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UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS GCE Ordinary Level

MARK SCHEME for the May/June 2009 question paper for the guidance of teachers

4037 ADDITIONAL MATHEMATICS

4037/01

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the May/June 2009 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2, 1, 0 means that the candidate can earn anything from 0 to 2.

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The follow	ving abbreviations may be used in a mark scheme or use	d on the scripts:
AG	Answer Given on the question paper (so extra checking the detailed working leading to the result is valid)	d on the scripts: is needed to ensure that
BOD	Benefit of Doubt (allowed when the validity of a solution clear)	on may not be absolutely
CAO	Correct Answer Only (emphasising that no "follow throus is allowed)	gh" from a previous error
ISW	Ignore Subsequent Working	
MR	Misread	
PA	Premature Approximation (resulting in basically correct accurate)	work that is insufficiently

Penalties

SOS

MR -1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{\ }$ " marks. MR is not applied when the candidate misreads his own figures - this is regarded as an error in accuracy.

See Other Solution (the candidate makes a better attempt at the same question)

- OW –1,2 This is deducted from A or B marks when essential working is omitted.
- PA -1 This is deducted from A or B marks in the case of premature approximation.
- S –1 Occasionally used for persistent slackness – usually discussed at a meeting.
- EX -1 Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

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			3
1	(i) $12 = 15\theta$, $\theta = 0.8$ rads	M1, A1 [2]	M1 for use of $s = r\theta$
	(ii) Area = $\frac{1}{2}15^2(0.8)$	M1	M1 for use of $s = r\theta$ M1 for use of $A = \frac{1}{2}r^2\theta$
	leading to 90 (cm ²)	A1	2
		[2]	
2	$x^3 = 8$, leading to $x = 2$	B1	B1 for finding where curve crosses the <i>x</i> axis
	$\frac{dy}{dx} = 3x^2 \text{ leading to grad of } -\frac{1}{12}$ for normal	M1	M1 for attempt to differentiate and use of $m_1m_2 = -1$
	$y - 0 = -\frac{1}{12}(x - 2)$	DM1 A1	DM1 for attempt at equation of normal Allow unsimplified
	$\left(y = -\frac{1}{12}x + \frac{1}{6}\right)$	[4]	
3			
i	$\frac{1-\cos^2\theta}{\sec^2\theta-1} = \frac{\sin^2\theta}{\tan^2\theta}$	M1	M1 for use of $1 - \cos^2 \theta = \sin^2 \theta$
	$\frac{\sec^2\theta - 1}{\sec^2\theta} = \frac{\tan^2\theta}{\tan^2\theta}$	M1	M1 for use of $\sec^2 \theta - 1 = \tan^2 \theta$
	$=\cos^2\theta$	M1	M1 for attempt to simplify
	$=1-\sin^2\theta$	A1 [4]	
	Alt Scheme		
	$\frac{1-\cos^2\theta}{\cos^2\theta} = \frac{\sin^2\theta}{\cos^2\theta}$	M1	M1 for use of $1 - \cos^2 \theta = \sin^2 \theta$
	$\frac{1-\cos^2\theta}{\sec^2\theta-1} = \frac{\sin^2\theta}{1-\cos^2\theta/\cos^2\theta}$	M1	M1 for attempting to get all in terms of cos
Ī	$=\frac{\sin^2\theta\cos^2\theta}{\sin^2\theta}$	M1	M1 for attempt to simplify
	$=\cos^2\theta$		
	$=1-\sin^2\theta$	A1	
4	(i) $5x-3 = kx^2 - 3x + 5$	M1	M1 for equating line and curve equations
	$kx^2 - 8x + 8 = 0$	DM1, A1	DM1 for use of $b^2 - 4ac$ on resulting
	using $b^2 - 4ac = 0$, $k = 2$	[3]	quadratic
	(Alt scheme: $5 = 2kx - 3$, $x = \frac{4}{k}$		(Alt scheme: M1 for attempt to differentiate
	$\frac{20}{k} - 3 = \frac{16}{k} - \frac{12}{k} + 5$		quadratic and equate to 5 DM1 for simplification and solution using
	$\begin{array}{ccc} k & k & k \\ \text{leading to } k = 2 \end{array}$		resulting quadratic
1	(ii) leading to $x = 2, y = 7$	M1, A1 [2]	M1 for obtaining x and y coords

		MAN
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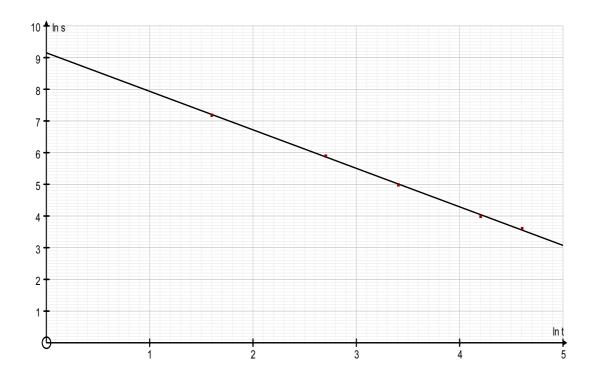
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5	(a) $3^{2(2x-1)} = 3^{3x}$	B1	B1 for $3^{2(2x-1)}$ B1 for 3^{3x} B1 for $x = 2$
	4x - 2 = 3x	B1	B1 for 3^{3x}
	x = 2	B1	B1 for $x = 2$
		[3]	
	(b) $a^{-2}b$ or $\frac{b}{a^2}$ (allow here) $p = -2, q = 1$	B1 B1 [2]	B1 for each
6	f(3), $f(-5)$ or $f(0.5) = 0$ spotted	B1	B1 for spotting one root
	Either $(2x-1)(x^2+2x-15)$	M1	M1 for attempt to obtain quadratic factor
	Or $(x+5)(2x^2-7x+3)$	A1	A1 all correct
	Or $(x-3)(2x^2+9x-5)$	M1	M1 for solution of quadratic
	x = 3, -5, 0.5	A2,1,0	A2 for all 3 solutions (–1 each error)
		F.63	Correct factors only – lose 1 A mark
		[6]	
7	(i) $3xe^{3x} + e^{3x} - e^{3x}$	M1, A1, B1	M1 for attempt to differentiate a product.
	$=3xe^{3x}$		A1 for correct product.
		[3]	B1 for $-e^{3x}$
	(ii) $\int xe^{3x} dx = \frac{1}{3} \left(xe^{3x} - \frac{e^{3x}}{3} \right)$	DM1 DM1 A1 [3]	DM1 for recognition of the 'reverse' to (i) DM1 for dealing with '3' A1 all correct (condone omission of c)
8	(i) $\frac{dy}{dx} = \frac{(x^2 + 9)2 - 2x(2x)}{(x^2 + 9)^2}$	B2,1,0	Attempt to differentiate a quotient —1 each error
	$= \frac{18 - 2x^2}{\left(x^2 + 9\right)^2}$, turning points,	M1	M1 for correct attempt to find the turning
	,		points.
	$x = \pm 3$	A1	A1 for both
		[4]	
	(ii) $\frac{\mathrm{d}x}{\mathrm{d}t} = 2$	B1	B1 for use of $\frac{dx}{dt} = 2$
	(ii) $\frac{1}{dt} - 2$	וטו	$\frac{1}{dt}$
	$\frac{\mathrm{d}y}{\mathrm{d}t} = 2 \times \left(\frac{16}{100}\right)$	M1	M1 for use of rates of change
	$= 0.32 \text{ or } \frac{8}{25}$	A1	
	25	[3]	

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	1	S
9 (i) $10\sqrt{2} \left(\frac{1}{\sqrt{2}} \mathbf{i} + \frac{1}{\sqrt{2}} \mathbf{j} \right) = 10\mathbf{i} + 10\mathbf{j}$	M1 A1	M1 for attempt at a correct direction vee A1 all correct M1 for valid attempt
(ii)		(2)
$(-4\mathbf{i} + 8\mathbf{j}) + (20\mathbf{i} + 20\mathbf{j}) = 16\mathbf{i} + 28\mathbf{j}$	M1	M1 for valid attempt
(11 · oj) · (201 · 20j) · 101 · 20j	A1	A1 all correct
		[2]
(iii) $(10i+10j)-(8i+6j)=2i+4j$	M1	M1 for attempt at vector difference
, , , = ,	A1	A1 condone negative
Col disulation of C		[2]
(iv) displacement of	M1	M1 for displacement and attempt to obtain
(19i + 34j) - (16i + 28j) = 3i + 6j	M1	M1 for displacement and attempt to obtain time
time =1330 hours	A1	A1 for correct time
(accept 1.5 hours)		
at $31\mathbf{i} + 43\mathbf{j}$	A1	A1 for correct position vector
		[3]
Alternative scheme:		
$(19\mathbf{i} + 34\mathbf{j}) + (8\mathbf{i} + 6\mathbf{j})t =$		M1 for attempt to equate like vectors
$(16\mathbf{i} + 28\mathbf{j}) + (10\mathbf{i} + 10\mathbf{j})t$		A marks as above
or equivalent		
10 (i) $m_{AB} = 0.75$	M1	M1 for attempt at m_{AB} and line AB
line $AB y - 0 = 0.75(x + 4)$	A1	
$m_{PQ} = -\frac{4}{3}$	M1	M1 for use of ' $m_1m_2 = -1$ ' and attempt at
\boldsymbol{J}		line PQ
line PQ $y-10 = -\frac{4}{3}(x-1)$	A1	
J	M1	M1 for attempt at solving simultaneous
intersection at $C(4,6)$	A1	equations
$Q(8.5\ 0)$	√B1	Ft on their line <i>PQ</i>
		[7]
(ii) $AC = 10, CQ = 7.5$	M1	M1 for attempt at lengths and area
Area = 37.5	A1	
		[2]

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	1	34
11 (i) $\ln s = n \ln t + \ln k$	M1, A1	M1 for attempt to take logs
ln t 1.6 2.7 3.4 4.2 4.6	M1	A1 for correct form
ln s 7.2 5.9 5 4 3.6	A1	M1 for attempt to take logs A1 for correct form M1 for attempt to plot correct graph A1 for a reasonable straight line
Plot ln s against ln t		A1 for a reasonable straight line
Tiov in a agminor inv	[4]	
(ii) grad $n = -1.2 (-1.4 \text{ to } -1.0)$	M1, A1	M1 for use of grad = n
Intercept = $\ln k$, leading to	M1, A1	M1 for use of intercept = $\ln k$
k = 7900 - 10000	[4]	
	[]	
(iii) when $t = 50$, $\ln t = 4.4$	M1	M1 for attempt to obtain s
leading to $s = 80 (72 - 92)$	A1	1
	[2]	
Alternative method		
(i) $\lg s = n \lg t + \lg k$		
lg t 0.7 1.2 1.5 1.8 2		
lg s 3.1 2.5 2.2 1.7 1.6		
		Same scheme applies



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					all.
12 EITHER					Dr.
(i) amplitude = 1		B1	[1]		E.
(#) married = 6= 10	0	B1	Γ1 1		.60
(ii) period = 6π , 18.	.8	ы	[1]		77
(r) 1	π 5π	M1		M1 for attempt to solve correctly	

12	FITHED
I Z	rii ork

((i)) $amplitude = 1$
٦	. ≖.	, ampirace

(iii)
$$\sin\left(\frac{x}{3}\right) = \frac{1}{2}, \ x = \frac{\pi}{2}, \frac{5\pi}{2}$$

(iv) Area under curve

$$\int_{\frac{\pi}{2}}^{\frac{5\pi}{2}} \left(1 + \sin\frac{x}{3}\right) dx = \left[x - 3\cos\frac{x}{3}\right]_{\frac{\pi}{2}}^{\frac{5\pi}{2}}$$

leading to $2\pi + 3\sqrt{3}$

Area of rectangle =
$$\left(\frac{5\pi}{2} - \frac{\pi}{2}\right) \times \frac{3}{2}$$

Shaded area = $3\sqrt{3} - \pi (2.05)$

Alternative solution: Shaded area

$$\int_{\frac{\pi}{2}}^{\frac{5\pi}{2}} \left(\sin \frac{x}{3} - 0.5 \right) dx = \left[-0.5x - 3\cos \frac{x}{3} \right]_{\frac{\pi}{2}}^{\frac{5\pi}{2}}$$

M1 A1, A1 [3]

M1

B1, B1

DM1

M1

A1

M1

M1

B1, B1

DM1, A1

[6]

M1 for attempt to solve correctly A1 for each (allow degrees here)

M1 for attempt to integrate

B1 for x, B1 for $-3\cos\frac{x}{3}$

DM1 for **correct** use of limits

M1 for attempt at rectangle plus subtraction – must be working in radians

M1 for subtraction (must be using radians) M1 for attempt to integrate

B1 for -0.5x, B1 for $-3\cos\frac{x}{3}$

DM1 for correct use of limits

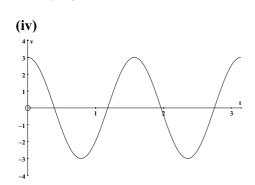
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			Call.
OR			andria
(i) $t = \frac{\pi}{\Omega}$	B1		Se
8	[1]		CON
$(ii) a = -4k \sin 4t$	M1, A1	M1 for attempt to differentiat	e

-	`	-
•	h	u

(i)	<i>t</i> —	π
(i)	ι –	8

(ii)
$$a = -4k \sin 4t$$

(iii)
$$12 = -4k \sin \frac{3\pi}{2}$$
 leading to $k = 3$



$$(\mathbf{v}) \quad s = \int_{0}^{\frac{\pi}{24}} 3\cos 4t. dt$$

$$= \left[\frac{3}{4}\sin 4t\right]_0^{\frac{\pi}{24}} \text{ leading to } \frac{3}{8}$$

M1, A1 [2]

M1

A1

[2]

B1 √B1

[2]

M1, $\sqrt{A1}$

DM1, A1 [4] M1 for attempt to substitute into their acceleration equation

B1 for correct shape

B1 ft on their value for k

M1 for attempt to integrate Ft on their value for k

DM1 for application of limits or equivalent