Differentiation and integration-2023 March Cambridge AS & A Level Mathematics

1. March/2023/Paper_9709/32/No.5

The parametric equations of a curve are

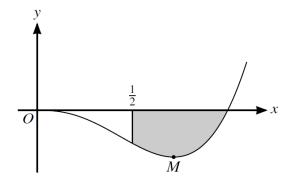
$$x = te^{2t}$$
, $y = t^2 + t + 3$.

(a) Show that
$$\frac{dy}{dx} = e^{-2t}$$
. [3]

norios (b) Hence show that the normal to the curve, where t = -1, passes through the point $\left(0, 3 - \frac{1}{e^4}\right)$. Papa

[3]

2. March/2023/Paper_9709/32/No.8



[4]

The diagram shows the curve $y = x^3 \ln x$, for x > 0, and its minimum point *M*.

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(a) Find the exact coordinates of M.

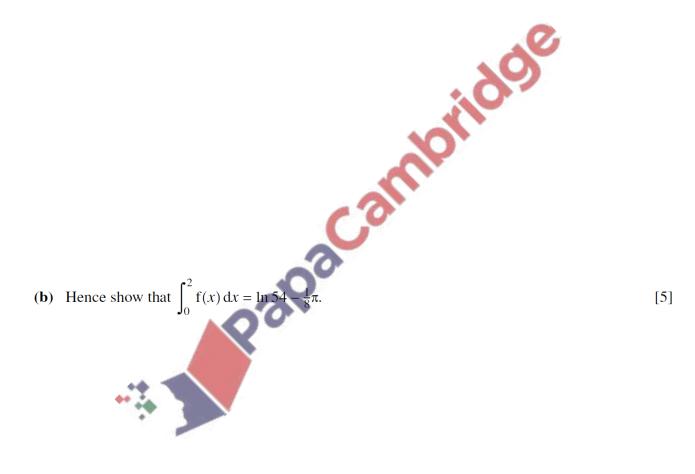
(**b**) Find the exact area of the shaded region bounded by the curve, the *x*-axis and the line $x = \frac{1}{2}$. [5]

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3. March/2023/Paper_9709/32/No.11

Let
$$f(x) = \frac{5x^2 + x + 11}{(4 + x^2)(1 + x)}$$
.

(a) Express f(x) in partial fractions.



[5]