## Cambridge IGCSE ${ }^{\text {TM }}$

CAMBRIDGE INTERNATIONAL MATHEMATICS
Paper 4 (Extended)
MARK SCHEME
Maximum Mark: 120

## Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes
Cambridge International is publishing the mark schemes for the October/November 2023 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

## Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

## GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.


## GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

## GENERIC MARKING PRINCIPLE 3:

Marks must be awarded positively:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.


## GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

## Mathematics-Specific Marking Principles

1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.

2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.

3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.

4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).

5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.

6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

## Types of mark

M Method marks, awarded for a valid method applied to the problem.
A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.

B Mark for a correct result or statement independent of Method marks.
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

## Abbreviations

| awrt | answers which round to |
| :--- | :--- |
| cao | correct answer only |
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| nfww | not from wrong working |
| oe | or equivalent |
| rot | rounded or truncated |
| SC | Special Case |
| soi | seen or implied |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 1(a) | 84.9 or 84.85 to 84.86 | 1 |  |
| 1(b) | 7.08 or 7.079 to 7.08 | 2 | M1 for distance divided by time. or B1 for 113 |
| 1(c) | 9.58 or 9.579 to 9.580 | 3 | M1 for distance divided by speed M1 for $\div 1000$ and $\times 60 \times 60$ |
| 2(a)(i) | 20 | 1 |  |
| 2(a)(ii) | 13.5 | 1 |  |
| 2(a)(iii) | 12.9 or 12.91 to 12.92 | 1 |  |
| 2(a)(iv) | 16 | 1 |  |
| 2(a)(v) | 17.5 | 1 |  |
| 2(b) | It's the highest oe | 1 |  |
| 3(a) | Triangle at ( $-4,4$ ), (-2, 4), (-4, 3) | 2 | B1 for translation through $\left(\frac{-5}{k}\right)$ or $\left(\frac{k}{2}\right)$ |
| 3(b) | Enlargement [Scale Factor]-2 [Centre] $(2,3)$ | 3 | B1 for each |
| 3(c)(i) | Triangle at ( $-2,-1$ ), (-1, -1) , (-2, -3) | 4 | B2 for triangle at $(1,-3),(1,-4),(3,-4)$ or $\mathbf{B 1}$ for reflection in $y=k$ or $x=-1$ <br> dep B1 for rotation of their first image $90^{\circ}$ clockwise or anticlockwise about ( $1,-$ 1) or rotation $90^{\circ}$ clockwise about wrong centre. <br> If 0 scored, SC1 for correct triangle translated |
| 3(c)(ii) | Reflection $y=-x \text { oe }$ | 2 | B1 for each |
| 4(a) |  | 2 | B1 for any cubic with positive $x^{3}$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 4(b) | $\begin{aligned} & -2.12 \text { or }-2.116 \ldots \\ & 0.537 \text { or } 0.5370 . . \\ & 3.08 \text { or } 3.079 \ldots \end{aligned}$ | 3 | B1 for each |
| 4(c) | 14 and -13 cao | 2 | B1 for each or B1 for both14 and -13 seen |
| 4(d) | $-1<x<2$ | 2 | B1 for each |
| 5(a) | 12500 | 2 | M1 for $P\left(1+\frac{60}{100}\right)=20000 \mathrm{oe}$ |
| 5(b) | $\begin{aligned} & 20000 \times\left(1+\frac{60}{100}\right)^{4} \mathrm{oe} \\ & {[=131072]} \end{aligned}$ | 1 |  |
| 5(c) | 2065 nfww | 4 | B3 for 9 or 8.32 or 8.323 ... or for 45 or 41 to 42 <br> OR <br> M3 for $n \log \left(1+\frac{60}{100}\right)=\log \left(\frac{1000000}{20000}\right)$ oe or good sketch indicating value between 8 and 9 or correct trials as far as 8 and 9 <br> or M2 for $\left(1+\frac{60}{100}\right)^{n}=\frac{1000000}{20000}$ oe or sketch that could lead to solution e.g. $y=1.6^{x}$ and $y=\frac{1000000}{20000}$ or at least 3 correct trials or M1 for $20000 \times\left(1+\frac{60}{100}\right)^{n}=1000000 \text { soi }$ <br> or at least 2 correct trials |
| 6(a)(i) | 400 | 2 | $\mathbf{M 1} \text { for } \frac{1}{3} \times 10^{2} \times 12$ |
| 6(a)(ii) | $\sqrt{\left(\frac{10}{2}\right)^{2}+12^{12}}$ <br> leading to 13 | M2 | M1 for $\left[V M^{2}=\right]\left(\frac{10}{2}\right)^{2}+12^{2}$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 6(b)(i) | 195.2 or 195 | 4 | B3 for 204.8 <br> OR <br> B2 for 9.6 or awrt 9.6 or M1 for [height of small pyramid] = $12 \times \frac{8}{10}$ oe <br> M1 for $\frac{1}{3} \times 8^{2} \times($ their 9.6$)$ <br> OR <br> M3 for their $400 \times\left(1-\left(\frac{8}{10}\right)^{3}\right)$ oe or M2 for their $400 \times\left(\frac{8}{10}\right)^{3}$ oe or M1 for $\left(\frac{8}{10}\right)^{3}$ oe |
| 6(b)(ii) | 257.6 or 258 | 4 | B1 for $13 \times \frac{2}{10}$ or $13 \times \frac{8}{10}$ <br> M1 for <br> $8 \times($ their 2.6$)+2 \times \frac{1}{2} \times 1 \times($ their 2.6$)$ oe <br> M1 for $8^{2}$ and $10^{2}$ soi |
| 7(a)(i) | 182 | 1 |  |
| 7(a)(ii) | 16 | 2 | B1 for [uq=] 189 or [lq=] 173 |
| 7(b) | 170 | 2 | B1 for 48 seen |
| 7(c) | $56,84,36,12,4$ | 2 | B1 for 3 or 4 correct |
| 7(d) | 181 | 2 | M1 for at least 4 mid-points soi |
| 8(a) | -36 | 2 | M1 for $60+(-32) \times 3$ oe or $\mathbf{B 1}$ for 96 seen |
| 8(b)(i) | 0.7 oe | 2 | M1 for $6 x+4 x=9-2$ or better |
| 8(b)(ii) | 5 and -2 nfww | 3 | B2 for -2 nfww <br> B1 for 5 <br> or M1 for $2 x-3=-7$ or $2 x-3= \pm 7$ or M1 for a correct diagram |
| 8(c) | $(3 x-2)(x-3)$ | M1 |  |
|  | $[x=] \frac{2}{3} \text { oe }, 3$ | B1 |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 8(d) | $\frac{3 b}{5 y-a}$ oe final answer | 3 | M1 for $5 x y=a x+3 b$ <br> M1FT for $5 x y-a x=3 b$ <br> M1FT for factorising and division <br> Incorrect answers score M2 maximum. |
| 8(e) | $\frac{a-2 b}{x-3 y}$ oe final answer | 4 | B2 for $(x+3 y)(a-2 b)$ or B1 for $x(a-2 b)+3 y(a-2 b)$ oe B1 for $(x+3 y)(x-3 y)$ |
| 9(a) | U <br> B | 2 | B1 for each |
| 9(b)(i) | 21 | 1 |  |
| 9(b)(ii) | $\frac{13}{120} \text { oe }$ | 1 |  |
| 9(b)(iii) | $\frac{35}{528} \text { oe }$ | 3 | M2 for $\frac{5}{33} \times \frac{7}{32}+\frac{7}{33} \times \frac{5}{32}$ oe or M1 for either product correct |
| 9(b)(iv) | $\frac{3}{1003} \mathrm{oe}$ | 3 | M2 for $k \times \frac{21}{120} \times \frac{20}{119} \times \frac{4}{118}$ oe $k=1,3$ or 6 or M1 for $\frac{p}{120} \times \frac{p-1}{119} \times \frac{4}{118}$ oe |
| 10(a)(i) | 9 | 1 |  |
| 10(a)(ii) | -33 | 2 | B1 for $[\mathrm{h}(4)]=-8$ or M1 for $4 \times 4(2-4)-1$ |
| 10(a)(iii) | $5-8 x$ final answer | 2 | M1 for 3-2(4x-1) or better |
| 10(a)(iv) | $2-\frac{x}{4}$ oe final answer | 2 | M1 for $x=4(2-y)$ or $\frac{y}{4}=2-x$ or $y-8=-4 x$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 10(b)(i) |  | 3 | B2 for correct left-hand branch or B1 for left-hand branch with a positive y -intercept or passing through origin <br> AND <br> B1 for correct right-hand branch |
| 10(b)(ii) | $x=1.5$ oe | 1 |  |
| 10(b)(iii) | $\begin{aligned} & 1.06 \text { or } 1.064 \text { to } 1.065 \\ & 2.94 \text { or } 2.935 \ldots \end{aligned}$ | 3 | B2 for one correct or M1 for sketch of $y=4(2-x)$ |
| 10(b)(iv) | 8, -32, 25 | 3 | B2 for 2 correct <br> OR <br> M1 for $4(2-x)(3-2 x)=4 x-1$ <br> B1 for $6-7 x+2 x^{2}$ or $24-28 x+8 x^{2}$ |
| 11(a) | 33.7 or 33.69... | 2 | $\mathbf{M 1} \text { for } \tan [p]=\frac{12}{18}$ |
| 11(b)(i) | $150^{2}+180^{2}$ | M1 |  |
|  | $[\cos =] \frac{192^{2}+230^{2}-\text { their }\left(180^{2}+150^{2}\right)}{2 \times 190 \times 230}$ | M2 | M1 for their $\left(180^{2}+150^{2}\right)=190^{2}+230^{2}$ $-2 \times 190 \times 230 \cos B$ |
|  | 67.03 to 67.04 | A1 |  |
| 11(b)(ii) | 175 or 174.8 to 174.9... | 3 | M2 for $\sin 67[.0]=\frac{x}{190}$ oe or M1 for distance required is perpendicular to $B C$ oe |
| 12(a)(i) | $(0,7)$ | 1 |  |
| 12(a)(i) | $\left(\frac{-5}{3}, 2\right)$ | 2 | M1 for $2-7=3 x$ or B1 for $\frac{-5}{3}$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 12(b) | $y=\frac{3}{5} x+\frac{21}{5} \text { oe }$ | 5 | B4 for $\frac{3}{5} x+\frac{21}{5}$ oe OR <br> B1 for midpoint $=(-2,3)$ <br> M1 for $m_{A B}=\frac{8-(-2)}{-5-1}$ oe <br> $\mathbf{M 1}$ for $m=\frac{-1}{\operatorname{their}\left(m_{A B}\right)}$ <br> M1 for substituting their $(-2,3)$ into $y=($ their $m) x+c$ oe |

