The Poisson distribution – 2023 March Cambridge AS & A Level Mathematics

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The number of orders arriving at a shop during an 8-hour working day is modelled by the random variable X with distribution Po(25.2).

(a) State **two** assumptions that are required for the Poisson model to be valid in this context. [2]

(b) (i) Find the probability that the number of orders that arrive in a randomly chosen 3-hour period is between 3 and 5 inclusive. [3]

(ii) Find the probability that, in two randomly chosen 1-hour periods, exactly 1 order will arrive in one of the 1-hour periods, and at least 2 orders will arrive in the other 1-hour period. [4]



(c) The shop can only deal with a maximum of 120 orders during any 36-hour period.

Use a suitable approximating distribution to find the probability that, in a randomly chosen 36-hour period, there will be too many orders for the shop to deal with. [4]