

## **Cambridge Assessment International Education**

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

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# **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/43

Paper 4 (Extended)

May/June 2019

2 hours 15 minutes

Candidates answer on the Question Paper.

Additional Materials: Geometrical Instruments

**Graphics Calculator** 

#### **READ THESE INSTRUCTIONS FIRST**

Write your centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

Do not use staples, paper clips, glue or correction fluid.

You may use an HB pencil for any diagrams or graphs.

DO NOT WRITE IN ANY BARCODES.

Answer all the questions.

 $Unless \ instructed \ otherwise, give \ your \ answers \ exactly \ or \ correct \ to \ three \ significant \ figures \ as \ appropriate.$ 

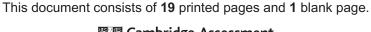
Answers in degrees should be given to one decimal place.

For  $\pi$ , use your calculator value.

You must show all the relevant working to gain full marks and you will be given marks for correct methods, including sketches, even if your answer is incorrect.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 120.





## Formula List

For the equation

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Curved surface area, A, of cylinder of radius r, height h.

$$A = 2\pi rh$$

Curved surface area, A, of cone of radius r, sloping edge l.

$$A = \pi r l$$

Curved surface area, A, of sphere of radius r.

$$A = 4\pi r^2$$

Volume, V, of pyramid, base area A, height h.

$$V = \frac{1}{3}Ah$$

Volume, V, of cylinder of radius r, height h.

$$V = \pi r^2 h$$

Volume, V, of cone of radius r, height h.

$$V = \frac{1}{3}\pi r^2 h$$

Volume, V, of sphere of radius r.

$$V = \frac{4}{3}\pi r^3$$

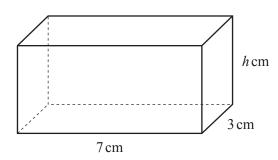
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$Area = \frac{1}{2}bc \sin A$$

# Answer all the questions.

1 (a)



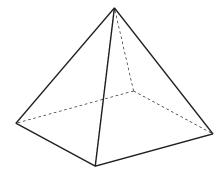
NOT TO SCALE

The diagram shows a cuboid. The volume of this cuboid is 52.5 cm<sup>3</sup>.

Find the value of *h*.

 [2

**(b)** 



NOT TO SCALE

The diagram shows a pyramid. The area of the base is  $500 \, \text{m}^2$ . The height of the pyramid is  $27 \, \text{m}$ .

Find the volume of this pyramid.

 $m^3$	[2]
 	L-1

2 The table shows the marks of 10 students in a physics examination and a chemistry examination.

Physics mark (x)	17	29	34	46	57	66	73	84	92	96
Chemistry mark (y)	26	42	41	56	52	61	76	65	73	80

(a)	Fino	1	
	(i)	the mean physics mark,	
		[	1
	(ii)	the mean chemistry mark.	
		[	1
(b)	Fino	If the equation of the regression line for $y$ in terms of $x$ .	
		y =  [2	2
(c)	Use	your regression line to estimate the chemistry mark when	
	(i)	the physics mark is 60,	
		[	1
	(ii)	the physics mark is 5.	
		[	1
(d)		ich physics mark, 60 or 5, is likely to give the most reliable chemistry mark? e a reason for your answer.	
		[	1

**3** There are 120 students at a school.

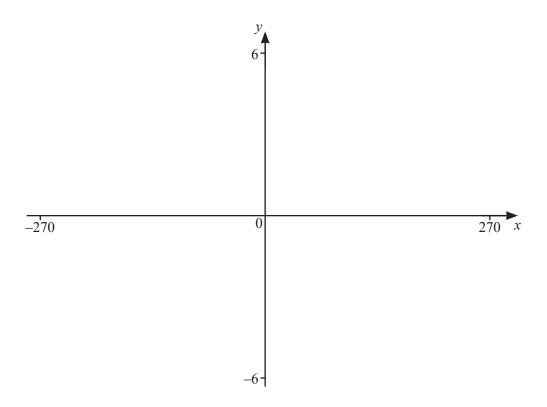
There are 30 students in each class.

The number of boys and the number of girls in each class is shown in the table.

	Class 1	Class 2	Class 3	Class 4
Boys	16	19	12	13
Girls	14	11	18	17

		Oll is	17	11	10	1 /
(a)	A stu	dent is chosen	at random from	the 120 students.		
	Calcu	ılate the proba	bility that the stu	dent chosen is		
	(i)	a boy from Cla	ass 2,			
	(**)					
	(ii)	not from Clas	s 3.			
(b)	A boy	y is chosen at i	random.			
	Calcu	ılate the proba	bility that he is fr	om Class 4.		
(c)	Three	e students fron	n Class 1 are chos	sen at random.		
	Color	ılate the proba				

.....[3]



(a) On the diagram, sketch the graph of y = f(x) where

$$f(x) = \frac{1}{\cos x}$$
 for values of x between -270 and 270.

**(b)** Write down the range of f(x).

		[2]
		121

(c) (i) On the same diagram, sketch the graph of y = g(x) where

$$g(x) = \frac{(720 + x)}{2x}$$
 for values of x between -270 and 270. [2]

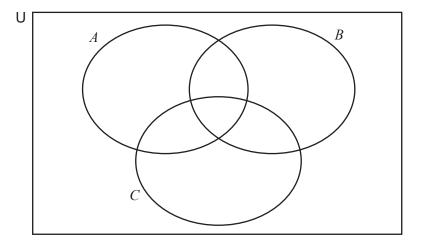
(ii) Find the values of the x co-ordinates of the points of intersection of the two graphs.

$$x = \dots$$
 or  $x = \dots$  [3]

(iii) Find the equation of each asymptote of the graph of y = g(x).



5 The Venn diagram shows the sets A, B and C.



 $U = \{2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13\}$ 

 $A = \{ prime numbers \}$ 

 $B = \{\text{factors of } 12\}$ 

 $C = \{\text{multiples of 3}\}\$ 

(a) List the elements of set A.

			•	•			•	•	•					•	•			•	•	•			•	•	•				•	•	•	•	•			•		•			1	]	

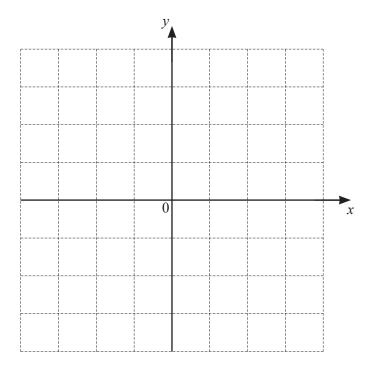
- **(b)** Write all the elements of U in the correct parts of the Venn diagram above. [3]
- (c) List the elements of  $(A \cup B)'$ .

.....[1]

(d) Find  $n((B \cup C) \cap A')$ .

.....[1]

6 You may use this grid to help you answer this question.



The transformation P is a reflection in the line y = x.

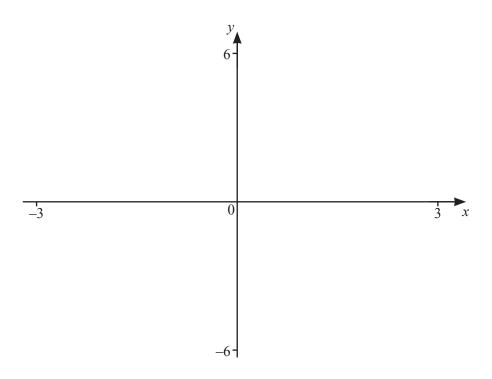
The transformation Q is a rotation of 180° about the origin.

The transformation R is a stretch, scale factor 2 with *x*-axis invariant.

The transformation S is a stretch, scale factor 2 with *y*-axis invariant.

(a)	(i)	Find the co-ordinates of the image of the point (5, 1) under the transformation P.
		(, ,
	(ii)	Find the co-ordinates of the image of the point $(x, y)$ under the transformation P followed by the transformation Q.
		(, ,) [2]
	(iii)	Describe fully the <b>single</b> transformation equivalent to P followed by Q.
(b)	Des	scribe fully the <b>single</b> transformation equivalent to R followed by S.
	••••	
(c)	Des	scribe fully the <b>single</b> transformation equivalent to the inverse of R.

(a)	Sergio in	vests \$2000 at	a rate of 3% p	er year compo	ound interest			
	(i) Find	the value of l	nis investment	at the end of 5	years.			
					\$			. [3]
	(ii) Afte	er how many c	omplete years	is the value of	his investm	ent greater than	n \$4000?	
								F23
		4.000	22.242	_				. [3]
(b)			a rate of 0.24%			erest.		
	Find the	value of her in	vestment at the	e end of 5 year	rs.			
					\$			. [3]
(c)	Calculate	the monthly	compound inte	erest rate that i	s equal to a	compound inte	rest rate of 3% per	year.
							0/	6 [ <b>3</b> ]
							/	ا [ی]



(a) On the diagram, sketch the graph of y = f(x), where

$$f(x) = |x^2 - 4|$$
 for values of x between  $-3$  and 3.

[3]

**(b)** Write down the equation of the line of symmetry of the graph.

Γ1	n	í
1	ш	1

(c) Write down the zeroes of f(x).

	and	[1]
--	-----	-----

(d) (i) Find the value of k when y = k meets the curve  $y = |x^2 - 4|$  three times.

$$k =$$
 [1]

(ii) Find the range of values of k when y = k meets the curve  $y = |x^2 - 4|$  four times.

9	(a)	Solve the	following	equations.
---	-----	-----------	-----------	------------

(i) 
$$\frac{135}{x} = 5$$

$$x = \dots [1]$$

(ii) 
$$3x+5=7x+25$$

$$x = \dots [2]$$

(iii) 
$$8x^2 = 11 - 2x$$

$$x = \dots \text{ or } x = \dots$$
 [4]

**(b)** Solve the following inequalities.

(i) 
$$6-2x \ge 10$$

(ii) 
$$\frac{1}{x-2} > 3$$

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(c)	Solve the simultaneous equations. You must show all your working.		
		3x + 5y = -3 $5x - 2y = 26$	
			<i>x</i> =

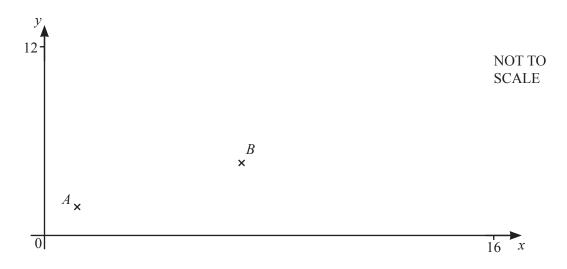
(d) Solve the equation.

$$\log x + 4\log 2 = \log 13$$

$$x =$$
 [3]

y = [4]

10 The points A(1, 2) and B(7, 5) are shown on the diagram below.



(a) Write  $\overrightarrow{AB}$  as a column vector.

**(b)** Calculate the length of the line *AB*.

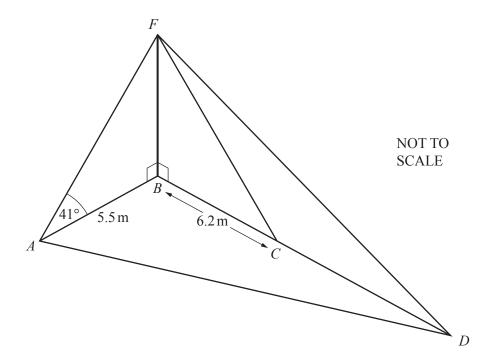
.....[2]

(c) The point C has co-ordinates (10, k). AB = BC and k > 0.

Show that k = 11.

[3]

(d)	Find the equation of the line that is perpendicular to $AC$ that passive your answer in the form $y = mx + c$ .	sses through the midpoint of AC.	
	y =	[4	]
(e)	The points A, B, C and D form a rhombus.		
	Find the co-ordinates of $D$ .		
		() [3	]



The diagram shows four points A, B, C and D on horizontal ground. There is a vertical flagpole, FB, held in place by straight wires AF, CF and DF. BCD is a straight line, AB = 5.5 m, BC = 6.2 m and angle  $FAB = 41^{\circ}$ .

(a) Show that FB = 4.781 m, correct to 3 decimal places.

[2]

**(b)** Calculate angle *FCB*.

Angle FCB = [2]

(c)	Angle $CDF = 18^{\circ}$ .		
	Show that $CD = 8.514$ , correct to 3 decimal places.		
		_	
(1)	A 1. A.D.C. 700	[:	3]
(d)			
	Find AD.		
		$AD = \dots m$ [3]	3]
(e)	Find the area of triangle <i>ABD</i> .		
		m <sup>2</sup> [2	21
		·	_1

12	(a)	y  va $y =$	aries directly as the square root of $(x + 1)$ . 8 when $x = 24$ .			
		(i)	Find the value of $y$ when $x = 15$ .			
				<i>y</i> =	=	[3]
		(ii)	Find the value of $x$ when $y = 16$ .			
				<i>x</i> =	=	[2]

(b)	Fine	d the next term in each of the following sequences.	
	(i)	18, 13, 8, 3, -2,	
			 [1]
	(ii)	3, 6, 11, 18, 27,	
			 [1]
	(iii)	-1000, 100, -10, 1,	
			 [1]
	(iv)	0, 0, 0, 6, 24, 60,	
			 [2]

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