

## **Cambridge Assessment International Education**

Cambridge International General Certificate of Secondary Education (9–1)

MATHEMATICS
Paper 4
October/November 2019
MARK SCHEME
Maximum Mark: 84

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2019 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This syllabus is regulated for use in England as a Cambridge International Level 1/Level 2 (9–1) Certificate.



# **Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

## **GENERIC MARKING PRINCIPLE 1:**

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

### **GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always whole marks (not half marks, or other fractions).

#### **GENERIC MARKING PRINCIPLE 3:**

## Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit
  is given for valid answers which go beyond the scope of the syllabus and mark scheme,
  referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these
  features are specifically assessed by the question as indicated by the mark scheme. The
  meaning, however, should be unambiguous.

## **GENERIC MARKING PRINCIPLE 4:**

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## **GENERIC MARKING PRINCIPLE 5:**

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

#### GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

## Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

## **Abbreviations**

awrt answers which round to cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

Question	Answer	Marks	Partial Marks
1	4 11	2	M1 for $\frac{11}{4}$ or for $\frac{1}{2\frac{3}{4}}$ oe or for $\frac{4}{their11}$
2	333	2	M1 for 153 + 180 oe seen or a correct sketch diagram shown
3(a)	4k+4 or $4(k+1)$ final answer	2	M1 for $2k \times 1.6 + 0.8 \times (k+5)$ oe or B1 for $3.2k$ seen or for $0.8k+4$ seen or for answer $4k+c$
3(b)	60	2	<b>M1FT</b> $their(4k+4) = 244$ oe soi
3(c)	65	1	<b>FT</b> <i>their</i> (b) + 5

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Question	Answer	Marks	Partial Marks
4	$5\frac{1}{6}$ or $5\frac{k}{6k}$	3	B1 for $\frac{11k}{18k}$ seen  M1 for $[5]\frac{14k}{18k}$ - their $\frac{11k}{18k}$ oe where denominators are both the same.  If 0 scored SC2 for answer $3\frac{13k}{54k}$ or SC1 for $\frac{175}{36}$ oe seen
5(a)	5.67×10 <sup>-2</sup> cao	1	
5(b)	7.324×10 <sup>14</sup> cao	2	M1 for $7.3 \times 10^{14} + 0.024 \times 10^{14}$ or $730 \times 10^{12} + 2.4 \times 10^{12}$ or answer figs $7324$
6	Correct enlargement drawn	2	<b>B1</b> for enlargement correct size and orientation but in the wrong position or for 4 or 5 vertices plotted correctly
7	Two different accurately constructed triangles	4	<b>B3</b> for one triangle <i>DEF</i> accurately drawn or <b>B2</b> for a triangle satisfying two conditions or <b>B1</b> for a triangle satisfying one condition or for an incomplete triangle satisfying two conditions.
8	4,5,5,5,11 or 3,5,5,7,10	3	B1 for five numbers with mode = 5 and median = 5 B1 for five numbers that total 30 B1 for five numbers with range = 7 Maximum 2 marks if answer not correct.
9(a)	-6x	2	M1 for $x^2 - 3x$ or $-x^2 - 3x$ or $x(x-3-(x+3))$
9(b)	$x^{10}$	1	
9(c)	$x^{18}$	1	
10(a)	[0].375	2	M1 for attempt at $3 \div 8$ or for [0].125 seen
10(b)	13 90	2	M1 for $10x - x = 1.4444 0.1444$ or better or $\frac{1}{10} + \frac{4}{90}$
11(a)	(2x-y)(2x+y)	2	M1 for $(ax + by)(cx + dy)$ where $ac = 4$ and $bd = -1$

Question	Answer	Marks	Partial Marks
11(b)	372 000 from use of correct factorisation	2	M1 for $(their\ a \times 343 - their\ b \times 314)$ $\times (their\ c \times 343 + their\ d \times 314)$
12(a)	0.8 oe	1	
12(b)	$\frac{1}{4}$ oe	2	<b>B1</b> for $(64)^{-\frac{1}{3}}$ or $2^{-2}$ or $\frac{1}{8^{\frac{2}{3}}}$ or better
13	С	1	
14(a)	100π final answer	2	<b>M1</b> for $\pi \times 5 \times 5[\times 4]$ oe
14(b)	2700π final answer	3	<b>B2</b> for volume factor = 27 or <b>M2</b> for $(\sqrt{9})^3 \times their 100\pi$ or <b>M1</b> for length scale factor is $\sqrt{9}$ soi
15(a)	$2+\sqrt{3}$	2	<b>M1</b> for $\frac{6}{4+2\sqrt{3}} = \frac{3}{v}$ oe
15(b)	$48-24\sqrt{3}$	4	M1 for $\frac{6}{4+2\sqrt{3}} \times 8$ or $\frac{3}{theirv} \times 8$ M1 for $\frac{k}{4+2\sqrt{3}} \times \frac{4-2\sqrt{3}}{4-2\sqrt{3}}$ or $\frac{k}{theirv} \times \frac{their(a-b\sqrt{3})}{their(a-b\sqrt{3})}$ M1 for $\frac{k(4-2\sqrt{3})}{16-4\times 3}$ or $\frac{k(their(a-b\sqrt{3}))}{their(a^2-3b^2)}$
16	$x^3 + 2x^2 - 16x - 32$	3	B1 for expanding and simplifying two sets of brackets correctly M1 for expanding <i>their</i> quadratic and final factor
17	$4\sqrt{6}$	5	<b>B1</b> for angle $EGF = 45$ <b>B1</b> for $\sin 60 = \frac{\sqrt{3}}{2}$ or $\sin 45 = \frac{1}{\sqrt{2}}$ oe <b>M2</b> for $FG = \frac{8 \times \sin 60}{\sin 45}$ or <b>M1</b> for $\frac{\sin 45}{8} = \frac{\sin 60}{FG}$

Question	Answer	Marks	Partial Marks
18	121	3	<b>M2</b> for $10\sqrt{y} = 22\sqrt{25}$ oe or for $w = \frac{110}{\sqrt{y}}$ or <b>M1</b> for $w = \frac{k}{\sqrt{y}}$ or $22\sqrt{25}$ or $k=110$
19	135, 315	2	<b>B1</b> for each or for a sketch of $y = \tan x$
20(a)	$a(ax+b)+b$ $= a^2x + ab + b$	1	
20(b)(i)	b=0 nfww	1	
20(b)(ii)	b can take any value oe	1	
21	$x = \sqrt[3]{\frac{7w^2y + 4}{5}}$ oe final answer	4	<ul> <li>M1 for squaring both sides</li> <li>M1 for eliminating fraction</li> <li>M1 for isolating x³</li> <li>M1 for cube rooting both sides</li> <li>Maximum of 3 marks if answer incorrect</li> </ul>
22(a)	Reflection $y = -x$ oe	2	B1 for each
22(b)	centre of enlargement is $(0,1)$ or is not $(0,0)$ oe scale factor from $C$ to $D$ is $\frac{1}{2}$ or is not 2 oe	2	B1 for each
22(c)	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	2	<b>B1</b> for a matrix satisfying $\mathbf{A} = \mathbf{A}^{-1}$ or for a rotation matrix or for a complete description: rotation 180 about origin
23(a)	$\frac{w}{n} \times \frac{w}{n}$ oe	1	
23(b)	$\frac{w}{n} \times \frac{w-1}{n-1}$ oe	1	
23(c)	For their $p_1 = \frac{21}{20}$ their $p_2$ Elimination of denominator or use of common denominator Correct completion to $n = \frac{20w}{21-w}$	M1 M1	
23(d)	20, 400	2	B1 for each