

Cambridge O Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

ADDITIONAL MATHEMATICS

4037/12

Paper 1 May/June 2020

2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Blank pages are indicated.

Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series

$$u_n = a + (n-1)d$$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a+(n-1)d\}$$

Geometric series

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \ (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \left(|r| < 1 \right)$$

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

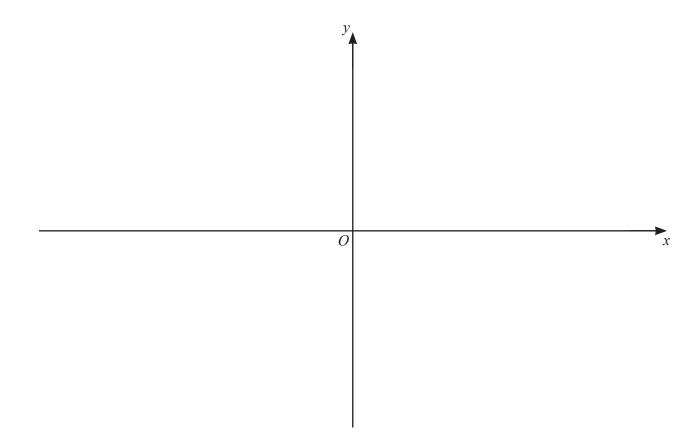
Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} bc \sin A$$

On the axes below, sketch the graph of y = |(x-2)(x+1)(x+2)| showing the coordinates of the points where the curve meets the axes. [3]



2 The volume, V, of a sphere of radius r is given by $V = \frac{4}{3}\pi r^3$.

The radius, r cm, of a sphere is increasing at the rate of 0.5 cms⁻¹. Find, in terms of π , the rate of change of the volume of the sphere when r = 0.25. [4]

3	(a)	Find the first 3 terms in the expansion of its simplest form.	$\left(4-\frac{x}{16}\right)^6$	in ascending powers of x .	Give each term in [3]
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(b) Hence find the term independent of
$$x$$
 in the expansion of $\left(4 - \frac{x}{16}\right)^6 \left(x - \frac{1}{x}\right)^2$. [3]

4	(a) ((i)	Find how many different 5-digit numbers can be formed using the digits 1, 2, 3, 5, 7 and 8 each digit may be used only once in any number.	8, if [1]
	(i	ii)	How many of the numbers found in part (i) are not divisible by 5?	[1]
	(ii	ii)	How many of the numbers found in part (i) are even and greater than 30 000?	[4]
	` /		number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times the number of combinations of n items taken 3 at a time is 6 times taken 3 at	
	(of n	items taken 2 at a time. Find the value of the constant <i>n</i> .	[4]

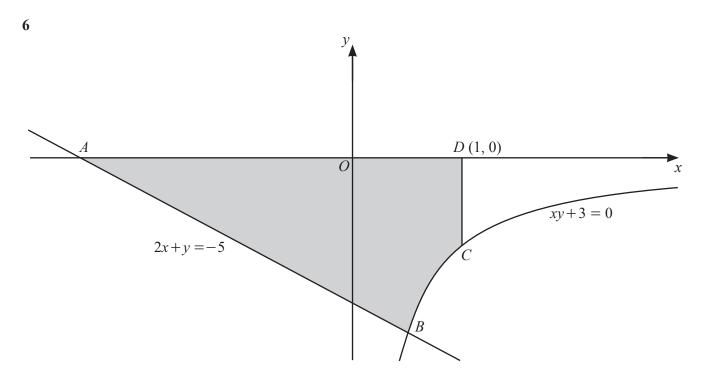
5
$$f: x \mapsto (2x+3)^2 \text{ for } x > 0$$

- (a) Find the range of f. [1]
- **(b)** Explain why f has an inverse. [1]

(c) Find f^{-1} . [3]

(d) State the domain of f^{-1} . [1]

(e) Given that $g: x \mapsto \ln(x+4)$ for x > 0, find the exact solution of fg(x) = 49. [3]



The diagram shows the straight line 2x+y=-5 and part of the curve xy+3=0. The straight line intersects the x-axis at the point A and intersects the curve at the point B. The point C lies on the curve. The point D has coordinates (1,0). The line CD is parallel to the y-axis.

(a) Find the coordinates of each of the points A and B. [3]

(b) Find the area of the shaded region, giving your answer in the form $p + \ln q$, where p and q are positive integers. [6]

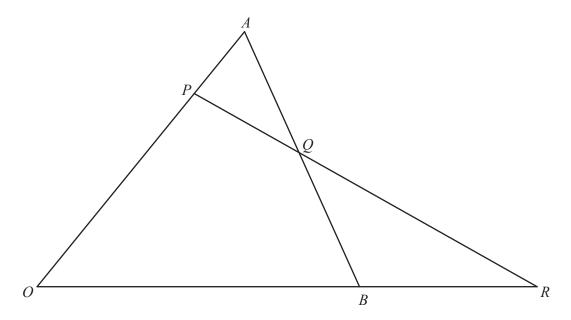
7 (a) Given that $y = (x^2 - 1)\sqrt{5x + 2}$, show that $\frac{dy}{dx} = \frac{Ax^2 + Bx + C}{2\sqrt{5x + 2}}$, where A, B and C are integers. [5]

(b) Find the coordinates of the stationary point of the curve $y = (x^2 - 1)\sqrt{5x + 2}$, for x > 0. Give each coordinate correct to 2 significant figures.

(c) Determine the nature of this stationary point.

[2]

8



The diagram shows a triangle OAB such that $\overrightarrow{OA} = \mathbf{a}$ and $\overrightarrow{OB} = \mathbf{b}$. The point P lies on OA such that $OP = \frac{3}{4}OA$. The point Q is the mid-point of AB. The lines OB and PQ are extended to meet at the point R. Find, in terms of \mathbf{a} and \mathbf{b} ,

(a)
$$\overrightarrow{AB}$$
, [1]

(b)
$$\overrightarrow{PQ}$$
. Give your answer in its simplest form. [3]

It is given that $n\overrightarrow{PQ} = \overrightarrow{QR}$ and $\overrightarrow{BR} = k\mathbf{b}$, where n and k are positive constants.

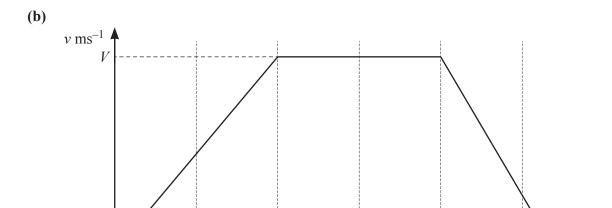
(c) Find \overrightarrow{QR} in terms of n, \mathbf{a} and \mathbf{b} .

[1]

(d) Find \overrightarrow{QR} in terms of k, \mathbf{a} and \mathbf{b} . [2]

(e) Hence find the value of n and of k. [3]

9	(a)	(a) A particle P moves in a straight line such that its displacement, x m, from a fixed point O at is given by $x = 10 \sin 2t - 5$.					
		(i)	Find the speed of P when $t = \pi$.	[1]			
		(ii)	Find the value of t for which P is first at rest.	[2]			
	,	(iii)	Find the acceleration of P when it is first at rest.	[2]			



10

5

The diagram shows the velocity–time graph for a particle Q travelling in a straight line with velocity $v\,\mathrm{ms}^{-1}$ at time $t\,\mathrm{s}$. The particle accelerates at 3.5 ms^{-2} for the first 10 s of its motion and then travels at constant velocity, $V\,\mathrm{ms}^{-1}$, for 10 s. The particle then decelerates at a constant rate and comes to rest. The distance travelled during the interval $20 \le t \le 25$ is $112.5\,\mathrm{m}$.

15

20

25

t s

(i) Find the value of V. [1]

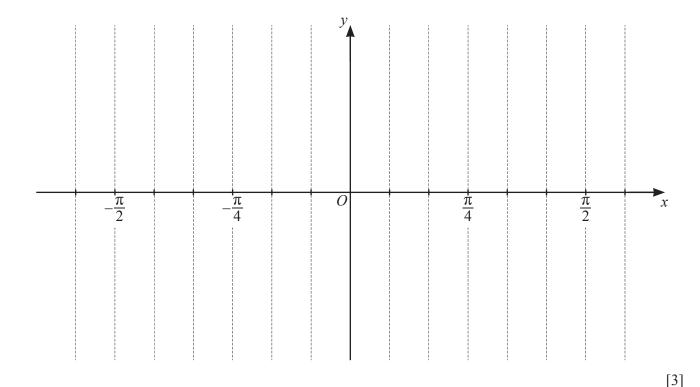
(ii) Find the velocity of Q when t = 25. [3]

(iii) Find the value of t when Q comes to rest. [3]

Question 10 is printed on the next page.

10 (a) Solve $\tan 3x = -1$ for $-\frac{\pi}{2} \le x \le \frac{\pi}{2}$ radians, giving your answers in terms of π . [4]

(b) Use your answers to part (a) to sketch the graph of $y = 4\tan 3x + 4$ for $-\frac{\pi}{2} \le x \le \frac{\pi}{2}$ radians on the axes below. Show the coordinates of the points where the curve meets the axes.



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