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4037 ADDITIONAL MATHEMATICS

4037/02

Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the October/November 2007 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

Mark Scheme Notes

Marks are of the following three types:

- www.papacambridge.com Μ Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- А Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- В Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol $\sqrt{}$ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- B2 or A2 means that the candidate can earn 2 or 0. Note: B2, 1, 0 means that the candidate can earn anything from 0 to 2.

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		C2				
The follo	wing abbreviations may be used in a mark scheme or used	d on the scripts:				
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)					
BOD	Benefit of Doubt (allowed when the validity of a solution	may not be absolutely				

- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- Correct Answer Only (emphasising that no "follow through" from a previous CAO error is allowed)
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)

Penalties

- MR -1 A penalty of MR -1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{}$ " marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy.
- OW -1,2 This is deducted from A or B marks when essential working is omitted.
- PA -1 This is deducted from A or B marks in the case of premature approximation.
- S -1 Occasionally used for persistent slackness – usually discussed at a meeting.
- EX -1 Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

	May May	
Page	4 Mark Scheme Syllabu	er oer
	GCE O LEVEL – October/November 2007 4037	Day
1 [4]	(i) $dy/dx = x^{-3}$ × (-1600) oe (ii) $\delta y = \frac{dy}{dx} \delta x = -\frac{1600}{1000} p = -1.6p$	oanacannbridge. M1 A1√
2 [5]	$sin(x/2-1) = 1/3$ 0.34 (19.5°) or 2.8(0) or $\pi - 0.34$ (160.5°)	B1 B1√
	Using radians, + 1, ×2 \Rightarrow 2.68 or 7.6(0) (both, no other values < 15)	M1 A1
	or 15.2~3 (no other values between 15 and 20)	A1
3 [5]	(i) $9^{x+1} \Rightarrow 3^{2x+2}$ (ii) $\sqrt[3]{27^{2x}} \Rightarrow 3^{2x}$	B1
	(ii) $\sqrt[3]{27^{2x}} \Rightarrow 3^{2x}$	B1
	(iii) Substitute (i) and (ii) into expression	В1√
	Correctly cancel powers involving <i>x</i> simplify $\Rightarrow 2/3$	M1 A1
4 [6]	$ (\mathbf{i}) (0.3 \ 0.3 \ 0.2 \ 0.2) \begin{pmatrix} 8 & 12 & 4 \\ 7 & 10 & 2 \\ 10 & 12 & 0 \\ 6 & 8 & 4 \end{pmatrix} \begin{pmatrix} 300 \\ 500 \\ 800 \end{pmatrix} \text{or} (300 \ 500 \ 800) \begin{pmatrix} 8 & 7 & 10 & 6 \\ 12 & 10 & 12 & 8 \\ 4 & 2 & 0 & 4 \end{pmatrix} \begin{pmatrix} 0.3 \\ 0.3 \\ 0.2 \\ 0.2 \end{pmatrix} $	M1 A1
	(ii) 1^{st} product (7.7 10.6 2.6) or $\begin{pmatrix} 11600 \\ 8700 \\ 9000 \\ 9000 \end{pmatrix}$ or transpose of either	M1 A1
	2^{nd} product [2310+5300 +2080 or 3480 +2610+1800+1800] \Rightarrow \$9690 for 9690 with no matrices allow sc 1	M1 A1
5 [6]	(i) $(1 + x)^5 = 1 + 5x + 10x^2 + 10x^3 + 5x^4 + x^5$	B1
	(ii) $(\sqrt{2})^3 = 2\sqrt{2}$ $(\sqrt{2})^5 = 4\sqrt{2}$ $(1 + \sqrt{2})^5 = 41 + 29\sqrt{2}$	B1 B1 B1
	(iii) $(1 - \sqrt{2})^5 = 41 - 29\sqrt{2}$ $(1 + \sqrt{2})^5 + (1 - \sqrt{2})^5 = 82$	B1√ B1√

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			AN. Papacambrida A1 AN
6 [6]	Uses	x, y or equivalent correctly in either equation	M
	π <i>x</i> ² +	$\pi y^2 = 29\pi / 2$ and $2\pi x + 2\pi y = 10\pi$	A1 A
	Elimin	ate one variable $[x^2 + (5 - x)^2 = 14.5]$	M1
	Correc	ctly substitute into formula or factorise 3 term quadratic [$4x^2 - 20x + 21 = 0$	0] M1
	1.5, 3	.5	A1
7 [6]	(i) <u>B</u> C	$\vec{c} = (k - 6)i + 15j$ (may be implied)	B1
	(<i>k</i>	$(x-6)^2 + 15^2 = 25^2 \implies k = 26 \text{ (ignore } -14 \text{)}$	M1 A1
	(ii) <i>AE</i>	$\vec{A} = 4\mathbf{i} + 6\mathbf{j}$ [or $\vec{AC} = (k-2)\mathbf{i} + 21\mathbf{j}$] or grad 6/4 or ratio 6:4	B1
	$\binom{k}{2}$	$ \binom{-6}{15} = \lambda \binom{4}{6} \text{or} \binom{k-2}{21} = \mu \binom{4}{6} \text{or} \binom{k-2}{21} = \nu \binom{k-6}{15} $	
	λ =	2.5 or $\mu = 3.5$ or $v = 1.4$ or x step =10 or solve sim equations	s M1
	<i>k</i> = 1	from <i>y</i> =m <i>x</i> +c	A1
8 [7]	A :	<i>x</i> < 6	B1
	<i>x</i> ² –	$11x + 28 = 0 \implies (x - 4)(x - 7) = 0 \implies x = 4, 7$	M1 A1
	B : 4	4 < <i>x</i> < 7	
	(i) 4	$4 < x < 6$ (ii) $7 \le x < 10$	M1A1 M1A1
	If integ	gers used allow sc1 for (i) {5} and sc1 for (ii) {7, 8, 9}	
9 [7]	(i) (a	$a =) \sin(t/2) \times (-4)$	M1 A1
	W	hen $t = 1$, $a \approx -1.92$	A1√
	(ii) (s	$s =) \sin(t/2) \times 16$	M1 A1
	At	P, $v = 0, t = \pi$ $OP = \left[16\sin\left(\frac{t}{2}\right)\right]_0^{\pi} = 16$	B1 A1√
10 [9]	(i) At	X, y = 0, x = 16	B1 cso
	dy .	$dx = x^{-1/2}$ $x + x^{1/2} - 1$	M1 A1
	(d <i>y</i> /d	$x) = 0 \implies \text{at } M, \ x = 4, \ y = 4$	M1 A1
	(ii) ∫	$4\sqrt{x}dx = x^{3/2} + 4x^{2/3} \text{ or } x4 \div 3/2 \int (-x)dx = -x^2/2$	M1 A1 B1
		$\frac{8x^{3/2}}{3} - \frac{x^2}{2} \bigg _{0}^{16} = 42^{2/3}$	A1

Page 6	Mark Scheme Syllabu	ger
	GCE O LEVEL – October/November 2007 4037	Space 1
1 [9]		ambrid
		Dana Cambridas
(i)	$m_{AO} = -1/2$ Equation of <i>OB</i> is $y = 2x$	B1 B1√
(ii)	(Length of $OA = \sqrt{45}$) \Rightarrow Length of $OB = 2\sqrt{5}$ oe	M1
	$\sqrt{x^2 + (2x)^2} = 2\sqrt{5} \implies x = 2$ B is (2, 4)	M1 A1
(iii	i) $\overrightarrow{OC} = \frac{1}{3}\overrightarrow{AO} = \frac{1}{3}(-6,3) = (-2,1)$	M1 A1
(iv	v) Area $COB = \frac{1}{3} \times \text{area } AOB = 5 \implies \text{Area } ABCD = 40 \text{ [Any valid method]}$	M1 A1
2E [10] (i)	$-\infty < (f) < \infty$ (i.e. all real values) (ii) $(f^{-1}) > 0$ (i.e. all positive values)	B1 B1
(iii	Graph of $f(x) = \ln x$ Graph of $f^{-1}(x)$ (as e^x or reflection in $y = x$)	B1 B1
(iv	fg(x) = ln (3x + 2) = 3 \Rightarrow x = (e ³ - 2)/3 [≈ 6.0(3)]	M1 A1
(v)	$g^{-1}(x) = (x-2)/3$ $f^{-1}(x) = e^{x} [can be earned anywhere]$	B1 B1
	$e^{(x-2)/3} = 7 \implies x = 3 \ln 7 + 2 \text{ oe} [\approx 7.84 \text{ condone } 7.8]$	M1 A1
	Or $g^{-1}(x) = (x-2)/3$ $f^{-1}g^{-1}(x) = 7 \Rightarrow g^{-1}(x) = f(7)$	B1 B1
	$(x-2)/3 = \ln 7 \implies x = 3\ln 7 + 2 \text{ oe} [\approx 7.84 \text{ condone } 7.8]$	M1 A1
	Or $f^{-1}g^{-1}(x) = 7 \implies g^{-1}(x) = f(7) \implies x = g f(7)$	B1 B1
	x = g(ln 7) = 3ln 7 + 2 oe [≈ 7.84 condone 7.8]	M1 A1
:O [10] (i)	Eliminate y and rearrange $[4x^2 + (2 - k)x + 1 = 0]$ Equal roots $\Rightarrow [(2 - k)^2 = 16]$	M1 M1
c	Or $dy/dx = k = 8x + 2$ Use 3 equations to eliminate 2 of k, y, x	M1 M1
5	Solve for 2 values of k $k = -2 \text{ or } 6$	M1 A1cso
(ii)	$4(x + \frac{1}{4})^2 + \frac{2}{4}$ or $a = 4, b = \frac{1}{4}, c = \frac{2}{4}$	B1 B1 B1
(iii) $4x^2 + 2x + 3 = 0 \implies 2^2 - 4 \times 4 \times 3 < 0 \implies$ no real roots	M1 A1
c	Dr using (ii), minimum value of $y = 2\frac{3}{4}$ [when $x = -\frac{1}{4}$]	M1 A1
C	Or minimum $y = 2\frac{3}{4}$ [when $x = -\frac{1}{4}$] via $dy/dx = 8x + 2$, and $d^2y/dx^2 = 8 > 0$ or indication of shape	M1 A1
c	Or $4(x + \frac{1}{4})^2 = -11/4$ not possible	M1 A1
(iv) f must be one-one ; hence, from (ii), $(p =) -\frac{1}{4}$	B1√