\overrightarrow{CD}$ . [3]
- (c) Show that the line through A and B does not intersect the line through C and D. [4]

**3.** June/2020/Paper\_9709/32/No.9

With respect to the origin O, the vertices of a triangle ABC have position vectors

$$\overrightarrow{OA} = 2\mathbf{i} + 5\mathbf{k}$$
,  $\overrightarrow{OB} = 3\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$  and  $\overrightarrow{OC} = \mathbf{i} + \mathbf{j} + \mathbf{k}$ .

[3]

[2]

(a) Using a scalar product, show that angle ABC is a right angle.

**(b)** Show that triangle *ABC* is isosceles.

(c) Find the exact length of the perpendicular from O to the line through B and C. [4]

## **4.** June/2020/Paper\_9709/32/No.10

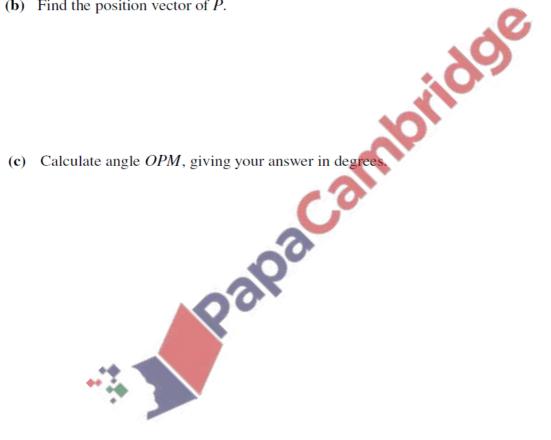
With respect to the origin O, the points A and B have position vectors given by  $\overrightarrow{OA} = 6\mathbf{i} + 2\mathbf{j}$  and  $\overrightarrow{OB} = 2\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$ . The midpoint of OA is M. The point N lying on AB, between A and B, is such that AN = 2NB.

(a) Find a vector equation for the line through M and N. [5]

The line through M and N intersects the line through O and B at the point P.

**(b)** Find the position vector of *P*. [3]

[3]



**5.** June/2020/Paper\_9709/33/No.8

Relative to the origin O, the points A, B and D have position vectors given by

$$\overrightarrow{OA} = \mathbf{i} + 2\mathbf{j} + \mathbf{k}$$
,  $\overrightarrow{OB} = 2\mathbf{i} + 5\mathbf{j} + 3\mathbf{k}$  and  $\overrightarrow{OD} = 3\mathbf{i} + 2\mathbf{k}$ .

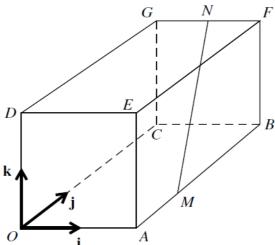
A fourth point C is such that ABCD is a parallelogram.

(a) Find the position vector of C and verify that the parallelogram is not a rhombus. [5]

**(b)** Find angle *BAD*, giving your answer in degrees. [3]

(c) Find the area of the parallelogram correct to 3 significant figures. [2]

## **6.** March/2020/Paper\_9709/32/No.8



In the diagram, OABCDEFG is a cuboid in which OA = 2 units, OC = 3 units and OD = 2 units. Unit vectors  $\mathbf{i}$ ,  $\mathbf{j}$  and  $\mathbf{k}$  are parallel to OA, OC and OD respectively. The point M on AB is such that MB = 2AM. The midpoint of FG is N.

(a) Express the vectors  $\overrightarrow{OM}$  and  $\overrightarrow{MN}$  in terms of i, j and k. [3]

**(b)** Find a vector equation for the line through M and N.





(c) Find the position vector of P, the foot of the perpendicular from D to the line through M and N. [4]