## Cambridge IGCSE ${ }^{\text {TM }}$



## CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/53
Paper 5 Investigation (Core)
October/November 2023
1 hour 10 minutes
You must answer on the question paper.
No additional materials are needed.

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a graphic display calculator where appropriate.
- You may use tracing paper.
- You must show all necessary working clearly, including sketches, to gain full marks for correct methods.
- In this paper you will be awarded marks for providing full reasons, examples and steps in your working to communicate your mathematics clearly and precisely.


## INFORMATION

- The total mark for this paper is 36 .
- The number of marks for each question or part question is shown in brackets [ ].

Answer all the questions.

## INVESTIGATION

## CLOCK HANDS

This investigation looks at the angle between the hands of a clock at different times of day.
You should not measure angles from the clock diagrams.
In this investigation:

- the hour hand is labelled $H$
- the minute hand is labelled $M$
- the hands of the clock rotate clockwise in the direction shown
- the clockwise angle between the two hands is shown on the clock.


1 (a) The clock shows the time 1.00 am .
(i) Write down the mathematical name for the type of angle shown.
(ii) Explain why hand $H$ rotates through $360^{\circ}$ in 12 hours.
$\qquad$
(iii) Write down the calculation to show that the clockwise angle from hand $M$ to hand $H$ is $30^{\circ}$.
(iv) Write down a calculation to show that the anticlockwise angle from hand $M$ to hand $H$ is $330^{\circ}$.
(b) This clock shows the time 4.00 am .
(i) Work out the clockwise angle from hand $M$ to hand $H$.

$\qquad$
(ii) Work out the anticlockwise angle from hand $M$ to hand $H$.
$\qquad$
(c) Write down the clockwise angle from hand $M$ to hand $H$ at 6.00 am .
(d) Complete the table using part (b) and part (c).

You may use the clock diagrams and patterns to help you.

| Hour shown by hand $H$ <br> $(x)$ | Angle between hand $H$ and hand $M$ in degrees |  |
| :---: | :---: | :---: |
|  | Clockwise angle | Anticlockwise angle |
| 1 | 30 | 330 |
| 2 |  |  |
| 3 |  |  |
| part (b) | 4 |  |


(e) Find an expression for the clockwise angle at hour $x$.
$\qquad$
(f) Write down the rule for continuing the sequence in the anticlockwise angle column.
$\qquad$
(g) Find an expression for the anticlockwise angle at hour $x$.

2 (a) In one hour, hand $H$ rotates clockwise from one number to the next number. For example, from 1.00 am to 2.00 am hand $H$ rotates from 1 to 2 .

Show that hand $H$ rotates $0.5^{\circ}$ in one minute.
(b) In one hour, hand $M$ rotates through a full circle.

Show that hand $M$ rotates $6^{\circ}$ in one minute.

3 (a) This clock shows the time 1.10 am .
(i) Use Question 2(a) to find the angle that hand $H$ has rotated in the 10 minutes since 1.00 am .

[2]
(ii) Use Question 2(b) to find the angle that hand $M$ has rotated in the 10 minutes since 1.00 am .
(iii) Show that the clockwise angle from hand $H$ to hand $M$ at 1.10 am is $25^{\circ}$.
(b) Complete the table using your results from part (a)(i) and part (a)(ii).

You may use the clock diagrams and patterns to help you.

|  | Number of minutes since 1.00 am ( $m$ ) | Angle rotated since 1.00 am in degrees |  | Clockwise angle between the hands in degrees |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Hand $H$ angle | Hand $M$ angle |  |
|  | 6 |  |  |  |
|  | 7 | 3.5 | 42 | 8.5 |
|  | 8 |  |  |  |
|  | 9 |  |  |  |
| $\begin{aligned} & \text { part (a)(i) } \\ & \text { part (a)(ii) } \end{aligned}$ | 10 |  |  | 25 |


[6]
(c) Find an expression, in terms of $m$, for the clockwise angle between the hands.
(d) Find how many minutes and seconds after 1.00 am the clockwise angle is $270^{\circ}$. Give your answer correct to the nearest second.
minutes $\qquad$ seconds [5]

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