

Cambridge IGCSE™

CAMBRIDGE INTERNATIONAL MATHEMATICS

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Paper 4 (Extended) MARK SCHEME Maximum Mark: 120

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2023 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

- awrt answers which round to
- cao correct answer only
- dep dependent
- FT follow through after error
- isw ignore subsequent working
- nfww not from wrong working
- oe or equivalent
- rot rounded or truncated
- SC Special Case
- soi seen or implied

Question	Answer	Marks	Partial Marks
1(a)	triangle $(-6, -2) (-4, -2) (-4, -5)$	2	B1 for reflection in $y = -1$ or reflection in $x = k$
1(b)	triangle (3, 2) (5, 2) (3, -1)	2	B1 for translation $\begin{pmatrix} 1 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$
1(c)	rotation 180° [centre] (0, 0) oe OR enlargement [centre] (0, 0) oe [sf] -1	3	B1 for each
1(d)	triangle (-1, 2) (0, 5) (0, 2)	2	B1 for correct shape but translated horizontally from correct position.
2(a)(i)	10	1	
2(a)(ii)	28	1	
2(b)	-5	1	
2(c)	$\frac{x-4}{2}$ oe	2	M1 for $2x = y - 4$ or $x = 2y + 4$ or $\frac{y}{2} = x + \frac{4}{2}$
2(d)	$2x^2 + 2x - 3$	2	M1 for $2x^2 + 4x - 2x - 4$ [+1]
2(e)	[x =]1 and [x =]4	3	M1 for $(x-1)^2 - 3(x-1)$ or better
			M1 for $(x-1)(x-4) = 0$
			or
			dep M1 for correct use of formula on <i>their</i> quadratic equation
			or
			dep M1 for sketch of their quadratic equation clearly showing 2 intersections with <i>x</i> -axis
3(a)	$\left[y=\right]\frac{36}{\left(x+1\right)^2}$	2	M1 for $\frac{k}{(x+1)^2}$
3(b)	2.25 oe	2	M1 for $\frac{their36}{(3+1)^2}$ or better

Question	Answer	Marks	Partial Marks
3(c)	2.3[0]	3	M2 for $x+1 = \sqrt[3]{their36}$ or M1 for $x+1 = \frac{their36}{(x+1)^2}$ M1 for sketch of a cubic crossing x axis once with a positive x intercept
4(a)(i)	4 correct points plotted	2	B1 for 3 correct
4(a)(ii)	5.5	1	
4(a)(iii)	[y =] - 0.323x + 7.48	2	B1 for $[y =] -0.323x + k$ or $[y =] kx + 7.48$ or $[y =] -0.32x + 7.5$
4(a)(iv)	[y=]-0.323x+12.48	1	FT their $(k) + 5$
4(b)	12.5	2	M1 for $x \left(\frac{100 - 36}{100} \right) = 8$ oe
4(c)	3.57 or 3.565	2	M1 for $5 \times 5 + 4 \times 6 + 3 \times 9 + 2 \times 3$ implied by 82
5(a)(i)	correct sketch	4	B1 for correct sketch of $2y = x + 5$ B1 for correct sketch of $y = -\frac{1}{2}x + 3$ B1 for correct sketch of $y = x$ passing through (0,0) B1 for all intersections in 1 st quadrant
5(a)(ii)	correct region indicated	2	FT their lines B1 for region satisfying 2 inequalities or for shading shown but region not clearly indicated
5(b)(i)	correct sketch	2	M1 for positive cubic curve with a maximum and minimum
5(b)(ii)	(0.709, 6.3[0])	2	B1 for one correct coordinate
5(b)(iii)	-2.3[0], their 6.3[0]	2	B1 for each

Question	Answer	Marks	Partial Marks
5b(iv)	correct sketch	2	M1 for negative quadratic curve
5b(v)	-0.599 or -0.5987 to -0.5986	1	
6(a)(i)	285	2	M1 for $360 - (180 - 105)$ oe or a sketch with correct indication of 75 or 105 at B
6(a)(ii)(a)	3.75 oe	2	M1 for $\frac{1.5 \times [60]}{24}$
6(a)(ii)(b)	6	2	M1 for $\frac{1.5 \times [1000 \times 100]}{25000}$ oe
6(b)	4430	4	B3 for 5200 OR M1 for $2 + \frac{36}{60}$ or $(2 \times 60) + 36$ or $\frac{\left(2 + \frac{36}{60}\right)}{60}$ M1 for their $2\frac{36}{60} \times 120 \times []$ or their $((2 \times 60) + 36) \times 120 \times []$ M1 for their $2\frac{36}{60} \times \frac{120 \times 1000}{60}$ or their $((2 \times 60) + 36) \times \frac{120 \times 1000}{60 \times 60}$
7(a)	$\cos ABD = \frac{7^2 + 5^2 - 7.63^2}{2 \times 7 \times 5}$	M2	M1 for $7.63^2 = 7^2 + 5^2 - 2 \times 7 \times 5 \times \cos ABD$
	<i>ABD</i> = 76.96	A1	no errors or omissions
7(b)	17.1 or 17.[0] or 17.04 to 17.05	2	M1 for $0.5 \times 5 \times 7 \times \sin 77$
7(c)	1.61 or 1.605 to 1.606	4	M3 for $\frac{7 \sin 12}{\sin (77 - 12)}$ oe or M2 for $\frac{BC}{\sin 12} = \frac{7}{\sin(77 - 12)}$ or B1 for $[ACD =]65^{\circ}$

Question	Answer	Marks	Partial Marks
8(a)(i)	26	2	M1 for $10^2 + 24^2$ or better
8(a)(ii)	15.2 or 15.19 to 15.20	3	M2 for $\sqrt{20^2 - \left(\frac{their26}{2}\right)^2}$ M1 for $20^2 - \left(\frac{their26}{2}\right)^2$
8(a)(iii)	71.8 or 71.78 to 71.80	3	M2 for tan $EFM = \frac{\sqrt{231}}{5}$ or using <i>their</i> height oe ALT M1 for $EF^2 = 20^2 - 12^2$ M1 for $\cos EFM = \frac{5}{their EF}$ or B1 for identifying correct angle or stating EFM
8(b)(i)	10.5	3	M2 for $\sqrt[3]{\frac{222.75}{66}} \times 7$ oe or M1 for $\sqrt[3]{\frac{222.75}{66}}$ oe or $\left(\frac{7}{l}\right)^3 = \frac{66}{222.75}$
8(b)(ii)	2.51 or 2.506 to 2.507	2	M1 for $\sqrt[3]{\frac{66 \times 3}{4\pi}}$
9(a)(i)	$\frac{3}{8}, \frac{5}{8}, \frac{2}{7}, \frac{5}{7}, \frac{3}{8}, \frac{5}{8}$	3	B1 for each correct pair in correct position
9(a)(ii)	365 1568 or 0.233	4	FT <i>their</i> tree diagram probabilities for method marks M3 for $\frac{3}{8} \times \frac{2}{7} \times \frac{5}{6} [+] \frac{3}{8} \times \frac{5}{7} \times \frac{2}{7} [+] \frac{5}{8} \times \frac{3}{8} \times \frac{2}{7}$ soi without extras or M2 for two correct products soi or M1 for one correct product soi or for clear indication on tree diagram of all three combinations. or list of the options
9(b)(i)	10 - x	1	
9(b)(ii)(a)	$\frac{x}{10+y} = \frac{1}{3}$ oe seen leading to $3x = 10 + y$	1	

Question	Answer	Marks	Partial Marks
9(b)(ii)(b)	[x = or red =] 6	5	B2 for $9x + 2y = 70$ oe
	[y = or blue =] 8		or B1 for $\frac{10-x}{10+y} = \frac{2}{9}$
			M1 for correct method to eliminate one variable
			A1 for $[x = or red =] 6$ or $[y = or blue =] 8$
10(a)	45	1	
10(b)	124	2	B1 for <i>BED</i> = 62
10(c)(i)	[<i>EOD</i> =] 72 or [<i>ODE</i> =] 54	B1	seen or implied by 36
	$2 \times 7.5 \times \tan 36 \text{ oe}$ or $2 \times \frac{7.5}{\tan 54}$	M2	M1 for $\tan(36) = \frac{halfside}{7.5}$ or $\tan 54 = \frac{7.5}{halfside}$
	10.89	A1	no errors or omissions
10(c)(ii)	13.1 or 13.11 to 13.13	4	M1 $r^2 = 7.5^2 + \left(\frac{10.9}{2}\right)^2$ or better or trig method for r M1 $\frac{1}{2} \times 10.9 \times 7.5$ or $\frac{1}{2} \times their r^2 \times their \sin 72$ oe M1 $\frac{their 72}{360} \times \pi \times their r^2$ oe
11(a)	$16x^4y^2$ final answer	3	B2 for final answer kx^4y^2 or $16x^ky^2$ or $16x^4y^k$ or $(4x^2y)^2$ B1 for 16 or x^4 or y^2 correct in 3 term final answer or M1 for $4 \times x^2 \times y$ or $4096 \times x^{12} \times y^6$ seen
11(b)	7 nfww	2	M1 for 128 or 6^x or 2187 seen OR M1 for $x = \frac{\log 279936}{\log 6}$

Question	Answer	Marks	Partial Marks
11(c)(i)	$\frac{15}{x+2} + \frac{15}{x+2} + \frac{2}{x} = 16$ or $\frac{30}{x+2} + \frac{2}{x} = 16$	M1	
	$\frac{30x+2(x+2)}{x(x+2)}$ [=16] or better	M2	M1 for $30x + 2(x+2)$ M1 for common denominator $x(x+2)$ oe
	30x + 2x + 4 = 16x(x + 2)	M1	FT <i>their</i> numerator with correct denominator to fraction removed
	rearranging to get to $4x^2 - 1 = 0$	A1	no errors or omissions
11(c)(ii)	6	2	M1 for $x = \frac{1}{2}$ or for 6 and 10 as answers