ANNA Pape		
TIONAL EXAMINATIONS	Y OF CAMBRIDGE INTE	
4037/02	ATHEMATICS	ADDITIONAL M
October/November 2005		Paper 2
2 hours	Answer Booklet/Paper Graph paper Mathematical tables	Additional Materials:

## **READ THESE INSTRUCTIONS FIRST**

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet. Write your Centre number, candidate number and name on all the work you hand in. Write in dark blue or black pen on both sides of the paper. You may use a soft pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** the questions.

Write your answers on the separate Answer Booklet/Paper provided.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question. At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 80.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.



## Mathematical Formulae

## 1. ALGEBRA

# Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

**Binomial Theorem** 

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ .

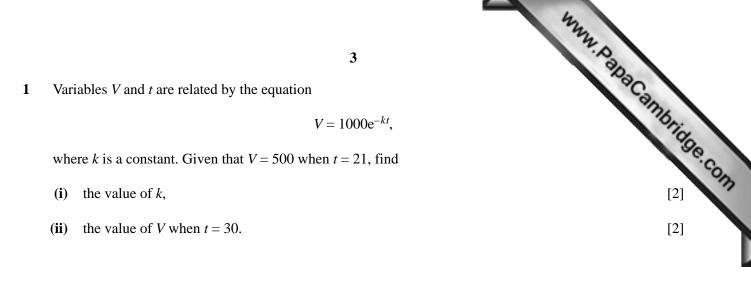
### 2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1.$$
$$\sec^2 A = 1 + \tan^2 A.$$
$$\csc^2 A = 1 + \cot^2 A.$$

Formulae for  $\triangle ABC$ 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}.$$
$$a^2 = b^2 + c^2 - 2bc \cos A.$$
$$\Delta = \frac{1}{2}bc \sin A.$$



- 2 The line x + y = 10 meets the curve  $y^2 = 2x + 4$  at the points *A* and *B*. Find the coordinates of the mid-point of *AB*. [5]
- 3 (i) Given that  $y = 1 + \ln (2x 3)$ , obtain an expression for  $\frac{dy}{dx}$ . [2]
  - (ii) Hence find, in terms of p, the approximate value of y when x = 2 + p, where p is small. [3]
- 4 The function f is given by  $f: x \mapsto 2 + 5 \sin 3x$  for  $0^\circ \le x \le 180^\circ$ .

State the amplitude and period of f.

(i)

(ii) Sketch the graph of y = f(x). [3]

[2]

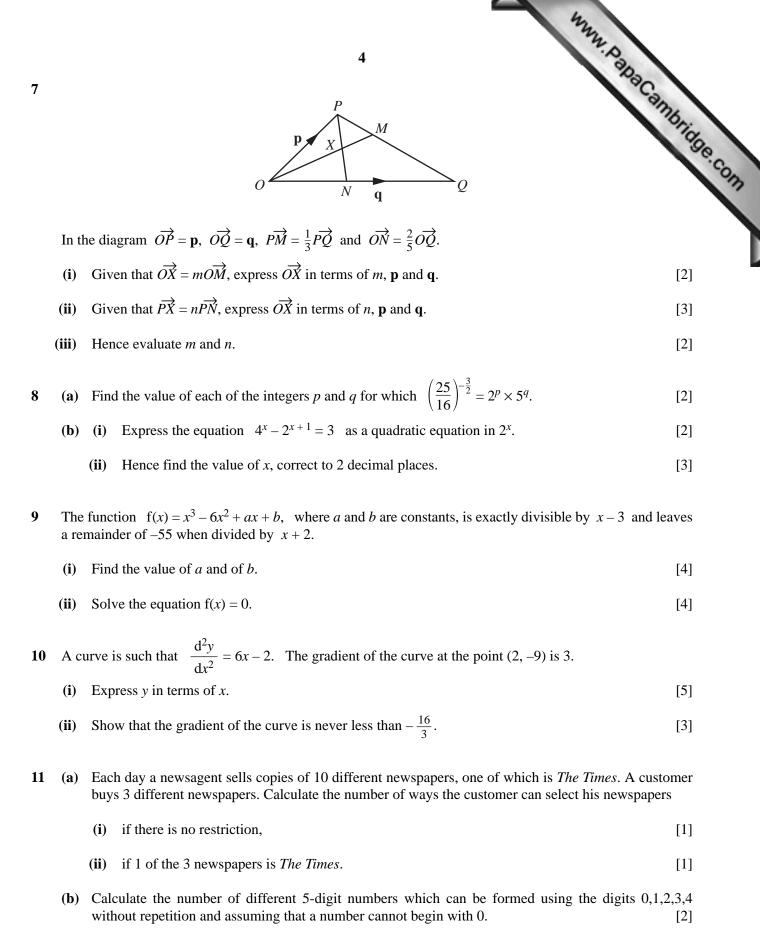
[6]

5 The binomial expansion of  $(1 + px)^n$ , where n > 0, in ascending powers of x is

$$1 - 12x + 28p^2x^2 + qx^3 + \dots$$

Find the value of n, of p and of q.

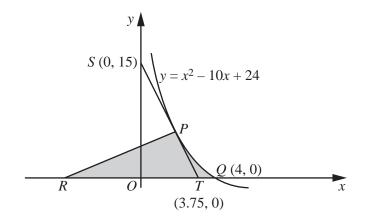
6 It is given that  $\mathbf{A} = \begin{pmatrix} 3 & 1 \\ 5 & p \end{pmatrix}$  and that  $\mathbf{A} + \mathbf{A}^{-1} = k\mathbf{I}$ , where *p* and *k* are constants and **I** is the identity matrix. Evaluate *p* and *k*. [6]



How many of these 5-digit numbers are even?

[4]

### EITHER



The diagram, which is not drawn to scale, shows part of the curve  $y = x^2 - 10x + 24$  cutting the x-axis at Q(4, 0). The tangent to the curve at the point P on the curve meets the coordinate axes at S(0, 15) and at T (3.75, 0).

The normal to the curve at P meets the x-axis at R.

(ii) Find the coordinates of 
$$R$$
. [2]

(iii) Calculate the area of the shaded region bounded by the *x*-axis, the line *PR* and the curve *PQ*. [5]

#### OR

A curve has the equation  $y = 2\cos x - \cos 2x$ , where  $0 < x \le \frac{\pi}{2}$ .

(i) Obtain expressions for 
$$\frac{dy}{dx}$$
 and  $\frac{d^2y}{dx^2}$ . [4]

(ii) Given that  $\sin 2x$  may be expressed as  $2\sin x \cos x$ , find the *x*-coordinate of the stationary point of the curve and determine the nature of this stationary point. [4]

(iii) Evaluate 
$$\int_{\pi/3}^{\pi/2} y \, dx.$$
 [3]

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