

Ay Cambridge IGCSE™

MATHEMATICS (US)

Paper 4 (Extended)

MARK SCHEME

Maximum Mark: 130

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Ma	Maths-Specific Marking Principles				
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.				
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.				
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.				
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).				
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.				
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.				

Abbreviations

cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

nfww not from wrong working

soi seen or implied

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Question	Answer	Marks	Partial Marks
1(a)	Triangle drawn at $(1, -5)$, $(1, -7)$, $(5, -5)$	2	B1 for reflection in any horizontal line If 0 scored, SC1 for reflection in $x = -2$
1(b)	Triangle drawn at $(-2, 0)$, $(-2, -1)$, $(0, -1)$	2	B1 for correct size and orientation but wrong position
1(c)	Rotation	3	B1 for each
	90 [anticlockwise] oe		
	[centre] (-1, 0)		
2(a)(i)	60.9 or 60.86 to 60.87	1	
2(a)(ii)	375	2	M1 for $\frac{250}{12}$ [× 18] oe
2(a)(iii)	30 nfww	3	M1 for figs2200 ÷ 800 [× 12]oe M1 for 1500 ÷ 600 [× 12] oe
2(b)(i)	1.92	2	M1 for $k \times \left(1 + \frac{25}{100}\right) = 2.4[0]$ oe or
- 4 \ 44			better
2(b)(ii)	43.75 or $43\frac{3}{4}$	3	M2 for $ \left(\left(1 + \frac{25}{100} \right) \times \left(1 + \frac{15}{100} \right) [-1] \right) [\times 100] \text{ oe} $ or $ \left(1 + \frac{25}{100} \right) \times \left(1 + \frac{15}{100} \right) \times 100 [-100] $ or for $ \frac{2.40 \times \left(1 + \frac{15}{100} \right)}{their(\mathbf{b})(\mathbf{i})} \times 100 [-100] $ oe or M1 for $ 2.40 \times \left(1 + \frac{15}{100} \right) \text{ or} $ $ \left(1 + \frac{25}{100} \right) \times \left(1 + \frac{15}{100} \right) \text{ oe} $
2(c)	15	2	M1 for $\frac{59}{50} \times 250$ oe (implied by 295)
3(a)(i)	p^{14} final answer	1	
3(a)(ii)	$6m^4$ final answer	2	B1 for $6m^k$ or km^4 in final answer or correct answer seen and spoilt

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Question	Answer	Marks	Partial Marks
3(a)(iii)	$\frac{4}{3x^3y^9} \text{ or } \frac{4x^{-3}y^{-9}}{3} \text{ final answer}$	3	B2 for correct answer seen and spoilt or 2 correct elements in final answer or B1 for one of $\frac{4}{3}$ or $\frac{3}{4}$ oe or x^3 or y^9 seen
3(b)	3, 12, 27	2	B1 for 12 or 27
3(c)(i)	3n + 10 oe final answer	2	B1 for $3n + k$ oe or $jn + 10$ oe $(j \neq 0)$ or for correct expression shown in working and then spoilt
3(c)(ii)	$2n^3 + 1$ oe final answer	2	B1 for 3rd diff = 12 (both needed) or for cubic answer or for correct expression shown in working and then spoilt
3(d)	38	3	M2 for $3x = 4 \times 23 + 22$ or M1 for $3x - 22 = 4 \times 23$ or for $\frac{3x}{4} = 23 + \frac{22}{4}$ oe
3(e)	$\frac{-8 \pm \sqrt{8^2 - 4(3)(-20)}}{2 \times 3}$ or $\frac{-8}{2 \times 3} \pm \sqrt{\frac{8^2}{4 \times 3^2} - \frac{(-20)}{3}}$ or better	B2	B1 for $\sqrt{8^2 - 4(3)(-20)}$ oe or $\frac{-8 + \sqrt{q}}{2 \times 3}$ oe or $\frac{-8 - \sqrt{q}}{2 \times 3}$ oe or both
	- 4.24, 1.57 final answers	B2	B1 for each If B0, SC1 for answers – 4.2 or –4.23 or –4.240 to – 4.239 and 1.6 or 1.572 to 1.573 or – 4.24 and 1.57 seen in working or for –1.57 and 4.24 as final answer
4(a)	$\left(\frac{(36+50)\times40}{2}\right)\times120 \text{ oe}$ or $\left(\frac{(0.36+0.5)\times0.4}{2}\right)\times1.2 \text{ oe}$	M2	M1 for $\frac{(36+50)\times 40}{2}$ oe or $\frac{(0.36+0.5)\times 0.4}{2}$ oe
	$206400 \div 1000 = 206.4$ or $0.2064 \times 1000 = 206.4$ nfww	A1	Must see an explicit conversion
4(b)	5 [minutes] 44 seconds	3	B2 for 344 [seconds] oe 5.73[mins] or M1 for figs206.4 ÷ figs 6 oe

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Question	Answer	Marks	Partial Marks
4(c)(i)	28[.0] or 27.96 to 27.97	3	M2 for $[r^2=]$ $\frac{\text{figs } 2064}{(figs 84)\pi}$
			or M1 for $\pi r^2 \times figs84 = \text{figs } 2064$
4(c)(ii)	140 cao	2	M1 for $0.6h = 84$ oe
			ALT method M1 for $\pi \times (their (\mathbf{c})(\mathbf{i}))^2 \times h = figs 206400 \div 0.66$ oe
4(d)	38.6 or 38.58	4	B3 for 14.1 or 14.08 or M2 for $11.1^2 + 9.5^2 - 3.9^2$ oe or M1 for $11.1^2 + 9.5^2$ or $\left(their AC\right)^2 - 3.9^2$
5(a)(i)	38	2	M1 for $5 \times 3^2 - 7$ oe
5(a)(ii)	$[\pm]\sqrt{\frac{P+7}{5}}$ oe final answer	3	M1 for $P + 7 = 5k^2$ or $\frac{P}{5} = k^2 - \frac{7}{5}$ M1 for $k^2 = \dots$ FT <i>their</i> first step M1 for square root to final answer Max M2 for incorrect answer
5(b)(i)	$x \ge -2.5$ final answer	2	M1 for $-4x \le 7 + 3$ or better
5(b)(ii)	-6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6	1	FT their inequality in (b)(i)
5(c)(i)	x = 2 broken line	B1	
	y = 32 - x solid line	B1	
	2x + 3y = 72 solid line	B2	B1 for line passing through (0, 24) or (36, 0)
	Correct region indicated cao	В2	B1 for region satisfying 3 of the inequalities
5(c)(ii)	(16, 16)	2	M1 for substitution into $2x + y$ for any integer point in <i>their</i> region

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Question	Answer	Marks	Partial Marks
6(a)(i)	$\frac{1}{15}$ oe	3	M2 for $2 \times \frac{1}{6} \times \frac{1}{5}$ oe or M1 for $\frac{1}{6} \times \frac{1}{5}$ oe or list or indication of 2 correct pairs If 0 scored, SC1 for answer $\frac{1}{18}$ oe
6(a)(ii)	7/15 oe	3	M2 for $\left(\frac{4}{6} \times \frac{3}{5}\right) + 2\left(\frac{1}{6} \times \frac{1}{5}\right)$ oe or 14 $\left(\frac{1}{6} \times \frac{1}{5}\right)$ oe or $1 - 2\left(\frac{2}{6} \times \frac{4}{5}\right)$ or M1 for $\left(\frac{4}{6} \times \frac{3}{5}\right)$ or $2\left(\frac{1}{6} \times \frac{1}{5}\right)$ oe or $2\left(\frac{2}{6} \times \frac{4}{5}\right)$ or correct identification of 14 pairs If 0 scored, SC1 for answer $\frac{5}{9}$
6(b)	1/10 oe nfww	4	M3 for $6\left(\frac{1}{6} \times \frac{1}{5} \times \frac{1}{4}\right) + 6\left(\frac{1}{6} \times \frac{1}{5} \times \frac{1}{4}\right)$ oe or M2 for $6\left(\frac{1}{6} \times \frac{1}{5} \times \frac{1}{4}\right)$ oe or $2\left(\frac{1}{6} \times \frac{1}{5} \times \frac{1}{4}\right)$ oe or M1 for $k\left(\frac{1}{6} \times \frac{1}{5} \times \frac{1}{4}\right)$ where k is an integer and $1 \le k \le 12$ but not $k = 2$ or $k = 6$ or identifies -2 , 2 and 5 or -3 , 3 and 5 as the 3 cards needed If 0 scored, SC1 for answer $\frac{1}{18}$
7(a)	Correct histogram	3	B1 for each correct block If 0 scored, SC1 for two of $\frac{28}{15}$, $\frac{33}{20}$, $\frac{13}{10}$ or 1.87 or 1.866 to 1.867, 1.65, 1.3

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Question	Answer	Marks	Partial Marks
7(b)	38.65	4	M1 for 12.5, 20, 32.5, 50, 65 soi
			M1 for $\sum fx$ where x is in the correct interval including boundaries
			M1dep for $\sum fx \div 100$
8(a)	[cos $B = $] $\frac{9.5^2 + 7.7^2 - 10^2}{2 \times 9.5 \times 7.7}$ oe	M2	M1 for $10^2 = 9.5^2 + 7.7^2 - 2 \times 9.5 \times 7.7 \cos B$ oe or better
	70.206 to 70.207 or 70.21 to 70.22	A2	A1 for $\frac{2477}{7315}$ oe or 0.339 or 0.3386
8(b)(i)	140.4	1	
8(b)(ii)	19.8	1	FT (180 − <i>their</i> (b)(i)) ÷ 2
8(b)(iii)	70.2	1	FT 90 – <i>their</i> (b)(ii)
8(c)	5.31 or 5.314 to 5.315	3	M2 for $\frac{5}{\cos their(\mathbf{b})(\mathbf{ii})}$ oe
			or M1 for $\frac{5}{r} = \cos(their(\mathbf{b})(\mathbf{ii}))$ oe
8(d)	38.8 or 38.78 to 38.85	4	M3 for $\frac{0.5 \times 9.5 \times 7.7 \times \sin 70.2}{\pi \times (their (\mathbf{c}))^2} [\times 100]$
			OR M1 for $0.5 \times 9.5 \times 7.7 \times \sin 70.2$
			M1 for $\pi \times (their(\mathbf{c}))^2$
9(a)(i)	2a drawn correctly with direction arrow	1	
9(a)(ii)	a − b drawn correctly with direction arrow	2	B1 for $\begin{pmatrix} 4 \\ -3 \end{pmatrix}$ seen or implied
			or M1 for correctly drawing <i>their</i> $\mathbf{a} - \mathbf{b}$ with an arrow
9(b)(i)(a)	$\mathbf{q} + \frac{3}{4} \mathbf{p}$ final answer	1	
9(b)(i)(b)	$\mathbf{q} - \frac{1}{4} \mathbf{p}$ final answer	2	M1 for a correct route

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Question	Answer	Marks	Partial Marks
9(b)(i)(c)	$\frac{13}{24} \mathbf{p} - \frac{2}{3} \mathbf{q}$ final answer	3	M2 for $\frac{3}{8}\mathbf{p} - \frac{2}{3}$ (their (b)(i)(b)) oe or for $-\frac{3}{8}\mathbf{p} - \mathbf{q} + \mathbf{p} + \frac{1}{3}$ (their (b)(i)(b)) oe or M1 for a correct route or for $[\overrightarrow{BN} =] -\frac{2}{3}$ (their (b)(i)(b)) or $[\overrightarrow{AN} =] \frac{1}{3}$ (their (b)(i)(b)) or final answer $k\mathbf{p} - \frac{2}{3}\mathbf{q}$ oe or $\frac{13}{24}\mathbf{p} - k\mathbf{q}$ oe
9(b)(ii)	$\frac{19}{16}$ p oe final answer	2	M1 for $\overrightarrow{AG} = \frac{3}{8}\mathbf{p} \div 2$ soi or for answer $k\mathbf{p}$ oe
10(a)	17 1.4 oe 0.4 oe	3	B1 for each
10(b)(i)	170	1	
10(b)(ii)	8.5	2	M1 for $50 + 30x = 305$ or better
10(b(iii)	1.5	2	M1 for $50 + 30x = 20 + 50x$ or better
10(c)	[a =] 5 [b =] 6	2	B1 for each
10(d)(i)	11.5 or 11.53 to 11.54 168.5 or 168.46	2	B1 for each If 0 scored, SC1 for two angles that add to give 180.0
10(d)(ii)	90 – <i>x</i> oe	1	
10(e)	119	2	M1 for $x = g(3)$ or better
10(f)	Stretch [factor =] 3 x-axis oe invariant	3	B1 B1 B1

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