

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

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CAMBRIDGE IGCSE MATHEMATICS (US)

0444/04

Paper 4 (Extended)

For examination from 2012

SPECIMEN SCORING GUIDE

MAXIMUM SCORE: 130

Types of score

M scores are given for a correct method.

A scores are given for an accurate answer following a correct method.

B scores are given for a correct statement or step.

D scores are given for a clear and appropriately accurate drawing.

P scores are given for accurate plotting of points.

E scores are given for correctly explaining or establishing a given result.

SC scores are given for special cases that are worthy of some credit.

Abbreviations

anything rounding to art correct answer only cao correct solution only cso ft follow through

ignore subsequent working isw

or equivalent oe seen or implied soi without working ww

without wrong working www

1 (a)	350, 250, 200	В3	M1 for $800 \div (7+5+4)$ Implied by 50 and M1 dep their $50 \times$ any one of 7, 5, or 4
(b)	275 cao	В3	B1 for 100 or 250 (may be implied in next step) their $250 \times 5 \times 2$
(c)	200	B2 ft	and M1 for ${200}$ seen ft $0.8 \times$ their 250 from (a) oe correctly evaluated
(d)	11:8:4 or 2.75:2:1 cao	B2	M1 for 0.8 × their 250 from (a) M1 for 275 or their (b): 200 or their (c): 100 [10]

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			3	M1 for $\frac{60+40}{35}$ (2.857) could be in parameter and M1 for correct method to convert a
2	(a)	14 46 or 2 46 pm cao	В3	M1 for $\frac{60+40}{35}$ (2.857) could be in pa
				and M1 for correct method to convert a decimal time to minutes ft a decimal either full answer or decimal part × 60 (e.g., 51.(428), 171.(4) or 2hrs 51 or 51 m)
	(b) (i)	260	B1	
	(ii)	145	B1 ft	ft their (b)(i) – 115
	(c)	85(.0) cao www	B4	M2 for $(AC^2 =) 40^2 + 60^2 - 2 \times 40 \times 60 \times \cos 115$ or M1 for correct implicit version and M1 dep $(AC =) $ of a correct combination
	(d)	39.76 to 39.8 cao www	В3	M2 for $(\sin A =) \frac{\sin 115}{\text{their } (\mathbf{c})} \times 60$ or M1 for $\frac{\sin A}{60} = \frac{\sin 115}{\text{their } (\mathbf{c})}$ Could use cosine rule as alt method
	(e)	73.76 – 73.81 cao	В3	M2 for $40 \sin 80 + 60 \sin 35$ oe (39.4) $(34.4)or their (c) × \sin(100 - \text{their (d)})or their (c) × \cos(\text{their (d)} - 10)or M1 for either 40 \sin 80 or 60 \sin 35or implicit trig version using their (c)$
				[15]

		4	$\frac{4 \pm \sqrt{(-4)^2 - 4.1.3}}{2} \text{ or } (x-2)^2 = 1 or beth high$
3 (a)	(x-3)(x-1) = 0	M1	$\frac{4 \pm \sqrt{(-4)^2 - 4.1.3}}{2} \text{ or } (x - 2)^2 = 1 \text{ or beta}$
	1 and 3 www B2	A1	
(b)	Correct first step of rearrangement	M1	e.g., $y + 1 = 2x$ or $x + 1 = 2y$ or better
	$\frac{x+1}{2}$ oe	A1	
(c)	$x^2 - 6x + 4 = 0$	M1	Can be implied by later work (method marks)
	$\frac{p \pm \sqrt{q}}{r} \text{ with } p = 6 \text{ and } r = 2$	B1 ft	ft if in the form $ax^2 + bx + c$ (= 0) with $a \neq 0$
	and $q = (-6)^2 - 4.1.4$ oe or 20	B1 ft	$[(x-3)^2 - 5 = 0 \mathbf{B1} \text{ then } x = (\pm)\sqrt{5} + 3 \mathbf{B1}$ is the equivalent for completing the square]
	5.24 cao 0.76 cao www	B1 B1	SC1 for both answers "correct" but not to 2 dp (5.236 067 977, 0.763 932 022) Can be truncated or correctly rounded
(d)	29	B2	SC1 for $[f(-2) =] 15$ seen or $2x^2 - 8x + 5$ oe seen
(e)	$(2x-1)^2 - 4(2x-1) + 3$	M1	
	$4x^2 - 12x + 8 \text{ final answer}$	A2	Or correctly factorized After A0 , SC1 for $4x^2 - 12x + 8$ seen [14]
4 (a) (i)	153.86 to 153.96 or 154	B2	M1 for $4 \pi 3.5^2$
(ii)	179.5 to 179.62 or 180	B2	M1 for $\frac{4}{3}\pi 3.5^3$
(iii)	1005 to 1006 or 1008 or 1010 (g)	B2 ft	ft their (ii) × 5.6 correct to 3sf or better (allow in kg) M1 for their (ii) × 5.6
(b)	9.78 to 9.79	B4	M1 for $\pi 8^2 \times 8$ (1608 – 1609) Alt $\pi 8^2 d = 2 \times \text{their}$ (ii) M1
			and M1 dep for $\pi 8^2 h = 2 \times \text{their } (\mathbf{ii}) + \pi 8^2 \times 8$ Alt $(2 \times \text{their } (\mathbf{a})(\mathbf{ii})) \div (\pi 8^2)$ M1 dep
			and M1 dep $(2 \times \text{their } (\mathbf{ii}) + \pi 8^2 \times 8) \div (\pi 8^2)$ Alt add 8 M1 dep [10]

		6.1(1.1) 7.11.0(11.00)	D4 D4 D4	78.
5	(a)	-6.1(11), 5, 11.9 (11.88)	B1 B1 B1	PO 6: C 12: 15 16
	(b)	16 correct points	Р3	P2 ft for 13 to 15 correct (in correct square) P1 ft for 10 to 12 correct
		Smooth curves through 14 points Ignoring $x = \pm 0.3$	D1	Correct shape, not ruled, within $\frac{1}{2}$ small square (curves could be joined)
		Graph does not cross the y-axis	B1	Indep but needs 2 "curves"
	(c) (i)	$0.45 \leqslant x \leqslant 0.5$	B1	
	(ii)	$-2.4 \leqslant x \leqslant -2.1$	B1	
		$-0.5 \leqslant x \leqslant -0.4$	B1	
		$0.3 \leqslant x \leqslant 0.4$	B1	If 0 scored, SC1 for evidence of $f(x) = -4$
	(d)	g(x) = 3x + 3 correct, ruled, full range (1mm accuracy at ends)	B2	Allow SC1 for any one of correct but short, slope of 3, <i>y</i> -intercept 3 on sloping line, "good" freehand
	(e) (i)	Gets closer	B1	Any correct comment isw dep on $g(x)$ correct or freehand
	(ii)	Answer rounds to 3.00	B1	[16]
6	(a)	108(.16) (allow 108.2(0)) www	B2	M1 for 100×1.04^2 oe
	(b)	148(.02), 324(.3)	B1 B1	
	(c)	5 correct pts 100, 148 ft, 219, 324 ft, 480	Р3	P2 ft for 4 correct, P1 ft for 3 correct Points must be in correct square vertically, including on line
		Smooth exponential curve, correct shape, through 5 points	D1	including on fine
	(d) (i)	265 – 270	B1	If out of range, then ft their graph at 25 years
	(ii)	17 or 18 cao	B1	
	(e) (i)	$\frac{(100) \times 7 \times 20}{(100)}$ oe	M1	
		$100 + 7 \times 20$ or better	E1	No errors
	(ii)	380	B1	
	(iii)	Correct straight ruled line for <i>x</i> -range 0 to 35	D2	P1 ft for 2 of (0, 100), (20, 240), (40, 380) ft correctly plotted
	(f)	27 – 29 cao	B1	[16]

1 B1

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7 (a) (i)	36 (36.0 – 36.4)	B1	Drig
(ii)	50 (50.0 – 50.4)	B1	3
(iii)	29 (28.6 – 29.4)	B1	
(iv)	20	B2	If B0 , SC1 for 19 or 21 or 180 seen
(b) (i)	p = 16, q = 4	B1 B1	If B0 , SC1 if p and q add up to 20
(ii)	36.1 cso www	B4	Answer 36 scores 4 marks after some correct working shown with no incorrect working seen M1 for using mid-values at least four correct from 5, 15, 25, 35, 45, 55, 65, 75 M1 (dep on x values within the correct class
			including the boundaries) for Σfx (at least four correct products soi) M1 (dependent on 2nd M1) for dividing sum by 200 or 180 + their p + their q
(c)	8.2 (8.19 – 8.20), 11.4, 5 (5.00 – 5.01)	B4	B3 for 2 correct or B2 for 1 correct After B0 , SC2 for fd's 2.7(3) oe, 3.8 oe, 1.6(6) oe or SC1 for 2 of fd's correct [15]

		7	Dep on B1 Accept Z angle, extras can spo
8 (a) (i)	x = 78	B1	Orio
	alternate angles	E1	Dep on B1 Accept Z <u>angle</u> , extras can spe Accept longer reasons using correct language and clarity with angles used, e.g., allied angles gives 102° and angles on a straight line = 180°
	either $y = 144$ or $z = 102$	B 1	
	(opposite angles of) cyclic quad (= 180)	E1	Dep on B1 , extras can spoil
	and $z = 102$ or $y = 144$	B1	D 11
	angles (in (a)) quadrilateral (= 360) or (opp angles of) cyclic quad (= 180)	E1	Dep on B1 , extras can spoil
(ii)	Their $z + 36 \neq 180$ oe	E1	Could also use their angles x and y provided $x + y \ne 180$ Could be a longer reason involving angles, must be clearly explained.
(iii)	72 or 288	B1	
(b) (i)	Similar (or enlargement)	B1	
(ii)	9.8 (9.79 to 9.81) www	B2	M1 for $\left(\frac{7}{10}\right)^2$ or $\left(\frac{10}{7}\right)^2$ oe seen (0.49), (2.04) It is possible to do (iii) then (ii) and full marks can still be scored
(iii)	4 www	B2	M1 for $\frac{1}{2} \times 10 \times \text{height} = 20$ [13]

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9 (a)	Sketch of 4 by 4 diagram	B1	Drie
(b) (i)	25, 40	B1 B1	
(ii)		B1	
	$(n+1)^2$ oe	B1	
	$(n+1)^2$ oe $(n+1)^2 + n^2 - 1$ or $2n^2 + 2n$ or 2n(n+1) oe	B2	Any one of these oe isw and if B0 allow SC1 for their $(n+1)^2$ + their (n^2) – 1 or an expression containing $2n^2$ as the highest order term, soi
(c) (i)	$\frac{2}{3} + f + g = 4$	B1	
(ii)	$\frac{2}{3} \times 2^3 + f \times 2^2 + g \times 2$ oe	M1	ie for substituting 2
	$4f + 2g = \frac{32}{3}$	E 1	No errors
(iii)	$\frac{2}{3} + f + g = 4$ $\frac{2}{3} \times 2^{3} + f \times 2^{2} + g \times 2 \text{ oe}$ $4f + 2g = \frac{32}{3}$ $2f + 2g = \frac{20}{3}, 4f + 2g = \frac{32}{3}$ $(f =) 2, (g =) \frac{4}{3} \text{ oe cao www } \mathbf{B3}$	M1	for correctly setting up for elimination of one variable
	$(f =) 2, (g =) \frac{4}{3}$ oe cao www B3	A1 A1	Accept $\frac{6}{3}$ for 2
(iv)	880 cao	B1	[14]
10 (a)	$s = \frac{1}{3}, t = \frac{1}{4}, u = \frac{5}{6}$	B1 B1 B1	All correctly placed on tree or clearly indicated
(b)	$\frac{2}{3} \times \frac{3}{4}$	M1	Accept all probabilities as frac/dec/% -1 once for words or 2 sf, do not accept ratios isw cancelling after correct answer
	$\frac{1}{2}$ oe cao	A1	is weathering after correct answer
(c)	$\frac{2}{3} \times \text{their } \frac{1}{4} + \text{their } \frac{1}{3} \times \text{their } \frac{5}{6}$ $\frac{4}{9} \text{ oe cao } (0.444)$	M1	Follow through method provided $0 < P < 1$
	$\frac{4}{9}$ oe cao (0.444)	A1	[7]