

1. Nov/2021/Paper_41/No.9

- (a) State, by reference to the power dissipated in a resistor, what is meant by the root-mean-square (r.m.s.) value of an alternating voltage.

Is the value of constant voltage (or current) that produces the same power in a resistor as the mean power of the alternating voltage (or current). [2]

- (b) A coil is rotating freely, on frictionless bearings, at constant speed in a uniform magnetic field. This rotation causes an induced alternating electromotive force (e.m.f.) across the open terminals of the coil. The induced e.m.f. has r.m.s. value 12 V and frequency 50 Hz.

The speed of rotation of the coil is now doubled.

- (i) State and explain, with reference to the principles of electromagnetic induction, the effect of the increased speed of rotation on the r.m.s. value of the induced e.m.f.

- At high speed, the rate of cutting of flux will double. This doubles the r.m.s. and thus doubles the induced e.m.f. [2]



- (ii) On Fig. 9.1, sketch the variation with time t of the induced e.m.f. E across the terminals of the coil at the **increased** speed of rotation. Your line should extend from time $t = 0$ to time $t = 20$ ms. Assume that $E = 0$ when $t = 0$.

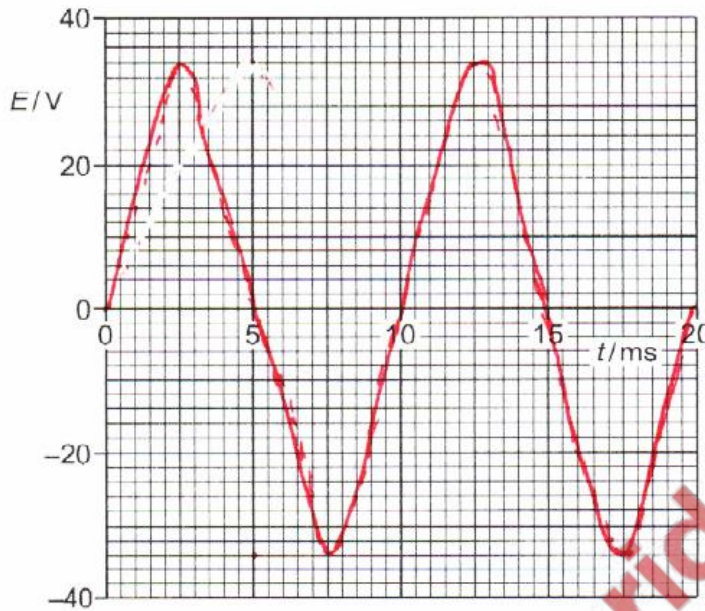


Fig. 9.1

$$V_{r.m.s} = \frac{V_0}{\sqrt{2}}$$

$$V_0 = V_{r.m.s} \times \sqrt{2}$$

$$= 24 \times \sqrt{2}$$

$$= 33.9 \text{ V}$$

$$\approx 34 \text{ V}$$

$$T = \frac{1}{50}$$

$$= 0.02 \text{ s}$$

$$= 20 \text{ ms}$$

Double speed
will half the
period

$$\frac{20}{2} = 10 \text{ ms}$$

[3]

$$\therefore T = 10 \text{ ms.}$$

- (c) State and explain the effect on the motion of the coil in (b) of connecting a load resistor across its terminals.

- Current flowing in the resistor
dissipates the energy of rotation
so the coil will stop to rotate.

[2]

[Total: 9]

Fig. 10.1 shows a simple laminated iron-cored transformer consisting of a primary coil of 25000 turns and a secondary coil of 625 turns.

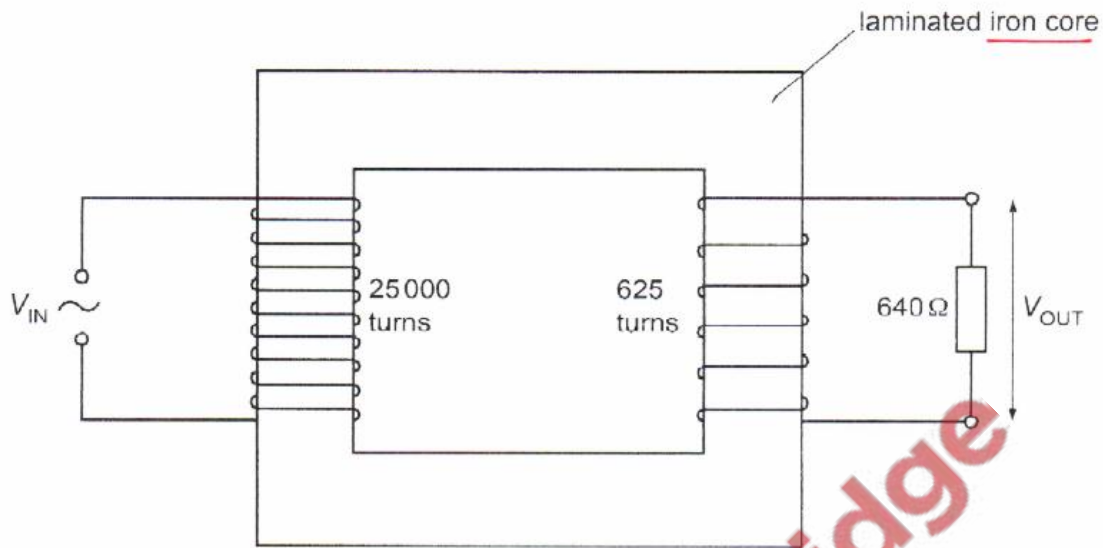


Fig. 10.1

The output potential difference (p.d.) V_{OUT} is applied to a load resistor of resistance $640\ \Omega$.

(a) (i) State the function of the iron core.

to increase the magnetic flux linkage between the coils. [1]

(ii) Explain why the iron core is laminated.

- To reduce eddy currents (induced currents) and hence minimise energy losses. [2]

(b) The input p.d. V_{IN} is a sinusoidal alternating voltage of peak value 12 kV and period 40 ms .

(i) Calculate the maximum value of V_{OUT} .

$$\frac{V_{out}}{V_{in}} = \frac{N_s}{N_p}$$

$$V_{out} = V_{in} \times \frac{N_s}{N_p}$$

$$V_{out} = \frac{12000 \times 625}{25000}$$

$$= 300\text{ V}$$

maximum $V_{OUT} = \dots\dots\dots 300 \dots\dots\dots \text{ V}$ [1]

(ii) Calculate the root-mean-square (r.m.s.) current in the load resistor.

$$I = \frac{V}{R} \quad I_{rms} = \frac{300V}{640\Omega} \div \sqrt{2} \quad I_{r.m.s} = 0.33 \text{ A}$$

$$I_{rms} = \frac{I_0}{\sqrt{2}} \quad = \frac{300}{640 \times \sqrt{2}}$$

r.m.s. current = 0.33 A [1]

(iii) On Fig. 10.2, sketch the variation with time t of the power P dissipated in the load resistor for time $t = 0$ to $t = 40$ ms. Assume that $P = 0$ when $t = 0$.

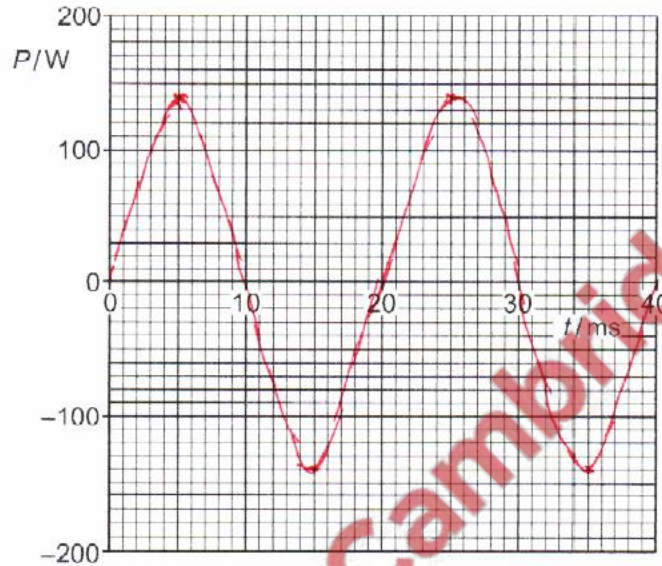


Fig. 10.2

$$I_{r.m.s} = \frac{I_0}{\sqrt{2}}$$

$$I_0 = I_{r.m.s} \times \sqrt{2}$$

$$= 0.33 \times \sqrt{2}$$

$$= 0.47 \text{ A}$$

$$P = I \times V$$

$$= 0.47 \times 300$$

$$= 140 \text{ W}$$

[3]

(c) Explain, with reference to Fig.10.2, why the mean power in the load resistor is 70W.

- The power curve is symmetrical about the midpoint on the power axis
 - So the mean power is half the peak power.

[2]

[Total: 10]

(a) By reference to heating effect, explain what is meant by the *root-mean-square (r.m.s.)* value of an alternating current.

- this is the value of direct current
that produces the same heating effect
as the alternating current [2]

(b) The variations with time t of two currents I_1 and I_2 are shown in Fig. 10.1 and Fig. 10.2.

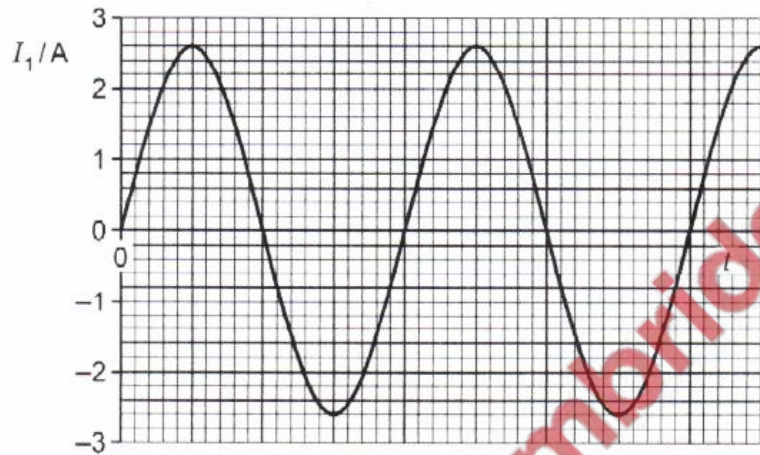


Fig. 10.1

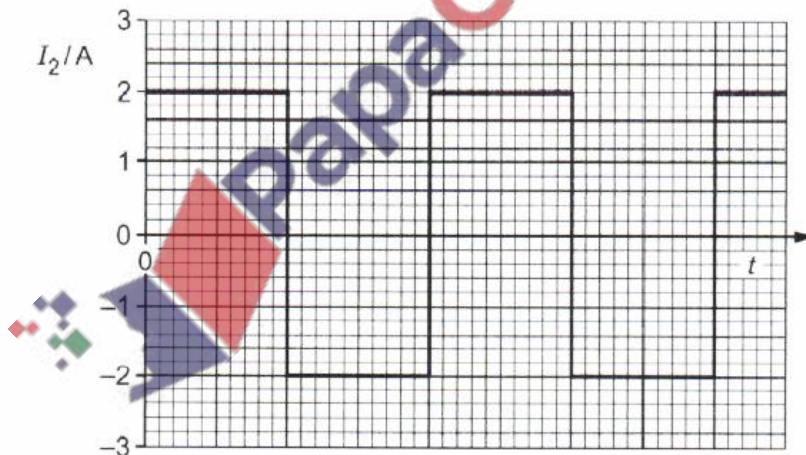


Fig. 10.2

(i) Use Fig. 10.1 to determine the peak value and the r.m.s. value of the current I_1 .

$$I_{\text{rms}} = \frac{I_0}{\sqrt{2}}$$

$$= \frac{2.6}{\sqrt{2}} = 1.838 \approx 1.8$$

peak value = 2.6 A

r.m.s. value = 1.8 A [1]

(ii) Use Fig. 10.2 to determine the peak value and the r.m.s. value of the current I_2 .

peak value = 2.0 A

r.m.s. value = 2.0 A

The current I_2 is not fluctuating only (changes direction at constant time). [1]

(c) The variation with time t of the supply voltage V to a house is given by the expression

$$V = 240 \sin kt$$

where V is in volts, t is in seconds and k is a constant with unit rads^{-1} .

(i) The frequency of the supply voltage is 50 Hz. \uparrow angular velocity

Determine k to two significant figures.

$$\omega = 2\pi f$$

$$\therefore k = 2\pi f$$

$$= 2\pi \times 50$$

$$= 310 \text{ rad s}^{-1}$$

$k = \dots\dots\dots 310 \dots\dots\dots \text{ rad s}^{-1}$ [2]

(ii) The supply voltage is applied to a heater. The mean power of the heater is 3.2 kW.

Calculate the resistance of the heater.

$$P = \frac{V_{\text{rms}}^2}{R}$$

$$R = \frac{V_{\text{rms}}^2}{P}$$

$$V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$$

$$= \frac{240}{\sqrt{2}}$$

$$V_{\text{rms}} = 169.7 \text{ V}$$

$$\therefore R = \frac{169.7^2}{3.2 \times 10^3}$$

$$= 8.999 \Omega$$

$$\approx 9.0$$

resistance = 9.0 Ω [2]

[Total: 8]

The output potential difference (p.d.) of an alternating power supply is represented by

$$V = 320 \sin(100\pi t)$$

$$V = V_0 \sin \omega t$$

where V is the p.d. in volts and t is the time in seconds.

(a) Determine the root-mean-square (r.m.s.) p.d. of the power supply.

$$V_{r.m.s} = \frac{V_0}{\sqrt{2}}$$

$$= \frac{320}{\sqrt{2}} = 226$$

r.m.s. p.d. = 230V V [1]

(b) Determine the period T of the output.

$$\omega = 100\pi$$

$$T = \frac{2\pi}{\omega}$$

$$= \frac{2\pi}{100\pi} = \frac{2}{100} = 0.02$$

$T =$ 0.02 s [2]

(c) The power supply is connected to resistor R and a diode in the circuit shown in Fig. 10.1.

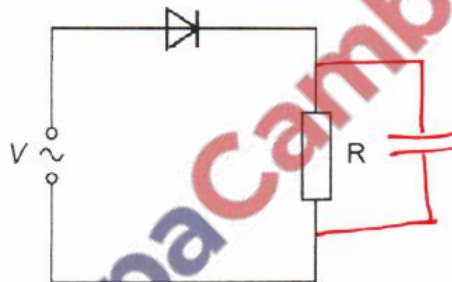
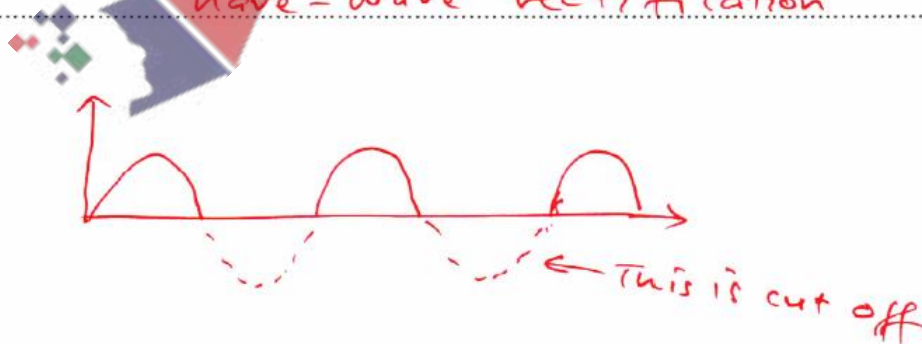


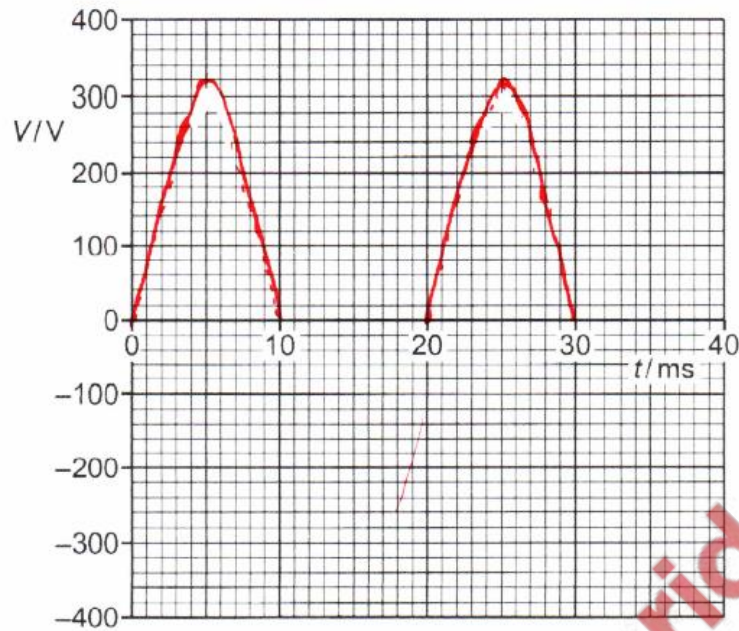
Fig. 10.1

(i) State the name of the type of rectification produced by the diode in Fig. 10.1.

..... half-wave rectification [1]



- (ii) On Fig. 10.2 sketch the variation with time t of the p.d. V_R across R from time $t = 0$ to time $t = 40$ ms.



$$V_0 = 320 \text{ V}$$

$$T = 0.02$$

$$= 20 \text{ ms.}$$

Fig. 10.2

[3]

- (iii) On Fig. 10.1, draw the symbol for a component that may be connected to produce smoothing of V_R .

[1]

↑ done by a capacitor.

[Total: 8]

