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Cambridge International General Certificate of Secondary Education (9-1)

MATHEMATICS
Paper 4
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MARK SCHEME
Maximum Mark: 84

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MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

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Question	Answer	Marks	Partial Marks
1(a)	4	2	M1 for $\frac{11-3}{2-0}$ oe soi
1(b)	[y =] 4x + 3 oe	1	FT from their gradient
2	35, 70, 75	4	M1 for sum of angles in a triangle = 180 soi or for 3 angles that fit two of the conditions M1 for $2x$ and $x + 40$ oe M1 for $x + 2x + x + 40 = 180$ soi
3	Correct angle bisector with correct arcs shown	2	B1 for angle bisector or correct arcs
4(a)	7	1	
4(b)	3, 7, 31 (with no extras)	2	B1 for two correct (with no extras) or for answer $[n =]2, 3, 5$ only or M1 for 3, 7, 15, 31 seen
4(c)	Valid reason	1	e.g. Because 63 is divisible by 3 or 7 or 9 or 21 e.g. because 63 has more than 2 factors
5(a)	$\frac{2}{5}$, $\frac{4}{7}$, $\frac{3}{7}$, $\frac{4}{7}$, $\frac{3}{7}$ correctly placed	2	B1 for $\frac{2}{5}$ or $\frac{3}{7}$ on a 'does not stop' branch
5(b)	$\frac{6}{35}$ oe	2	M1 for their $\frac{2}{5} \times their \frac{3}{7}$
6(a)	(x+3)(x-6)	2	M1 for $x(x-6) + 3(x-6)$ or $x(x+3) - 6(x+3)$ or for $(x+a)(x+b)$ where $a+b=-3$ or $ab = -18$
6(b)	$x = -3, \ x = 6$	1	FT their factors
7	60	4	M1 for time for A to B = $125 \div 50$ soi M1 for time for B to C = $4 - their$ 2.5 M1 for $90 \div their$ 1.5
8	$x^2 + 7x - 4x - 28$	M1	Must have at least 3 terms correct or $x^2 + 3x - 28$, must have at least 2 terms correct
	$3x^2 - 3x$	B1	
	$x^{2} + 7x - 4x - 28 + 3x^{2} - 3x$ $= 4x^{2} - 28 = 4(x^{2} - 7)$	A1	

Question	Answer	Marks	Partial Marks
9(a)(i)	18	1	
9(a)(ii)	14	2	B1 for 26 or 12 or M1 for attempt at difference of quartiles
9(b)	15	3	B2 for answer 85
			OR
			M1 for $[t < 30] = 102$ or $[t > 30] = 18$ seen M1 for $\frac{120 - their \ 102}{120}$ soi
10(a)	$3k^7$	1	
10(b)	$\frac{5}{2}$ oe	2	M1 for $\frac{2}{5}$ seen or $\left(\frac{25}{4}\right)^{\frac{1}{2}}$
10(c)	$\frac{1}{3}$	1	
11	$12x^3$	4	M1 for $2x \times 2x \times 2x$
			M1 for $\frac{1}{3} \times 2x \times 2x \times (5x - 2x)$
			M1 for their $8x^3$ – their $4x^3$
12	270	3	B2 for $\left(\frac{9}{6}\right)^3$ or $\left(\frac{6}{9}\right)^3$ oe soi
			or B1 for $\frac{9}{6}$ or $\frac{6}{9}$ oe soi
13	$\frac{26}{33}$	3	M2 for $x = \frac{78}{99}$
			or M1 for $x = 0.78$ and $100x = 78.78$ soi
14(a)	5	1	
14(b)	36 700	1	
14(c)	6	1	
15(a)	$ \begin{pmatrix} 12 & 9 \\ 18 & 21 \end{pmatrix} $	1	
15(b)	10	1	
15(c)	$\frac{1}{10} \begin{pmatrix} 7 & -3 \\ -6 & 4 \end{pmatrix} \text{ oe }$	1	FT from their determinant.

Question	Answer	Marks	Partial Marks
16	$(-1\frac{1}{2}, 1\frac{1}{2}), (2, 5)$	5	M1 for $2x^2 - 3 = x + 3$ M1 for $2x^2 - x - 6 = 0$ M1 for $(2x+3)(x-2) = 0$ A1 FT from their factorised quadratic, for $x = -1\frac{1}{2}$ or 2 After A0, SC1 for their x co-ordinates being +3 more than their y co-ordinates
17(a)	Total of flour in grams is $250x + 375y$	M1	
	$250x + 375 \leqslant 6000$ $\rightarrow 2x + 3y \leqslant 48$	A1	
17(b)	$x + y \leqslant 20 \text{ oe}$ $y \geqslant 3 \text{ oe}$	2	B1 for each or SC1 for $x + y * 20$ and $y*3$ where * can be an equals or any inequality sign.
17(c)	Correct region clearly identified	4	B3 for three correct boundaries $2x + 3y = 48$, $x + y = 20$, $y = 3$ or B2 for two correct boundaries or B1 for one correct boundary
17(d)	116	2	M1 for $x = 12$ and $y = 8$ identified or for $5x + 7y$ for integer (x, y) in their region
18	g = 3 $h = -5$	4	B3 for one correct OR M1 for $2x^3 - 2gx^2 + x^2 - gx - 15x + 15g$ or $(x - g)(2x - 5)(x + 3)$ M1 for $2x^3 + hx^2 - 18x - 9h$ or $(x - 3)(x + 3)(2x + h)$
19(a)	2 q – 2 p oe	3	M1 for $\overrightarrow{DA} = -2\mathbf{p}$ or $\overrightarrow{AX} = 2\mathbf{q}$ or $\overrightarrow{BX} = -\mathbf{q}$ M1 for $\overrightarrow{DX} = \overrightarrow{DA} + \overrightarrow{AX}$ oe soi
19(b)	$\overrightarrow{DY} = 3\mathbf{q} - 3\mathbf{p} [= 3(\mathbf{q} - \mathbf{p})]$ or $\overrightarrow{XY} = \mathbf{q} - \mathbf{p}$	M1	
	which is a multiple of \overrightarrow{DX} and X is on DX and on DY oe	A1	

Question	Answer	Marks	Partial Marks
20	243 and 297	3	B2 for one correct or M1 for $180 + 63$ or $360 - 63$ oe or M1 for sketch of sine curve for $0^{\circ} \le x \le 360^{\circ}$ seen
21	$\frac{2}{\sqrt{27}} = \frac{2}{3\sqrt{3}}$	M1	$\frac{2\sqrt{3} + \sqrt{27}}{\sqrt{27} \times \sqrt{3}}$
	$\frac{5}{3\sqrt{3}}$	M1	$\frac{2\sqrt{3} + \sqrt{27}}{\sqrt{81}} \text{ or numerator } 2\sqrt{3} + \sqrt{27} \text{ or better}$
	$\frac{5}{3\sqrt{3}} = \frac{5 \times \sqrt{3}}{3\sqrt{3} \times \sqrt{3}}$	M1	$\frac{2\sqrt{3}+3\sqrt{3}}{9}$
	$\frac{5\sqrt{3}}{9}$	A1	$\frac{5\sqrt{3}}{9}$