

## CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/42 May/June 2016

Paper 4 (Extended) MARK SCHEME Maximum Mark: 120

Published

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## Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfww	not from wrong working
soi	seen or implied

(	Question	Answer	Mark	Part Marks
1	(a)	Image at (5, 5), (7, 5), (6, 6), (5, 6)	2	If 0 scored SC1 for translation $\begin{pmatrix} 3 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$
	<b>(b)</b>	Image at $(-1, -2)$ , $(-1, -4)$ , $(-2, -3)$ , $(-2, -2)$	2	If 0 scored <b>SC1</b> for reflection in line $y = x$
	(c)	Image at (-2, 5), (-2, 7), (-3, 5), (-3, 6)	3	If 0 scored SC2 for 90° clockwise about (-2, 1) or SC1 for 90° anticlockwise about other centre
	(d) (i)	Enlargement [scale factor] 3 [centre] (2, 4)	B1 B1 B1	If combined transformations, all three marks lost
	(ii)	Stretch [factor] 2 y-axis oe invariant	B1 B1 B1	If combined transformations, all three marks lost
2	(a)	$\frac{630}{9} \times 5$ and $\frac{630}{9} \times 4$ oe	M2	M1 for $630 \div 9$ [=70] or $\frac{5 \times 630 \text{ or } 3150}{9}$ or $\frac{4 \times 630 \text{ or } 2520}{9}$
	(b) (i)	120	3	<b>M2</b> for 98.4[0] ÷ [0].82 oe or <b>M1</b> for recognising 98.4[0] is 82%
	(ii)	69.5 or 69.51	3	M2 for $\frac{98.4[0]-30}{98.4[0]} \times 100$ oe or M1 for $\frac{98.4[0]-30}{98.4[0]}$ oe or $\frac{30}{98.4[0]} \times 100$ If 0 scored, SC1 for answer 75%
	(iii)	211.6[0] cao final answer	1	

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Question	Answer	Mark	Part Marks
(iv)	183	4	<b>B3</b> for answers 182.8 or 182.84 to 182.85 or <b>M2</b> for $150(1.02)^{10}$ seen oe or <b>M1</b> for $150(1.02)^n$ seen oe where $n > 1$
(c)	September or October 2035 nfww	5	<b>B4</b> for 2035 or 19 years and 9 or 10 or 9.96 or 9.961 to 9.962 months nfww or <b>B3</b> for 19.8 or 19.83 seen or <b>M2</b> for $\frac{\log\left(\frac{500}{350}\right)}{\log(1.0015)}$ oe or 350×1.0015 <sup>n</sup> = 500 <b>and</b> at least two valid trials or sketch of appropriate graph or <b>M1</b> for 350×1.0015 <sup>n</sup> [= 500] or $350 \times \left(1 + \frac{0.15}{100}\right)^n$ [= 500] If 0 scored <b>SC2</b> for 24[.0] or 23.95 to 23.98 or 2.55 or 2.552 to 2.554 seen
3 (a) (i)	60	1	
(ii)	8	2	<b>B1</b> for [lq = ] 56 or [uq = ] 64
(iii)	12	2	<b>M1</b> for 188 seen
(b)	68.6 or 68.57	3	M2 for 50 $\times \frac{2.4}{1.75}$ oe or M1 for <i>their</i> distance $\div$ 1.75 or B1 for distance = 120 or for 2.4 and 1.75 or 144 and 105 or 8640 and 6300 seen If 0 scored, SC1 for 77.2 or 77.24
4 (a)	24	3	<b>M2</b> for $6w + 5(w + 30) = 414$ oe or better or <b>B1</b> for $6w$ and $5(w + 30)$ oe
(b)	$2x^2 + 4x - 7 = 0$ oe	B2	i.e. a correct simplified quadratic equation <b>M1</b> for $x^2 + (x+1)(x+3)$ [=10] oe
	Sketch of appropriate graph or correct use of formula or completing square	M1 dep	Dep on a quadratic from addition of two areas. Must see some valid method
	4.48 or 4.49	B2	<b>B1</b> for 4.484 to 4.485 or $6\sqrt{2} - 4$ or 1.12 or 1.121 or $1.5\sqrt{2} - 1$

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Q	Question	Answer	Mark	Part Marks
5	(a)	Any 2 of the following		
		Angle $ADX$ = Angle $BCX$ and same segment oe Angle $DAX$ = Angle $CBX$ and same segment oe Angle $AXD$ = Angle $BXC$ and vertically opp oe	2	<b>B1</b> for one of the three pairs or for at least two pairs of angles without reasons or with incorrect reasons
	(b)	7.5 oe	2	M1 for $\frac{2}{3} = \frac{5}{BX}$ oe
	(c)	67.2 or 67.20 to 67.21 nfww	3	<b>M2</b> for [cos = ] $\frac{2^2 + 5^2 - 4.61^2}{2 \times 2 \times 5}$
				or <b>M1</b> for $4.61^2 = 2^2 + 5^2 - 2 \times 2 \times 5 \cos(AXD)$
6	(a)	Correct sketch		
			2	M1 for shape i.e. starting at origin then one maximum then one minimum A1 for two zeros to right of $x = 10$ and to the left of $x = 20$
	(b)	13.4 or 13.41 to 13.42 19[.0] or 18.97	1 1	
	(c)	(9.49, 1) or (9.486 to 9.487, 1)	B1 B1	
	(d)	(16.4, -1) or (16.43, -1)	B1 B1	
	(e)	$-1 \leq f(x) \leq 1$	1	
	(f)	Correct sketch of parabola shape from	<b>B</b> 1	
		approximately $y = -1$ 5.48 or 5.477	B1	
7	(a) (i)	576 or 575.8 to 576.0	3	<b>M1</b> for $\frac{2}{3}\pi \times 5^3$ (262 or 261.7 to 261.8)
				<b>M1</b> for $\frac{1}{3}\pi \times 5^2 \times 12$ (314 or 314.1 to 314.2 )
	(ii)	0.547 or 0.5470 to 0.5472	2FT	<b>FT</b> <i>their</i> (a)(i) <b>M1</b> for <i>their</i> (a)(i) × 0.95 ÷ 1000
	(iii)	1827 or 1828	2FT	<ul><li>FT with consistent units usual accuracy and truncated</li><li>M1 for 1000 ÷ <i>their</i> (a)(ii)</li></ul>

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Q	Juestion	Answer	Mark	Part Marks
	(iv)	361 or 361.2 to 361.3	4	M1 for $2\pi \times 5^2$ (157 or 157.0 to 157.1) M2 for $\pi \times 5 \times \sqrt{5^2 + 12^2}$ (204 or 204.2) or M1 for $\sqrt{5^2 + 12^2}$ (13)
	(b)	5.37 or 5.369	5	M4 for $\sqrt{\frac{377}{\pi(1+\sqrt{10})}}$ or M3 for $\frac{377}{\pi(1+\sqrt{10})}$ or M2 for $\pi r^2 + \pi r \left(\sqrt{(3r)^2 + r^2}\right) = 377$
				or <b>M1</b> for $r^2 + (3r)^2$ oe
8	(a)	[a, b, c = ] -2, 1, 2	1, 1, 1	In any order
		[d=] 0	1	
	<b>(b)</b>	- 1	1	
	(c)	- 1	1	
	( <b>d</b> )	Parabola vertex downwards and vertex below <i>x</i> -axis	M1	
		Cuts given graph in 5 places	A1	
9	(a)	11	1	
	(b)	$\frac{7}{23}$ oe	1	
	(c)	$\frac{110}{182}$ oe	3	M2 for $\frac{their(a)}{their(a)+3} \times \frac{their(a)-1}{their(a)+2}$ or M1 for a single product of two fractions with first fraction $\frac{their(a)}{their(a)+3}$
	(d)		1	

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Q	uestion	Answer	Mark	Part Marks
10	(a)	31	2	<b>B1</b> for $[f(7) = ]$ 12 or <b>M1</b> for $2(x^2 - x - 30) + 7$
	(b)	$\frac{x-7}{2}$ oe	2	M1 for $y - 7 = 2x$ or $x = 2y + 7$ or $\frac{y}{2} = x + \frac{7}{2}$
	(c)	(2x+13)(2x+1) final answer	3	<b>B2</b> for $(2x+7+6)(2x+7-6)$ or for $4x^2 + 28x + 13$ or <b>M1</b> for $(2x+7)^2 - 36$
	(d)	$\frac{x+5}{x+6}$ final answer nfww	4	<b>B2</b> for $(x - 6)(x + 5)$ or <b>SC1</b> for $(x + a)(x + b)$ where ab = -30 or $a + b = -1and B1 for (x + 6)(x - 6)$
11	<b>(a)</b>	5.4[0] or 5.396	2	M1 for $\tan 34 = \frac{AB}{8}$ oe or better
	(b)	20.4 or 20.38 nfww	5	<b>B1</b> for angle $D = 146$
	(c)	48[.0] or 48.1 or 48.04 to 48.12 cao	2	M2 for $[\sin C = ]$ $\frac{8\sin(theirD)}{19}$ or M1 for $\frac{8}{\sin C} = \frac{19}{\sin(theirD)}$ oe A1 for $[\text{angle } C = ]$ 13.6 or 13.61 to 13.63 OR B1 for angle $A = 56$ M2 for $[\sin C = ]$ $\frac{their AB \times \sin(theirA)}{19}$ or M1 for $\frac{their AB}{\sin C} = \frac{19}{\sin(theirA)}$ oe A1 for $[\text{angle } C = ]$ 13.6 or 13.61 to 13.63 M1 for $0.5 \times their(a) \times 19 \times \sin(90 + their(b))$ oe
12	(a)	$n^3$ cao	1	
	(b) (i)	392	2	<b>B1</b> for second differences 14, 20, 26 and 32
	(ii)	$n^3 + n^2$ oe	2	<b>M1</b> for cubic expression but not $n^3$ or $kn^3$ only