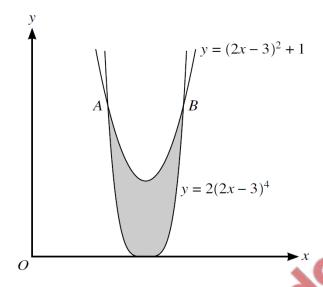
<u>Integration – 2023 AS Mathematics 9709</u>

1. Nov/2023/Paper_9709/11/No.8



The diagram shows the curves with equations $y = 2(2x - 3)^4$ and $y = (2x - 3)^2 + 1$ meeting at points A and B.

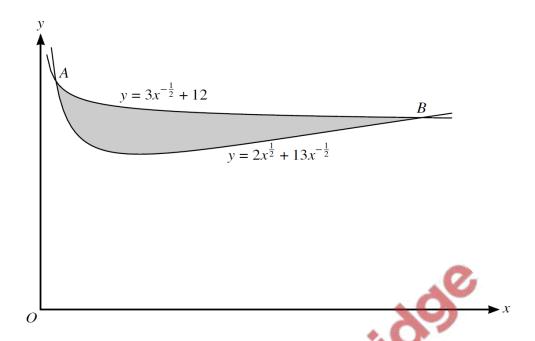
(a)	By using the substitution $u = 2x - 3$ find, by calculation, the coordinates of A and B . [4]
	CP .
	1 000

Find the exact are	a of the shaded region.	
		0-
		100
		109
	~	
	(0)	
	40	
	VO.0.	
•		

Nov	/2023/Paper_9709/12/No.3	
The equation of a curve is such that $\frac{dy}{dx} = \frac{1}{2}x + \frac{72}{x^4}$. The curve passes through the point $P(2, 8)$.		
(a)	Find the equation of the normal to the curve at <i>P</i> .	[2]
		•••••
	20	
(b)	Find the equation of the curve.	[4]
	100	

2.

3. Nov/2023/Paper_9709/12/No.9



The diagram shows curves with equations $y = 2x^{\frac{1}{2}} + 13x^{-\frac{1}{2}}$ and $y = 3x^{-\frac{1}{2}} + 12$. The curves intersect at points *A* and *B*.

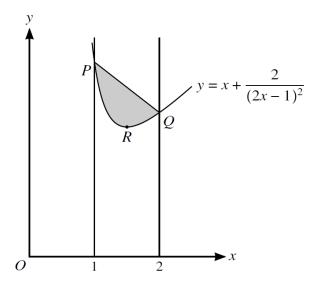
(a)	Find the coordinates of A and B .		[4]
		O'O'	
	.00	X	

)	Hence find the area of the shaded region.	[5]
		•••••
	Co	
		•••••
		•••••
		•••••
		•••••

Nov/2023/Paper_9709/13/No.1
A curve is such that its gradient at a point (x, y) is given by $\frac{dy}{dx} = x - 3x^{-\frac{1}{2}}$. It is given that the curve passes through the point $(4, 1)$.
Find the equation of the curve. [4]

5. Nov/2023/Paper_9709/13/No.11

(a)



The diagram shows part of the curve with equation $y = x + \frac{2}{(2x-1)^2}$. The lines x = 1 and x = 2 intersect the curve at P and Q respectively and R is the stationary point on the curve.

Verify that the <i>x</i> -coordinate of <i>R</i> is $\frac{3}{2}$ and find the <i>y</i> -coordinate of <i>R</i> .	[4]
50	
	•••••

Find the exact value of the area of the shaded region.	[6]
	••••••
<u>.0</u>	
29	
(2)	

(b)