

Vectors – 2021 A2 Nov P3

1. Nov/2021/Paper_9709/31/No.9

Two lines l and m have equations $\mathbf{r} = 3\mathbf{i} + 2\mathbf{j} + 5\mathbf{k} + s(4\mathbf{i} - \mathbf{j} + 3\mathbf{k})$ and $\mathbf{r} = \mathbf{i} - \mathbf{j} - 2\mathbf{k} + t(-\mathbf{i} + 2\mathbf{j} + 2\mathbf{k})$ respectively.

- (a) Show that l and m are perpendicular. [2]

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- (b) Show that l and m intersect and state the position vector of the point of intersection. [5]

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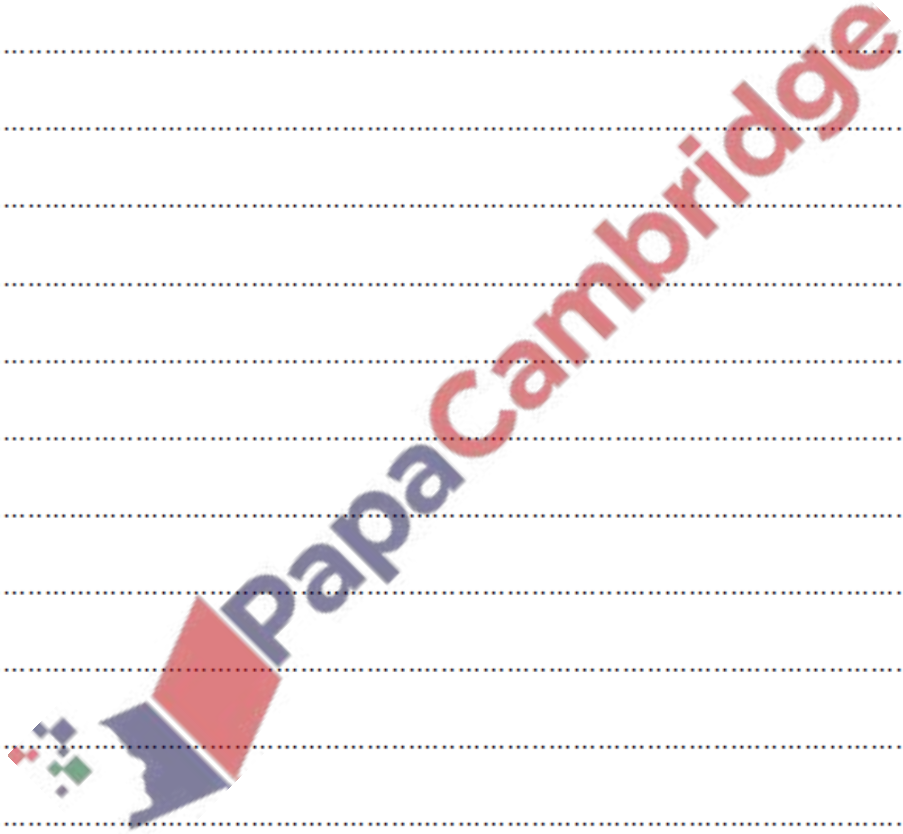
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- (c) Show that the length of the perpendicular from the origin to the line m is $\frac{1}{3}\sqrt{5}$. [4]



With respect to the origin O , the position vectors of the points A and B are given by $\vec{OA} = \begin{pmatrix} 1 \\ 2 \\ -1 \end{pmatrix}$ and $\vec{OB} = \begin{pmatrix} 0 \\ 3 \\ 1 \end{pmatrix}$.

- (a) Find a vector equation for the line l through A and B . [3]

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- (b) The point C lies on l and is such that $\vec{AC} = 3\vec{AB}$. Find the position vector of C . [2]

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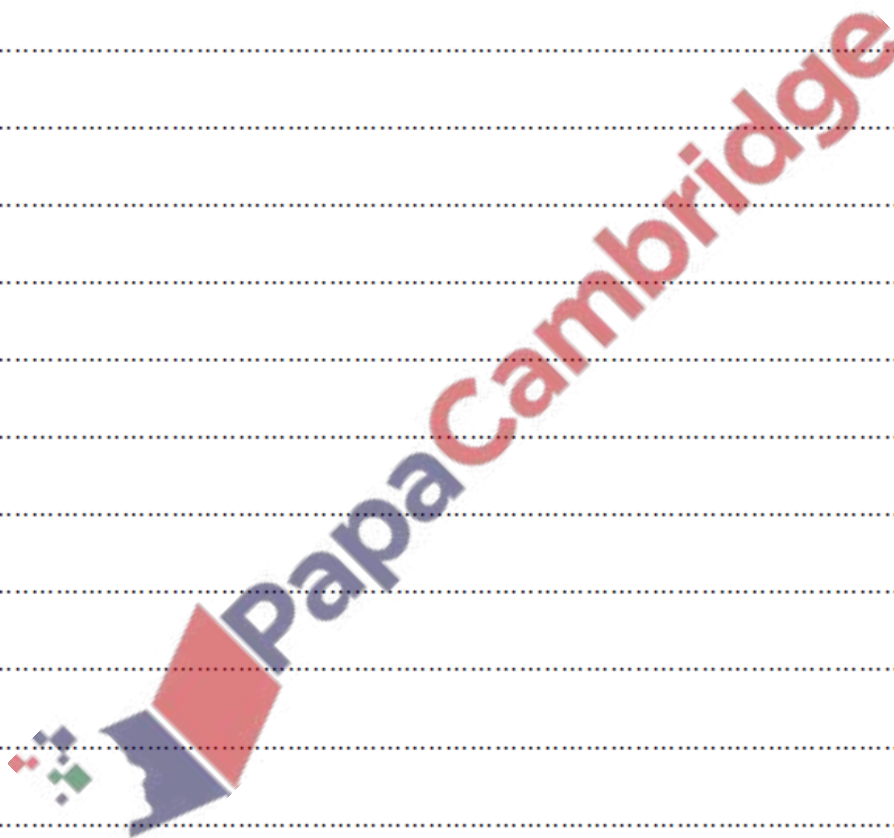
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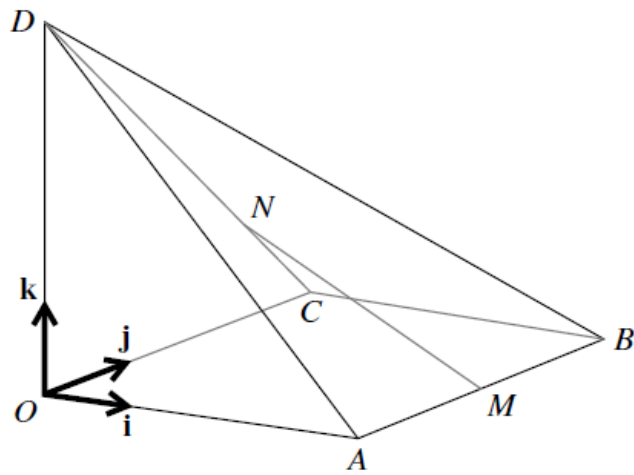
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(c) Find the possible position vectors of the point P on l such that $OP = \sqrt{14}$.

[5]





In the diagram, $OABCD$ is a pyramid with vertex D . The horizontal base $OABC$ is a square of side 4 units. The edge OD is vertical and $OD = 4$ units. The unit vectors \mathbf{i} , \mathbf{j} and \mathbf{k} are parallel to OA , OC and OD respectively.

The midpoint of AB is M and the point N on CD is such that $DN = 3NC$.

- (a) Find a vector equation for the line through M and N . [5]

(b) Show that the length of the perpendicular from O to MN is $\frac{1}{3}\sqrt{82}$.

[4]

