

1. Nov/2022/Paper_41/No.7

(a) A sinusoidal alternating voltage has a root-mean-square (r.m.s.) potential difference (p.d.) of 4.2V and a frequency of 50 kHz.

(i) The alternating voltage is applied across a resistor of resistance 760Ω.

By considering the peak voltage, show that the maximum power dissipated by the resistor is 46 mW.

$$V_{rms} = \frac{V_0}{\sqrt{2}}$$

$$\begin{aligned} V_0 &= V_{r.m.s} \times \sqrt{2} \\ &= 4.2 \times \sqrt{2} \\ &= 5.9 \text{ V} \end{aligned}$$

$$P = \frac{V^2}{R}$$

$$= \frac{5.9^2}{760}$$

$$= 0.046 \text{ W}$$

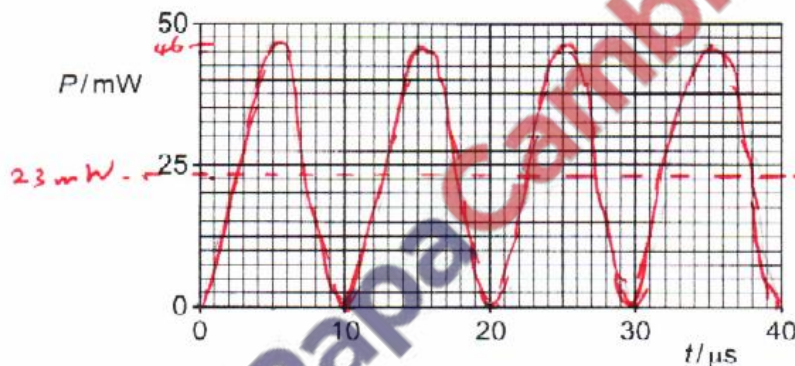
$$\approx 4.6 \times 10^{-2} \text{ W}$$

$$= 46 \times 10^{-3} \text{ W}$$

$$= \underline{46 \text{ mW}}$$

[2]

(ii) On Fig. 7.1, draw a smooth curve to show how the power P dissipated in the resistor varies with time t between $t = 0$ and $t = 40 \mu\text{s}$. Assume that $P = 0$ when $t = 0$.



$$\begin{aligned} T &= \frac{1}{f} \\ &= \frac{1}{50 \times 10^3} \\ &= 0.00002 \text{ s.} \\ &= 20 \mu\text{s} \end{aligned}$$

Fig. 7.1

[3]

(iii) Use your line in (a)(ii) to explain why the mean power dissipated in the resistor is 23 mW.

The graph is symmetrical at around $P = 23 \text{ mW}$ line.

[1]

(b) The alternating voltage in (a) is now applied to a piezoelectric crystal in air.

(i) Explain what happens to the air surrounding the crystal.

- the alternating p-d makes the crystal to vibrate.
- The vibration of crystals cause air to vibrate in the frequency of ultrasound $f > 20,000 \text{ Hz}$ [3]

(ii) A second piezoelectric crystal is placed in the air near to the first crystal.

Explain the effect of the surrounding air in (b)(i) on the second crystal.

- air makes the 2nd crystal to vibrate and this causes an emf to be generated across the 2nd crystal. [1]
- [Total: 10]



(a) State Lenz's law of electromagnetic induction.

- Direction of the induced e.m.f is such that it tends to oppose the flux change causing it. [2]

(b) Two coils of insulated wire are wound on an iron bar, as shown in Fig. 8.1.

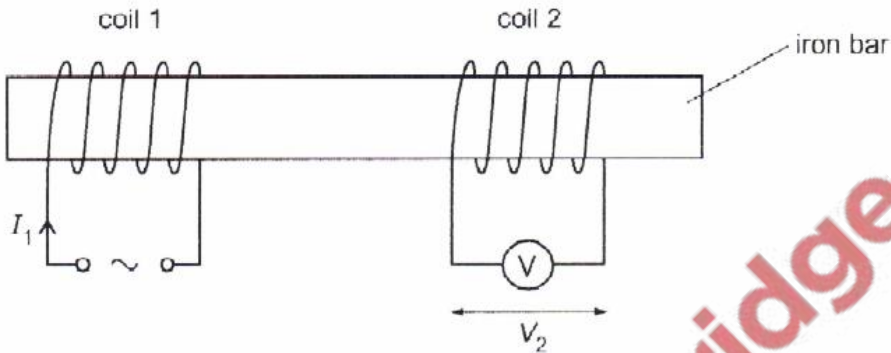


Fig. 8.1

There is a current I_1 in coil 1 that varies with time t as shown in Fig. 8.2.

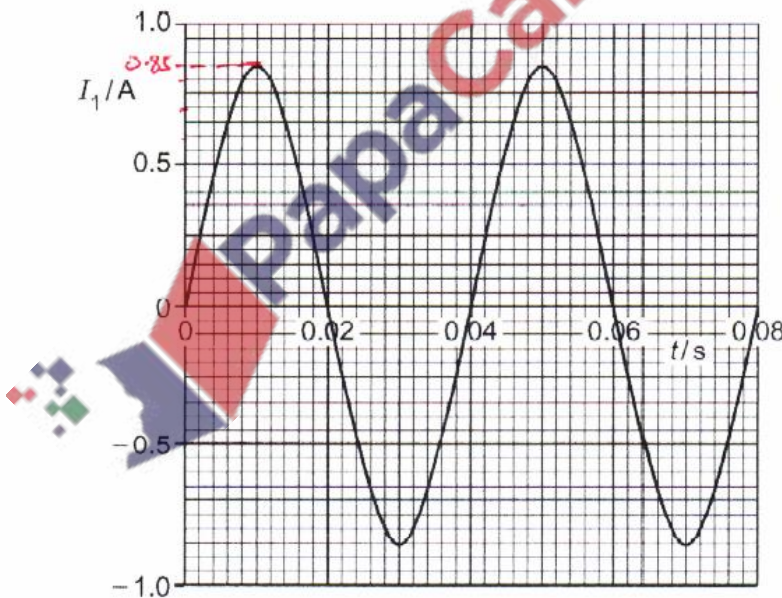


Fig. 8.2

- (i) The variation with t of I_1 can be represented by the equation

$$I_1 = X \sin Yt$$

$$I = I_0 \sin \omega t$$

\uparrow \uparrow
 X Y

where X and Y are constants.

Use Fig. 8.2 to determine the values of X and Y . Give units with your answers.

$$I_0 = \text{Peak value} = 0.85 \text{ A}$$

$$X = 0.85 \text{ unit A}$$

$$\omega = \frac{2\pi}{T} = \frac{2\pi}{0.04} = 160 \text{ rad s}^{-1}$$

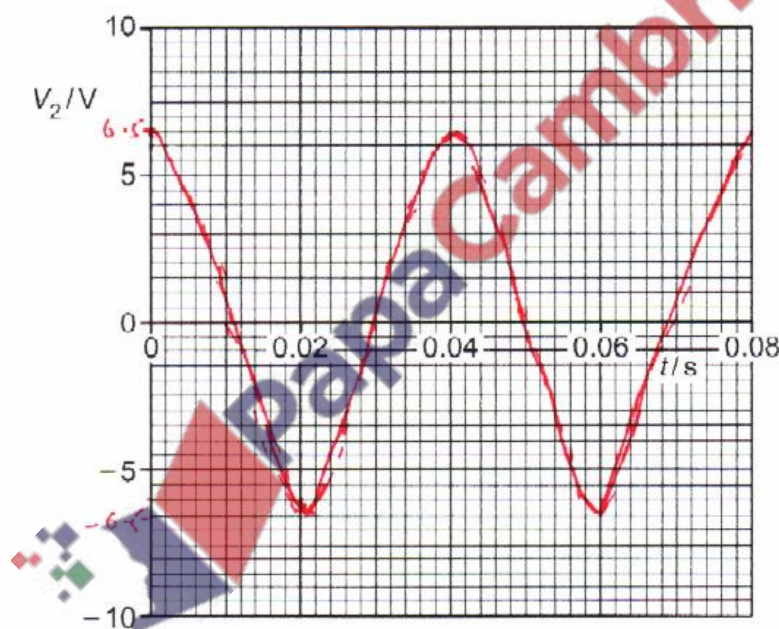
$$Y = 160 \text{ unit rad s}^{-1}$$

[3]

- (ii) The current in coil 1 gives rise to a magnetic field in the iron bar. Assume that the flux density of this magnetic field is proportional to I_1 .

An alternating electromotive force (e.m.f.) is induced across coil 2. The p.d. across coil 2 is measured using the voltmeter and has a root-mean-square (r.m.s.) value of 4.6 V.

On Fig. 8.3, sketch a line to show the variation with t of V_2 between $t = 0$ and $t = 0.08$ s.



$$V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$$

$$V_0 = V_{\text{rms}} \sqrt{2} = 4.6 \times \sqrt{2} = 6.5 \text{ V}$$

V_2 max/min when $I = 0, 0.02, 0.04, 0.06, 0.08$

Fig. 8.3

[3]

- (iii) Use the laws of electromagnetic induction to explain the shape of your line in (b)(ii).

- Magnitude of induced e.m.f. (V_2) is proportional to rate of change of magnetic flux.
- V_2 is proportional to gradient in $I_1 - t$ graph.
- V_2 is zero at maximum/minimum current in $I_1 - t$ curve.

[3]

[Total: 11]

Fig. 5.1 shows four diodes and a load resistor of resistance $1.2\text{ k}\Omega$, connected in a circuit that is used to produce rectification of an alternating voltage.

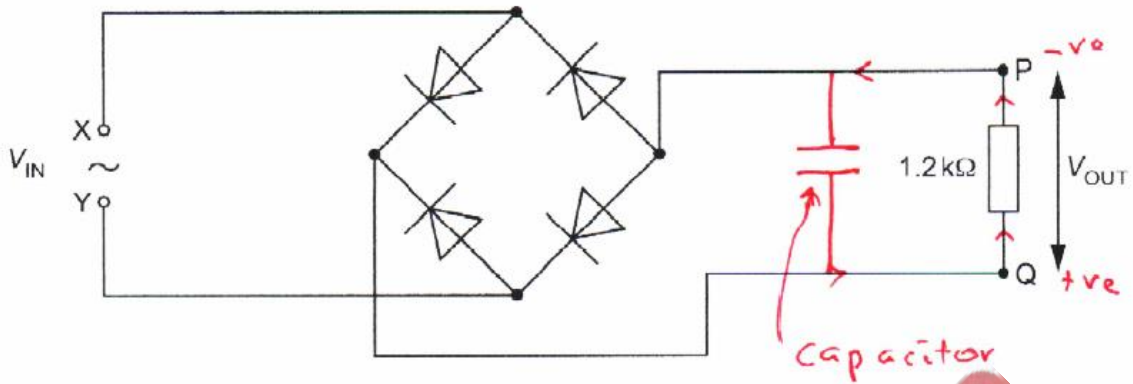


Fig. 5.1

(a) (i) State what is meant by rectification.

Is the conversion of a.c. to d.c.

..... [1]

(ii) State the type of rectification produced by the circuit in Fig. 5.1.

full wave rectification.

..... [1]

(b) A sinusoidal alternating voltage V_{IN} is applied across the input terminals X and Y. The variation with time t of V_{IN} is given by the equation

$$V_{IN} = 6.0 \sin 25\pi t$$

$$V = V_0 \sin \omega t$$

where V_{IN} is in volts and t is in seconds.

(i) On Fig. 5.1, label the output terminals P and Q with the appropriate symbols to indicate the polarity of the output voltage V_{OUT} . [1]

*Current flows from Q to P.
So Q is +ve while P is -ve.*

(ii) The magnitude of the output voltage V_{OUT} varies with t as shown in Fig. 5.2.



Fig. 5.2

On Fig. 5.2, label both of the axes with the correct scales. Use the space below for any working that you need.

$$\begin{aligned}
 V_0 &= 6 \text{ V} & T &= \frac{2\pi}{\omega} \\
 \omega &= 25\pi & &= \frac{2\pi}{0.08} \\
 \omega &= \frac{2\pi}{T} & &= 0.08 \text{ s}
 \end{aligned}$$

[3]

(c) The output voltage in (b) is smoothed by adding a capacitor to the circuit in Fig. 5.1. The difference between the maximum and minimum values of the smoothed output voltage is 10% of the peak voltage.

$$\begin{aligned}
 100\% &- 6 \text{ V} \\
 90\% &- ? & \frac{96 \times 6}{100} &= 5.4 \text{ V}
 \end{aligned}$$

(i) On Fig. 5.1, draw the circuit symbol for a capacitor showing the capacitor correctly connected into the circuit. [1]

(ii) On Fig. 5.2, sketch the variation with t of the smoothed output voltage. [2]

(iii) Calculate the capacitance C of the capacitor.

$$\begin{aligned}
 V_0 &= 6.0 \text{ V} \\
 V &= 0.9 \times 6.0 \\
 &= 5.4 \text{ V} \\
 \text{discharge time} &= 0.054 - 0.02 \\
 &= 0.034 \text{ s} \\
 V &= V_0 e^{-\frac{t}{RC}} \\
 5.4 &= 6 e^{-\frac{0.034}{1.2 \times 10^3 \times C}} \\
 \ln\left(\frac{5.4}{6}\right) &= -\left(\frac{0.034}{1.2 \times 10^3 \times C}\right) \\
 -0.11 &= -\frac{0.034}{1.2 \times 10^3 \times C} \\
 C &= \frac{0.034}{1.2 \times 10^3 \times 0.11} \\
 C &= \dots\dots\dots 2.6 \times 10^{-4} \text{ F} \quad [3]
 \end{aligned}$$

[Total: 12]

- (a) Alternating current (a.c.) is converted into direct current (d.c.) using a full-wave rectification circuit. Part of the diagram of this circuit is shown in Fig. 7.1.

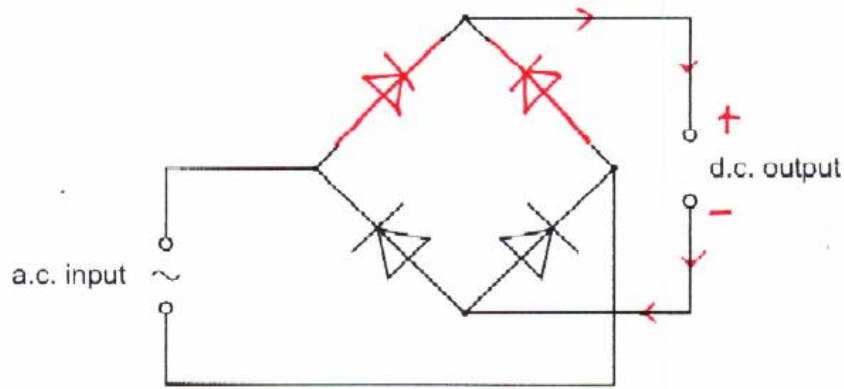


Fig. 7.1

- (i) Complete the circuit in Fig. 7.1 by adding the necessary components in the gaps. [1]
- (ii) On Fig. 7.1 mark with a + the positive output terminal of the rectifier. [1]
- (b) The output voltage V of an a.c. power supply varies sinusoidally with time t as shown in Fig. 7.2.

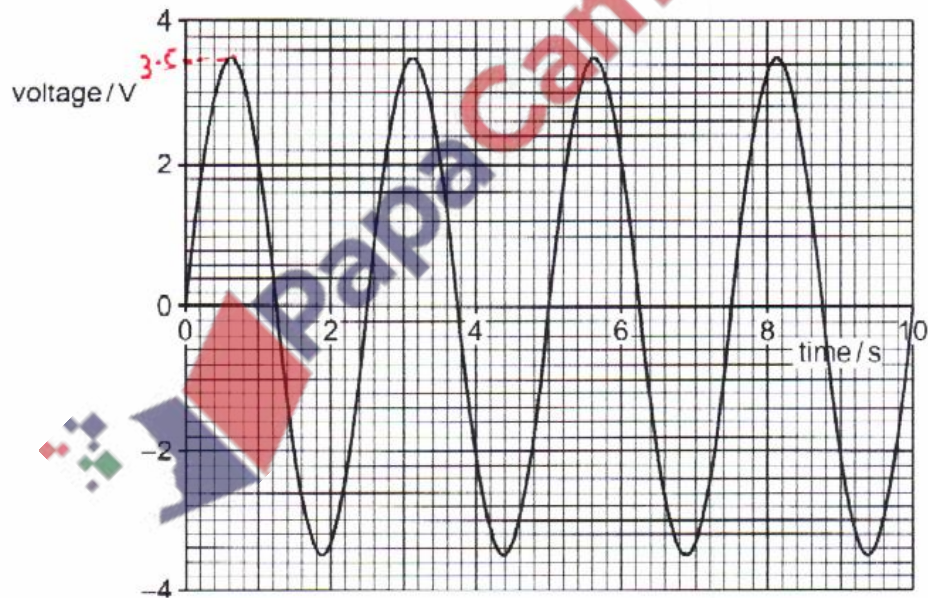


Fig. 7.2

(i) Determine the equation for V in terms of t , where V is in volts and t is in seconds.

$$V = V_0 \sin \omega t$$

$$V_0 = 3.5 \text{ V}$$

$$\omega = \frac{2\pi}{T}$$

$$\therefore V = 3.5 \sin 2.5t$$

$$T = \frac{10}{4} = 2.5 \text{ s}$$

$$V = \underline{3.5 \sin 2.5t} \quad [2]$$

$$\therefore \omega = \frac{2\pi}{2.5} = 2.5 \text{ rad s}^{-1}$$

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