

# Cambridge O Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

#### ADDITIONAL MATHEMATICS

4037/22

Paper 2 October/November 2023

2 hours

You must answer on the question paper.

No additional materials are needed.

#### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

#### **INFORMATION**

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [ ].

This document has 16 pages. Any blank pages are indicated.

#### Mathematical Formulae

#### 1. ALGEBRA

Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ 

Arithmetic series  $u_n = a + (n-1)d$ 

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$$

Geometric series  $u_n = ar^{n-1}$ 

$$S_n = \frac{a(1-r^n)}{1-r} \ (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \ (|r| < 1)$$

### 2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for  $\triangle ABC$ 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

1 (a) A straight line passes through the points (4, 23) and (-8, 29). Find the point of intersection, P, of this line with the line y = 2x + 5. [5]

**(b)** Find the distance of *P* from the origin.

[2]

Find the non-zero value of k for which the line y = -2x - 6k - 1 is a tangent to the curve y = x(x + 2k). [5]

## 3 DO NOT USE A CALCULATOR IN THIS QUESTION.

A cylinder has base radius  $(2+\sqrt{3})$  m and volume  $\pi(16+9\sqrt{3})$  m<sup>3</sup>. Find the exact value of its height, giving your answer in its simplest form. [4]

4 Solve the following equations.

(a) 
$$\frac{(e^{x+1})^2}{\sqrt{e^x}} = 10$$
 [4]

**(b)** 
$$2\log_9 y - \log_9 (4y - 9) = \frac{1}{2}$$
 [5]

5 (a) Find the equation of the normal to the curve  $y = x^3 - 7x^2 + 12x - 5$  at the point (1, 1). [5]

(b) Find the x-coordinates of the two points where the normal cuts the curve again. Give your answers in the form  $x = a \pm \sqrt{b}$  where a and b are integers. [5]

6 Find the exact value of  $\int_2^3 \frac{(x+2)^2}{x} dx.$  [6]

7	A particle is travelling in a straight line. Its displacement, s metres, from the origin at time t seconds is given by $s = 1.5e^{2t} + 2e^{-2t} - t$ .											
	(a) Find expressions for the velocity, $v \text{ms}^{-1}$ , and acceleration, $a \text{ms}^{-2}$ , of the particle.	[3]										
	<b>(b)</b> Find the time, T seconds, when the particle is at rest.	[4]										
	(c) Find the acceleration of the particle at time <i>T</i> seconds.	[2]										
	-											

8 A curve has equation  $y = x \sin 2x$ .

(a) Find 
$$\frac{dy}{dx}$$
. [2]

**(b)** Find the equation of the tangent to the curve at  $x = \frac{\pi}{4}$ . [3]

(c) Use your answer to part (a) to find the exact value of  $\int_0^{\frac{\pi}{6}} 2x \cos 2x dx$ . [5]

9 (a) An arithmetic progression has twelve terms. The sum of the first three terms is -36 and the sum of the last three terms is 72. Find the first term and the common difference. [5]

(b) The first three terms of a geometric progression are 1, 1.2 and 1.44. Find the smallest value of n such that the sum of the first n terms is greater than 500. [5]

10 (a) By writing  $\cot x$  and  $\tan x$  in terms of  $\cos x$  and  $\sin x$ , show that

$$\frac{\sin x}{1 - \cot x} + \frac{\cos x}{1 - \tan x} = \sin x + \cos x.$$
 [5]

(b) Solve the equation  $9 \cot x + 3 \csc x = \tan x$ , for  $0^{\circ} < x < 360^{\circ}$ .

[5]

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