CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge Ordinary Level

MARK SCHEME for the October/November 2014 series

4037 ADDITIONAL MATHEMATICS

4037/12 Paper 1, maximum raw mark 80

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Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Page 2	Mark Scheme	Syllabus	Paper
	Cambridge O Level – October/November 2014	4037	12

1		$\frac{dy}{dx} = 2x - \frac{16}{x^2}$ When $\frac{dy}{dx} = 0$, $x = 2, y = 12$	M1 A1 DM1	for attempt to differentiate all correct for equating $\frac{dy}{dx}$ to zero and an attempt to solve for x . A1 for both, but no extra solutions
2	(a)	2	B1 B1	for correct shape for max value of 2, starting at (0, 2) and finishing at (180°, 2) for min value of –4
	(b) (i)	4	B1	must be positive
	(ii)	60° or $\frac{\pi}{3}$ or 1.05 rad	B1	
3	(i)	$y = 4(x+3)^{\frac{1}{2}}(+c)$ $10 = 4\left(9^{\frac{1}{2}}\right) + c$ $c = -2$ $y = 4(x+3)^{\frac{1}{2}} - 2$	M1, A1 M1	M1 for $(x+3)^{\frac{1}{2}}$, A1 for $4(x+3)^{\frac{1}{2}}$ for a correct attempt to find c , but must be from an attempt to integrate Allow A1 for $c = -2$
	(ii)	$6 = 4(x+3)^{\frac{1}{2}} - 2$ $x = 1$	A1 ft	ft for substitution into <i>their</i> equation to obtain <i>x</i> ; must have the first M1

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4	(i)	$5y^2 - 7y + 2 = 0$	B1, B1	B1 for 5, B1 for –7
	(ii)	(5y-2)(y-1)=0	M1	for solution of quadratic equation from (i)
		$y = \frac{2}{5}, x = \frac{\ln 0.4}{\ln 5}$	M1	for use of logarithms to solve equation of the type $5^x = k$
		x = -0.569	A1	must be evaluated to 3sf or better
		y=1, x=0	B1	
5	(i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = 3x^2 - \frac{1}{x}$	M1	for attempt to differentiate
		When $x = 1$, $y = 1$ and $\frac{dy}{dx} = 2$	B 1	for $y = 1$
		Tangent: $y - 1 = 2(x - 1)$	DM1	for attempt to find equation of tangent
		(y=2x-1)	A1	allow equation unsimplified
	(ii)	Mid-point (5, 9)	B1	for midpoint from given coordinates
		9 = 2(5) - 1	B1	for checking the mid-point lies on tangent
		Alternative Method: Tangent equation $y = 2x - 1$ Equation of line joining (-2, 16) and (12, 2)		
		y = -x + 14 Solve simultaneously $x = 5, y = 9$	B1	for a complete method to find the coordinates of the point of
		Mid-point (5, 9)	B1	intersection for midpoint from given coordinates
6	(i)	$(2+px)^6 = 64+192px+240p^2x^2$	B1	for $240p^2$ or $240p^2x^2$ or ${}^6C_2 \times 2^4 \times (px)^2$ or ${}^6C_2 \times 2^4 \times p^2$ or ${}^6C_2 \times 2^4 \times p^2x^2$
		$240p^2 = 60$	M1	for equating <i>their</i> term in x^2 to 60
		$p = \frac{1}{2}$	A1	and attempt to solve
	(ii)	$(3-x)(64+192px+240p^2x^2)$	B1 ft	ft for 192 <i>p</i> , 96 or 192 × <i>their p</i>
		Coefficient of x^2 is $180-192p$ = 84	M1 A1	for 180 – 192 <i>p</i>

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7	(i)	$\mathbf{A}^{-1} = \frac{1}{5ab} \begin{pmatrix} b & -2b \\ a & 3a \end{pmatrix}$	B1, B1	B1 for $\frac{1}{5ab}$, B1 for $\begin{pmatrix} b & -2b \\ a & 3a \end{pmatrix}$
	(ii)	$\mathbf{X} = \mathbf{B}\mathbf{A}^{-1}$	M1	for post-multiplication by inverse matrix
		$= \begin{pmatrix} -a & b \\ 2a & 2b \end{pmatrix} \begin{pmatrix} \frac{1}{5a} & -\frac{2}{5a} \\ \frac{1}{5b} & \frac{3}{5b} \end{pmatrix}$	DM1	for correct attempt at matrix multiplication, needs at least one term correct for their BA ⁻¹ (allow unsimplified)
		$= \begin{pmatrix} 0 & 1 \\ \frac{4}{5} & \frac{2}{5} \end{pmatrix}$	A1 A1	for each correct pair of elements, must be simplified
8	(i)	$\overrightarrow{AB} = \begin{pmatrix} 12\\16 \end{pmatrix}, \text{ at } P, \ x = -2 + \frac{1}{4}(12)$ so at P , $x = 1$	В1	for convincing argument for $x = 1$
		$y = 3 + \frac{1}{4}(16), y = 7$	B1	for $y = 7$
	(ii)	Gradient of $AB = \frac{16}{12}$, so perp gradient = $-\frac{3}{4}$	M1	for finding gradient of perpendicular
		Perp line: $y-7 = -\frac{3}{4}(x-1)$	M1	for equation of perpendicular through their <i>P</i>
		(3x + 4y = 31)	A1	Allow unsimplified
	(iii)	$Q\left(0,\frac{31}{4}\right)$	B1 ft	ft on their perpendicular line, may be implied
			M1	for any valid method of finding the area of the correct triangle, allow use of <i>their Q</i> ; must be in the form
		Area $AQB = 12.5$	A1	(0,q).

Page 5	Mark Scheme	Syllabus	Paper
	Cambridge O Level – October/November 2014	4037	12

9	(i)	$\log y = \log y$	$\log a + x1$	$\log b$				B1		for the statement, may be seen or
		x	2	2.5	3	3.5	4			implied in later work,
		lg y	1.27	1.47	1.67	1.87	2.07			
			2	2.5	3	3.5	4			
		lny	2.93	3.39	3.84	4.31	4.76			
		logy	. [-							
		logy						M1		for attempt to draw graph of x against $\log y$
							x	A2,1	,0	-1 each error in points plotted
	(ii)	Gradient $\lg b = 0.4$		= 0.92				DM	1	for attempt to find gradient and equate it to log <i>b</i> , dependent on M1
		b = 2.5 (allow 2.4 to 2.6)						A1		in (i)
		Intercept $\lg a = 0.4$		a=1.10)			DM	1	for attempt to equate <i>y</i> -intercept to log <i>a</i> or use <i>their</i> equation with <i>their</i> gradient and a point on the
		a=3 (all	ow 2.8 t	o 3.2)				A1		line, dependent on M1 in (i)
		Alternati Simultan points the used.	eous equ	ations	•	_		DM DM		for a pair of equations using points on the line, dependent on M1 in (i) for solution of these equations, dependent on M1 in (i)
		a = 3 (all $b = 2.5$ (a)			A1 A1		A1 for each

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10	(a) (i)	360	B1	
10	(ii)	60	B1	
	(iii)	36	B1	
	(b) (i)	${}^{8}C_{5} \times {}^{12}C_{5}$	B1, B1	B1 for each, allow unevaluated with no extra terms
		$56 \times 792 = 44352$	B1	Final answer must be evaluated and from multiplication
	(ii)	4 places are accounted for Gender no longer 'important'	M1	for realising that 4 places are accounted or that gender is no longer important
		Need ${}^{16}C_6 = 8008$	A1	for 8008
		Alternative Method		
		$\binom{6}{6} \binom{10}{6} + \binom{6}{6} \binom{10}{5} + \binom{6}{6} \binom{10}{6} \binom{10}{6} \binom{10}{6}$	M1	for at least 5 of the 7 cases, allow
		1+60+675+2400+3150+1512+210=8008	A1	unsimplified
11	(a)	$2\cos 3x - \frac{\cos 3x}{\sin 3x} = 0$	M1	for use of $\cot 3x = \frac{\cos 3x}{\sin 3x}$, may be
		$\cos 3x \left(2 - \frac{1}{\sin 3x}\right) = 0$		implied
		Leading to $\cos 3x = 0$, $3x = 90^{\circ}$, 270°	DM1	for attempt to solve $\cos 3x = 0$ correctly from correct factorisation
		$x = 30^{\circ}, 90^{\circ}$	A1	to obtain <i>x</i> A1 for both, no excess solutions in the range
		and $\sin 3x = \frac{1}{2}$, $3x = 30^{\circ}$, 150°	DM1	for attempt to solve $\sin 3x = \frac{1}{2}$
	(b)	$x = 10^{\circ}, 50^{\circ}$	A1	correctly to obtain <i>x</i> A1 for both, condone excess solutions
		$\cos\left(y + \frac{\pi}{2}\right) = -\frac{1}{2}$	M1	for dealing with $\sec\left(y + \frac{\pi}{2}\right)$
		$y + \frac{\pi}{2} = \frac{2\pi}{3}, \frac{4\pi}{3}$		correctly
		_	DM1	for correct order of operations, must not mix degrees and radians
		so $y = \frac{\pi}{6}, \frac{5\pi}{6}$ (0.524, 2.62)	A1, A1	

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12	(i)	$\overrightarrow{AQ} = \lambda \mathbf{b} - \mathbf{a}$	B1	
	(ii)	$\overrightarrow{BP} = \mu \mathbf{a} - \mathbf{b}$	B1	
	(iii)	$\overrightarrow{OR} = \mathbf{a} + \frac{1}{3} (\lambda \mathbf{b} - \mathbf{a}) \text{ or } \lambda \mathbf{b} - \frac{2}{3} (\lambda \mathbf{b} - \mathbf{a})$	M1	for $\mathbf{a} + \frac{1}{3}$ their (i)
		$=\frac{2}{3}\mathbf{a}+\frac{1}{3}\lambda\mathbf{b}$	A1	Allow unsimplified
	(iv)	$\overrightarrow{OR} = \mathbf{b} + \frac{7}{8} (\mu \mathbf{a} - \mathbf{b}) \text{ or } \mu \mathbf{a} - \frac{1}{8} (\mu \mathbf{a} - \mathbf{b})$	M1	for $\mathbf{b} + \frac{7}{8}$ their (ii)
		$=\frac{1}{8}\mathbf{b}+\frac{7}{8}\mu\mathbf{a}$	A1	Allow unsimplified
		$\frac{2}{3}\mathbf{a} + \frac{1}{3}\lambda\mathbf{b} = \frac{1}{8}\mathbf{b} + \frac{7}{8}\mu\mathbf{a}$	M1	for equating (iii) and (iv) and then
		$\frac{2}{3} = \frac{7}{8}\mu, \mu = \frac{16}{21}$ Allow 0.762	A1	equating like vectors
		$\frac{1}{3}\lambda = \frac{1}{8}, \lambda = \frac{3}{8} \text{Allow 0.375}$	A1	