## <u>Differential Equations – 2022 A2 June</u>

1.	March.	/2022	/Paper	9709	/32	/No.9
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The variables x and y satisfy the differential equation

$$(x+1)(3x+1)\frac{\mathrm{d}y}{\mathrm{d}x} = y,$$

and it is given that y = 1 when x = 1.

Solve the differential equation and find the exact value of $y$ when $x = 3$ , giving your answer in a simplified form.
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$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{xy}{1+x^2},$
and $y = 2$ when $x = 0$ .
Solve the differential equation, obtaining a simplified expression for $y$ in terms of $x$ . [7]
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**2.** June/2022/Paper\_9709/31/No.4 The variables x and y satisfy the differential equation

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3.	June, The	/2022/Paper_9709/32/No.6 variables $x$ and $y$ satisfy the differential equation
		$\frac{\mathrm{d}y}{\mathrm{d}x} = x\mathrm{e}^{y-x},$
	and	y = 0 when $x = 0$ .
	(a)	Solve the differential equation, obtaining an expression for $y$ in terms of $x$ . [7]
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Find the value of $y$ when $x = 1$ , giving your answer in the form $a - \ln b$ , where $a$ and $b$ are integers.

**(b)** 

	ne number of insects is modelled by a differential equation of the form $\frac{dN}{dt} = kN^{\frac{3}{2}}\cos 0.02t$ , where a constant and $N$ is a continuous variable. It is given that when $t = 0$ , $N = 100$ .
(a)	Solve the differential equation, obtaining a relation between $N$ , $k$ and $t$ . [5]
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At time t days after the start of observations, the number of insects in a population is N. The variation

**4.** June/2022/Paper\_9709/33/No.8

(	Given also that $N = 625$ when $t = 50$ , find the value of $k$ .
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	Obtain an expression for $N$ in terms of $t$ , and find the greatest value of $N$ predicted by this m
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	Obtain an expression for $N$ in terms of $t$ , and find the greatest value of $N$ predicted by this m
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