

HEST

# **GCSE 2012 Methods in Mathematics (Pilot)**

Specification

AT=

1=2x+3x

J926

(X-m)

Sino

 $(x + \alpha) = x$ 

LUMPUR

NGAPORE LONDON LUMPUR

GAPORE LONDON

NGAPORE LONDON

1. ctgx-2

KUALA

KUA

KUA

30

30

5

sing =

FAU O

Version 2

July 2013

± (q-c



(9.4)

= 3.1415

22

2,79

2x+3x

2,79

+41-141





Stat 24



#### A few good reasons to work with OCR

• You can enjoy the **freedom and excitement** of teaching qualifications which have been developed to help you inspire students of all abilities.

FOR

FLEXIBILI

AND

CHOICE

- We've built specifications with you in mind, using a clear and easy-to-understand format, making them straightforward for you to deliver.
- Our **clear and sensible assessment** approach means that exam papers and requirements are clearly presented and sensibly structured for you and your students.
- **Pathways for choice** we have the broadest range of qualifications and our GCSEs provide an ideal foundation for students to progress to more advanced studies and into the workplace.
- Working in partnership to support you together with teachers we've developed a range of practical help and support to save you time. We provide everything you need to teach our specifications with confidence and ensure your students get as much as possible from our qualifications.
- A personal service as well as providing you with lots of support resources, we're also here to help you with specialist advice, guidance and support for those times when you simply need a more individual service.

#### Here's how to contact us for specialist advice:

By phone: 0300 456 3142 By email: maths@ocr.org.uk By online: http://answers.ocr.org.uk

By fax: 01223 552627

By post: Customer Contact Centre, OCR, Progress House, Westwood Business Park, Coventry CV4 8JQ

**DON'T FORGET** – you can download a copy of this specification and all our support materials at **www.ocr.org.uk/maths** 

#### QN 500/7881/1

1.	Intro	oduction to GCSE Methods in Mathematics	3
	1.1	Overview of GCSE Methods in Mathematics	3
	1.2	Key aspects of GCSE Methods in Mathematics	4
	1.3	Guided learning hours	4
	1.4	Aims and learning outcomes	4
	1.5	Prior learning	4
2.	Con	tent of GCSE Methods in Mathematics	5
	2.1	Summary of GCSE Methods in Mathematics	5
	2.2	Content – Foundation Tier – (B391/01)	6
	2.3	Content – Foundation Tier – (B392/01)	18
	2.4	Content – Higher Tier – (B391/02)	27
	2.5	Content – Higher Tier – (B392/02)	42
3.	Ass	essment of GCSE Methods in Mathematics	54
	3.1	Overview of the assessment in GCSE Methods in Mathematics	54
	3.2	Tiers	54
	3.3	Assessment Objectives (AOs)	55
	3.4	Grading and awarding grades	56
	3.5	Grade descriptions	57
	3.6	Quality of Written Communication	58
4.	Sup	port for GCSE Methods in Mathematics	59
	4.1	Free resources available from the OCR website	59
	4.2	Training	59
	4.3	OCR support services	59
5.	Equ	ality and Inclusion in GCSE Methods in Mathematics	61
	5.1	Equality Act Information relating to GCSE Methods in Mathematics	61
	5.2	Arrangements for candidates with particular requirements	61
6.	Adm	ninistration of GCSE Methods in Mathematics	62
	6.1	Availability of assessment	62
	6.2	Certification rules	62
	6.3	Rules for re-taking a qualification	62
	6.4	Making entries	63
	6.5	Enquiries about results	63
	6.6	Prohibited qualifications and classification code	64
7.	Othe	er information about GCSE Methods in Mathematics	65
	7.1	Overlap with other qualifications	65
	7.2	Progression from this qualification	65
	7.3	Avoidance of bias	65
	7.4	Regulatory requirements	65
	7.5	Language	65
	7.6	Spiritual, moral, ethical, social, legislative, economic and cultural issues	66
	7.7	Sustainable development, health and safety considerations and European developments, consistent with international agreements	66
	7.8	Key Skills	67
	7.9	ICT	67
	7.10	) Citizenship	67
$\frown$	Verl	ical black lines indicate a significant change to the previous printed version.	

## **1.1** Overview of GCSE Methods in Mathematics

Unit B391/01 <i>Methods in</i> <i>Mathematics 1 (Foundation)</i>		Unit B391/02 <i>Methods in</i> <i>Mathematics 1 (Higher)</i>
Written paper		Written paper
1 hour	Or	1 hour 15 mins
60 marks	•••	60 marks
40% of the qualification		40% of the qualification
Calculator <b>not</b> permitted		Calculator <b>not</b> permitted

## AND

Mathematics 2 (Higher)
Written paper
2 hours
90 marks
60% of the qualification
Calculator permitted

(1



## **1.2 Key aspects of GCSE Methods in Mathematics**

The broad objectives in designing the scheme have been to:

- Provide access to a Grade C in mathematics to all candidates.
- Encourage an awareness of the links between different areas within mathematics.
- Foster the development of the ability to reason logically and develop mathematical arguments.
- Provide, together with GCSE Applications of Mathematics, the best possible mathematics qualification offer currently available in the UK.

#### **1.3 Guided learning hours**

GCSE Methods in Mathematics requires 120-140 guided learning hours in total.

### **1.4** Aims and learning outcomes

The aims of this specification are to:

- Develop knowledge, skills and understanding of mathematical methods, techniques and concepts.
- Make connections between different areas of mathematics.
- Select and apply mathematical methods in mathematical contexts.
- Reason mathematically, construct arguments and simple proofs, and make logical deductions and inferences.
- Develop and refine strategies for solving a range of mathematical problems.
- Communicate mathematical information in a variety of forms.

### **1.5 Prior learning**

Candidates entering this course should have achieved a general educational level equivalent to National Curriculum Level 3, or an Entry 3 at Entry Level within the National Qualifications Framework.

This specification comprises 2 mandatory units, Unit B391 and Unit B392, available at Foundation Tier and Higher Tier.

The content of Foundation Tier – Unit B391/01 and Unit B392/01 – is detailed in section 2.2 and 2.3.

The content of Higher Tier – Unit B391/02 and Unit B392/02 – is detailed in Section 2.4 and 2.5.

The content of GCSE Applications of Mathematics and Methods in Mathematics **together** cover the Key Stage 4 programme of study plus some additional content.

There is some overlap in content between GCSE Applications of Mathematics and GCSE Methods in Mathematics. There is some content that is additional to the programme of study that is unique to GCSE Methods in Mathematics.

This is indicated in the content (Section 2.2 to 2.5) as follows:

- the content from the programme of study that is found in **both** GCSE Applications of Mathematics and Methods in Mathematics is shaded in grey
- the content from the programme of study that is found only in GCSE Methods in Mathematics is in plain text
- the content that is additional to the programme of study and is unique to GCSE Methods in Mathematics is in *italics*.

At both Foundation Tier and Higher Tier, the content listed for Unit B391 will **not** be the focus of a question for Unit B392. However, knowledge of it is assumed and may form part of the assessment for Unit B392.

The content for the Foundation Tier is subsumed in the content for the Higher Tier.

F1A General problem solvi	Notes and Examples	
These skills should underpin a	and influence the learning experiences of all candidates in mathematics. They will be assess	ed within this specification.
1. Solve problems using	Candidates should be able to:	
mathematical skills	a. select and use suitable problem solving strategies and efficient techniques to solve numerical problems;	
	b. identify what further information may be required in order to pursue a particular line of enquiry and give reasons for following or rejecting particular approaches;	
	c. break down a complex calculation into simpler steps before attempting to solve it and justify their choice of methods;	
	d. use notation and symbols correctly and consistently within a problem;	
	e. use a range of strategies to create numerical representations of a problem and its solution; move from one form of representation to another in order to get different perspectives on the problem;	
	f. interpret and discuss numerical information presented in a variety of forms;	
	g. present and interpret solutions in the context of the original problem;	
	h. review and justify their choice of mathematical presentation;	
	i. understand the importance of counter-example and identify exceptional cases when solving problems;	
	j. show step-by-step deduction in solving a problem;	
	<ul> <li>k. recognise the importance of assumptions when deducing results; recognise the limitations of any assumptions that are made and the effect that varying those assumptions may have on the solution to a problem.</li> </ul>	

2



F1B Number		Notes and Examples
1. Add, subtract,	Candidates should be able to:	
multiply and divide any number	a. understand and use positive numbers and negative integers, both as positions and translations on a number line;	
	b. add, subtract, multiply and divide integers and then any number;	
	c. multiply or divide any number by powers of 10;	
	d. multiply or divide any positive number by a number between 0 and 1;	
	e. multiply and divide by a negative number;	
	f. recall all positive integer complements to 100;	
	g. recall all multiplication facts to 10 × 10, and use them to derive quickly the corresponding division facts;	
	h. develop a range of strategies for mental calculation; derive unknown facts from those they know;	
	i. add and subtract mentally numbers with up to two decimal places;	
	j. multiply and divide numbers with no more than <b>one</b> decimal place, using place value adjustments, factorisation and the commutative, associative, and distributive laws, where possible;	
	k. add and subtract integers and decimals understanding where to position the decimal point;	
	I. perform a calculation involving division by a decimal (up to <b>two</b> decimal places) by transforming it to a calculation involving division by an integer.	



F1B Number		Notes and Examples
2. Approximate to a specified or appropriate degree of accuracy	<ul> <li>Candidates should be able to:</li> <li>a. use their previous understanding of integers and place value to deal with arbitrarily large positive numbers;</li> <li>b. estimate answers to problems involving decimals;</li> <li>c. use a variety of checking procedures, including working the problem backwards, and considering whether a result is of the right order of magnitude;</li> <li>d. round to the nearest integer, to any number of decimal places, specified or appropriate.</li> </ul>	<ul> <li>Write 13 066 using words and to the nearest 100.</li> <li>Round 345.46 to the nearest integer, 1 decimal place, 2 significant figures.</li> <li>Know that 3.5 on a calculator</li> </ul>
	<ul> <li>and to any number of significant figures;</li> <li>e. give solutions in the context of the problem to an appropriate degree of accuracy, and recognise limitations on the accuracy of data and measurements.</li> </ul>	<ul> <li>means 3.50 in money context.</li> <li>Know that 3.666666667 on a calculator is a recurring decimal.</li> </ul>
3. Understand and use Venn diagrams and set notation to solve problems	Candidates should be able to: a. use 'two circle' Venn diagrams including in contexts other than number; b. understand and use set notation, and be able to solve related problems.	

F1C Hierarchy of operati	Notes and Examples	
1. Hierarchy of	Candidates should be able to:	• Calculate $\frac{(6+8)^2}{2.5^2-1.5^2}$
operations	a. use brackets and the hierarchy of operations.	

(8)



F1D Factors, multiples	Notes and Examples	
1. Factors, multiples and primes	<ul> <li>Candidates should be able to:</li> <li>a. use the concepts and vocabulary of factor (divisor), multiple, common factor, common multiple, highest common factor, least common multiple, prime number and prime factor decomposition;</li> <li>b. find the prime factor decomposition of positive integers;</li> <li>c. understand that the number of factors of a number can be derived from its prime factorisation.</li> </ul>	<ul> <li>Write down a number between 25 and 30 that is (i) a multiple of 7, (ii) a prime number and (iii) a factor of 104.</li> <li>Write 96 as a product of prime factors using indices.</li> </ul>



F1E Fractions, decimals a	Notes and Examples	
1. Calculate with fractions	Candidates should be able to:	(1) Multiplication by $\frac{1}{5}$ is equivalent
	a. calculate a given fraction of a given quantity, expressing the answer as a fraction;	
	b. express a given number as a fraction of another;	to division by 5
	c. add and subtract fractions by writing them with a common denominator;	
	d. convert a simple fraction to a decimal;	
	e. multiply and divide a fraction by an integer and by a unit fraction;	
	f. understand and use unit fractions as multiplicative inverses <sup>(1)</sup> ;	
	g. use efficient methods to calculate with fractions, including cancelling common factors before carrying out a calculation.	
2. Order rational numbers	Candidates should be able to:	
	a. order integers;	
	b. order fractions;	
	c. order decimals.	
3. Understand equivalent	Candidates should be able to:	
fractions	<ul> <li>a. understand and use equivalent fractions and simplify a fraction by cancelling all common factors.</li> </ul>	
4. Relationship between	Candidates should be able to:	137
fractions and decimals	a. use decimal notation and recognise that each terminating decimal is a fraction <sup>(1)</sup> ;	$(1) 0.137 = \frac{1000}{1000}$
	<ul> <li>b. distinguish between fractions with denominators that have only prime factors of 2 and 5 (which are represented by terminating decimals), and other fractions.</li> </ul>	

(10)



F1F Indices and surds		Notes and Examples
1. Indices in common use	Candidates should be able to:	
	a. use the terms 'square', 'positive square root', 'negative square root', 'cube' and 'cube root';	
	b. recall integer squares from $11 \times 11$ to $15 \times 15$ and the corresponding square roots;	
	c. recall the cubes of 2, 3, 4, 5 and 10.	
2. Use index notation	Candidates should be able to:	
	a. use index notation for squares, cubes and powers of 10;	
	b. use index notation for simple positive integer powers;	
	c. use index laws for multiplication and division of integer powers;	
	d. use index laws to simplify, and calculate the value of, numerical expressions involving multiplication and division of integer powers.	

F1G Algebra		Notes and Examples
1. Symbols and notation	Candidates should be able to:	
	a. distinguish the different roles played by letter symbols in algebra, using the correct notational conventions for multiplying or dividing by a given number;	(1) $5x + 1 = 16$ (2) $V = IR$
	<ul> <li>know that letter symbols represent definite unknown numbers in equations<sup>(1)</sup> and defined quantities or variables in formulae<sup>(2)</sup>;</li> </ul>	(3) $y = 2x$
	c. know that in functions, letter symbols define new expressions or quantities by referring to known quantities <sup>(3)</sup> .	

F1H Coordinates		Notes and Examples
1. Use the conventions for	Candidates should be able to:	
coordinates in the plane	a. use the conventions for coordinates in the plane; plot points in all four quadrants;	(1) Plot (3, 6) and (2, -4) on a grid.
	<ul> <li>b. understand that one coordinate identifies a point on a number line and two coordinates identify a point in a plane, using the terms '1D' and '2D';</li> </ul>	
	c. use axes and coordinates to specify points in all four quadrants;	
	d. locate points with given coordinates <sup>(1)</sup> .	

F1I Sequences and formu	lae	Notes and Examples
1. Understand and use formulae	Candidates should be able to: a. substitute numbers into formulae <sup>(1)</sup> .	<ol> <li>For area of a triangle or a parallelogram, area enclosed by a circle, volume of a prism.</li> </ol>

(12)



F1J Linear equations		Notes and Examples
<ol> <li>Manipulate algebraic expressions</li> </ol>	Candidates should be able to:	
	a. understand that the transformation of algebraic expressions obeys and generalises the rules of arithmetic <sup>(1)</sup> ;	(1) $a(b + c) = ab + ac$ (2) $x + 5 - 2x - 1 = 4 - x$ (3) $9x - 3 = 3(3x - 1)$ or $x^2 - 3x = x(x - 3)$
	b. manipulate algebraic expressions by collecting like terms <sup>(2)</sup> , by multiplying a single term over a bracket, and by taking out common factors <sup>(3)</sup> ;	
	c. use index laws in algebra.	
2. Set up and solve simple equations	Candidates should be able to:	
	a. set up simple equations <sup>(1)</sup> ;	(1) Richard is <i>x</i> years, Julie is twice as old and
	b. solve simple equations <sup>(2)</sup> by transforming both sides in the same way;	their combined age is 24 years. Write an equation to show this information
	c. solve linear equations, with integer coefficients, in which the unknown appears on either side or on both sides <sup>(3)</sup> of the equation.	(2) $11 - 4x = 2$ ; $3(2x + 1) = 8$ . (3) $2(1 - x) = 6(2 + x)$ .

F1K Functions and graphs		Notes and Examples
1. Recognise and plot equations that correspond to straight line graphs in the coordinate plane	Candidates should be able to:	
	a. plot graphs of functions in which <i>y</i> is given explicitly or implicitly in terms of <i>x</i> , where a table and/or axes are provided and where no table or axes are given;	
	b. read off values of x- or y-coordinates where two lines cross, where a line meets an axis, or where one coordinate is given.	
2. Use geometric information to complete diagrams on a coordinate grid	Candidates should be able to:	
	<ul> <li>a. use geometric information about shapes, or parallel or perpendicular lines, to complete diagrams on a coordinate grid.</li> </ul>	





F1L Angles and properties of shapes		Notes and Examples
1. Lines and angles	Candidates should be able to:	
	<ul> <li>a. recall and use properties of angles at a point, angles at a point on a straight line (including right angles), perpendicular lines, and vertically opposite angles;</li> </ul>	
	b. distinguish between acute, obtuse, reflex and right angles; estimate the size of an angle in degrees.	
2. Properties of shapes	Candidates should be able to:	
	a. use angle properties of equilateral, isosceles and right-angled triangles;	
	b. recall the essential properties and definitions of special types of quadrilateral, including square, rectangle, parallelogram, trapezium, kite and rhombus;	
	c. classify quadrilaterals by their geometric properties;	
	d. recall the definition of a circle and the meaning of related terms, including centre, radius, chord, diameter, circumference, tangent, arc, sector and segment;	
	e. understand that inscribed regular polygons can be constructed by equal division of a circle.	

(14)



F1M Transformations		Notes and Examples
1. Transformations of 2D shapes	Candidates should be able to:	
	a. recognise and visualise rotations <sup>(1)</sup> , reflections <sup>(2)</sup> and translations, including reflection symmetry of 2D and 3D shapes, and rotation symmetry of 2D shapes;	<ol> <li>Includes the order of rotation symmetry of a shape.</li> </ol>
	b. understand that rotations are specified by a centre and an (anticlockwise) angle;	(2) Includes reflection in <i>x</i> -axis or <i>y</i> -axis or
	c. understand that reflections are specified by a mirror line, at first using a line parallel to an axis, then a mirror line such as $y = x$ or $y = -x$ ;	(3) Includes the single transformation
	d. understand that translations are specified by a vector;	equivalent to a combination of transformations.
	e. transform triangles and other 2D shapes by translation, rotation and reflection and by combinations of these transformations <sup>(3)</sup> ;	<ul> <li>(4) Includes enlarging a shape on a grid and enlarging a shape by a scale</li> </ul>
	f. recognise that these transformations preserve length and angle, and hence that any figure is congruent to its image under any of these transformations;	factor given the centre of enlargement.
	g. understand from this that any two circles and any two squares are mathematically similar, while, in general, two rectangles are not;	
	h. understand that enlargements <sup>(4)</sup> are specified by a centre;	
	i. describe and transform enlargements of shapes using positive scale factors;	
	j. distinguish properties that are preserved under particular transformations;	
	k. identify the scale factor of an enlargement as the ratio of the lengths of any two corresponding line segments and apply this to triangles;	
	I. understand and use vector notation for translations.	

(15)

F1N Area and volume		Notes and Examples
1. Perimeter, area and volume	Candidates should be able to:	
	a. find areas of rectangles, recalling the formula, understanding the connection to counting squares and how it extends this approach;	
	b. find the area of a parallelogram and a triangle;	
	c. work out the surface area of simple 3D shapes composed of triangles and rectangles;	
	d. calculate perimeters and areas of shapes made from triangles and rectangles;	
	e. find volumes of cuboids, recalling the formula and understanding the connection to counting cubes and how it extends this approach.	



F1O Probability		Notes and Examples
1. Probability	Candidates should be able to:	
	a. understand and use the vocabulary of probability and the probability scale <sup>(1)</sup> ;	(1) Use impossible, certain, evens,
	b. understand and use theoretical models of probabilities including the model of equally likely outcomes <sup>(2)</sup> ;	likely, unlikely. (2) Associate 0, 0⋅5, 1 with
	c. understand and use estimates of probability from relative frequency;	impossible, evens and certain and position events on a
	d. use sample spaces for situations where outcomes are single events and for situations where outcomes are two successive events <sup>(3)</sup> ;	<ul> <li>(3) Use a sample space or list combinations systematically e.g for 2 dice.</li> </ul>
	e. identify different mutually-exclusive and exhaustive outcomes and know that the sum of the probabilities of these outcomes is 1 <sup>(4)</sup> ;	
	f. understand that if they repeat an experiment, they may (and usually will) get different outcomes, and that increasing sample size generally leads to better estimates of probability <sup>(5)</sup> ;	(4) Given the P(A) find P(not A), and given P(A) and P(B) find P(not A or B).
	g. compare experimental data to theoretical probabilities, and make informal inferences about the validity of the model giving rise to the theoretical probabilities;	(5) Compare the dice experiment results to theoretical and
	h. understand and use set notation to describe events and compound events;	comment on possible blas.
	<i>i.</i> use Venn diagrams to represent the number of possibilities and hence find probabilities.	

## 2.3 Content – Foundation Tier – Unit B392/01

F2A General problem solvir	ng skills	Notes and Examples
These skills should underpin	and influence the learning experiences of all candidates in mathematics. They are asses	sed within this specification.
1. Solve problems using mathematical skills	Candidates should be able to:	
	a. select and use suitable problem solving strategies and efficient techniques to solve numerical problems;	
	b. identify what further information may be required in order to pursue a particular line of enquiry and give reasons for following or rejecting particular approaches;	
	c. break down a complex calculation into simpler steps before attempting to solve it and justify their choice of methods;	
	d. use notation and symbols correctly and consistently within a problem;	
	e. use a range of strategies to create numerical representations of a problem and its solution; move from one form of representation to another in order to get different perspectives on the problem;	
	f. interpret and discuss numerical information presented in a variety of forms;	
	g. present and interpret solutions in the context of the original problem;	
	h. review and justify their choice of mathematical presentation;	
	i. understand the importance of counter-example and identify exceptional cases when solving problems;	
	j. show step-by-step deduction in solving a problem;	
	k. recognise the importance of assumptions when deducing results; recognise the limitations of any assumptions that are made and the effect that varying those assumptions may have on the solution to a problem.	

(18)



F2B Number		Notes and Examples
1. Approximate to a specified or appropriate degree of accuracy	Candidates should be able to:	
	a. use their previous understanding of integers and place value to deal with arbitrarily large positive numbers;	
	b. use a variety of checking procedures, including working the problem backwards, and considering whether a result is of the right order of magnitude;	
	<ul> <li>c. round to the nearest integer, to any number of decimal places, specified or appropriate, and to any number of significant figures;</li> </ul>	
	d. give solutions in the context of the problem to an appropriate degree of accuracy, interpreting the solution shown on a calculator display, and recognising limitations on the accuracy of data and measurements;	
	e. understand the calculator display, knowing when to interpret the display, when the display has been rounded by the calculator, and not to round during the intermediate steps of a calculation.	
2. Use calculators effectively and efficiently	Candidates should be able to:	
	a. use calculators effectively and efficiently <sup>(1)</sup> ;	(1) Calculate $1 \cdot 6^3$ , $\sqrt{7 \cdot 29}$
	b. know how to enter complex calculations and use function keys for reciprocals, squares and powers <sup>(2)</sup> ;	(2) $\sqrt[3]{6 \cdot 1^2 - 0 \cdot 81}$ (3) When using money interpret a
	c. enter a range of calculations <sup>(3)</sup> .	calculator display of 2.6 as £2.60.

F2C Hierarchy of operation	ons	Notes and Examples
1. Hierarchy of operations	Candidates should be able to:	(0,0)2
	a. understand and use number operations and the relationships between them, including inverse operations.	• Calculate $\frac{(6+8)^2}{2 \cdot 5^2 - 1 \cdot 5^2}$

(19)



F2D Ratio		Notes and Examples
1. Use ratio notation, including reduction to its simplest form and its various links to fraction notation	Candidates should be able to:	Write the ratio 24:60 in its simplest form.
	a. use ratio notation, including reduction to its simplest form expressed as 1: <i>n</i> or <i>n</i> :1 or <i>m</i> : <i>n</i> ;	
	b. know and use the links between ratio notation and fraction notation.	
2. Divide a quantity in a	Candidates should be able to:	<ul> <li>(1) Divide £120 in the ratio 3:7.</li> <li>(2) 8 calculators cost £59.52. How much do 3 calculators cost?</li> </ul>
given ratio	a. divide a quantity in a given ratio <sup>(1)</sup> ;	
	b. determine the original quantity by knowing the size of one part of the divided quantity;	
	c. solve word problems about ratio, including using informal strategies and the unitary method of solution <sup>(2)</sup> .	



F2E Fractions, decimals a	nd percentages	Notes and Examples
1. Calculate with fractions	Candidates should be able to:	
	a. convert a simple fraction to a decimal;	
	b. multiply and divide a fraction by an integer and by a unit fraction;	
	c. understand and use unit fractions as multiplicative inverses;	
	d. use efficient methods to calculate with fractions, including cancelling common factors before carrying out a calculation;	
	e. recognise that, in some cases, only a fraction can express the exact answer;	
	f. understand 'reciprocal' as multiplicative inverse and know that any non-zero number multiplied by its reciprocal is 1 (and that zero has no reciprocal, since division by zero is not defined).	
2. Relationship between	Candidates should be able to:	
fractions and decimals	a. recognise that recurring decimals are exact fractions;	
	b. know that some exact fractions are recurring decimals;	
	c. convert a recurring decimal to a fraction.	
3. Understand percentage	Candidates should be able to:	
	a. understand that 'percentage' means 'number of parts per 100' and use this to compare proportions;	
	b. know the fraction-to-percentage (or decimal) conversion of familiar simple fractions.	





F2E Fractions, decimals an	d percentages	Notes and Examples
4. Interpret fractions, decimals and percentages as operators	Candidates should be able to:	
	a. interpret percentage as the operator 'so many hundredths of';	(1) A 15% decrease in Y is calculated as 0.85 × Y.
	b. convert between fractions, decimals and percentages;	
	c. understand the multiplicative nature of percentages as operators;	
	d. use multipliers for percentage change <sup>(1)</sup> .	
5. Proportional change	Candidates should be able to:	
	a. find proportional change using fractions, decimals and percentages;	
	b. understand and use direct proportion.	

F2F Algebra		Notes and Examples
1. Symbols and notation	Candidates should be able to:	(1) $5x + 1 = 16$ (2) $V = IR$ (3) $y = 2x$
	a. distinguish the different roles played by letter symbols in algebra, using the correct notational conventions for multiplying or dividing by a given number;	
	b. know that letter symbols represent definite unknown numbers in equations <sup>(1)</sup> and defined quantities or variables in formulae <sup>(2)</sup> ;	
	c. know that in functions, letter symbols define new expressions or quantities by referring to known quantities <sup>(3)</sup> ;	
	d. understand the concept of an inequality.	
2. Proof	Candidates should be able to:	
	a. use algebra to support and construct arguments.	

F2G Coordinates		Notes and Examples
1. Use the conventions for coordinates in the plane	Candidates should be able to:	
	a. given the coordinates of the points A and B, find coordinates of the midpoint of the line segment AB;	
	b. given the coordinates of the points A and B, find the length of AB.	

F2H Sequences and formu	lae	Notes and Examples
1. Generate terms of a	Candidates should be able to:	
sequence using term- to-term and position-to-	a. generate terms of a sequence using term-to-term and position-to-term <sup>(1)</sup> definitions of the sequence;	(1) Write down the first two terms of the sequence whose $n$ th term is $3n - 5$ .
sequence	b. generate common integer sequences (including sequences of odd or even integers, squared integers, powers of 2, powers of 10, triangular numbers).	
2. Form linear expressions	Candidates should be able to:	Foundation also includes simple sequence of odd or even numbers, squared integers and sequences derived from diagrams.
to describe the <i>n</i> th term of an arithmetic sequence	a. use linear expressions to describe the <i>n</i> th term of an arithmetic sequence, justifying its form by referring to the activity or context from which it was generated.	
3. Derive a formula,	Candidates should be able to:	
substitute numbers into a formula and change the subject of a formula	a. derive a formula for a given sequence;	<ul> <li>(1) Wage earned = hours worked × rate per hour.</li> <li>(2) Find <i>r</i> given that C = πr, find x given y = mx + c.</li> </ul>
	b. derive a formula in a physical or everyday context <sup>(1)</sup> ;	
	c. substitute numbers into a formula;	
	d. change the subject of a formula <sup>(2)</sup> .	



F2I Linear equations		Notes and Examples
<ol> <li>Set up and solve simple equations and inequalities</li> </ol>	Candidates should be able to:	
	a. solve linear equations that require prior simplification of brackets, including those that have negative signs occurring anywhere in the equation, and those with a negative solution;	
	<ul> <li>b. understand that the point of intersection of two different lines in the same two variables that simultaneously describe a real situation is the solution to the simultaneous equations represented by the lines;</li> </ul>	
	c. set up simple inequalities;	
	d. solve simple inequalities by transforming both sides in the same way.	

F2J Functions and graph	IS	Notes and Examples
1. Solve quadratic	Candidates should be able to:	
equations using a graph	a. understand that approximate solutions of quadratic equations can be found from their graphs;	
	b. draw graphs of quadratic equations and find their approximate solution.	
2. Recognise and	Candidates should be able to:	
use equivalence in numerical, algebraic and graphical representations	a. recognise that straight line graphs can be represented by equations, and vice versa;	
	b. interpret numerical data in graphical form.	

(24)



F2K Pythagoras in 2D		Notes and Examples
1. Use Pythagoras' theorem	Candidates should be able to:	
	a. understand, recall and use Pythagoras' theorem to solve simple cases in 2D.	

F2L Angles and properties of shapes		Notes and Examples
1. Lines and angles	Candidates should be able to:	
	a. distinguish between lines and line segments;	
	b. use parallel lines, alternate angles and corresponding angles;	
	c. understand the consequent properties of parallel and intersecting lines, triangles (including a proof that the angle sum of a triangle is 180°) and parallelograms;	
	d. understand a proof that an exterior angle of a triangle is equal to the sum of the interior angles at the other two vertices;	
	e. explain why the angle sum of a quadrilateral is 360°.	
2. Angles and polygons	Candidates should be able to:	
	a. calculate and use the sums of the interior and exterior angles of polygons;	
	b. calculate and use the angles of regular polygons;	
	c. solve problems in the context of tiling patterns and tessellations.	

F2M Transformations		Notes and Examples
1. Congruence and similarity	Candidates should be able to:	
	a. understand congruence;	
	b. understand similarity of plane figures including the relationship between lengths and angles.	

(25)



F2N Area and volume		Notes and Examples
1. Perimeter, area (including circles), and volume	Candidates should be able to:	
	a. solve problems involving simple areas;	<ol> <li>Could involve semicircles, and inverse problems e.g. find the diameter if the circumference is 60cm.</li> <li>Could involve inverse calculations find the length of an edge given the volume and two other edges.</li> </ol>
	b. find circumferences of circles <sup>(1)</sup> and areas enclosed by circles, recalling relevant formulae;	
	c. find volumes of cuboids <sup>(2)</sup> , recalling the formula and understanding the connection to counting cubes and how it extends this approach;	
	d. calculate volumes of right prisms and of shapes made from cubes and cuboids.	



# 2.4 Content – Higher Tier – Unit B391/02

H1A General problem solvi	ng skills	Notes and Examples
These skills should underpin and influence the learning experiences of all candidates in mathematics. They will be asse		essed within this specification.
1. Solve problems using mathematical skills	Candidates should be able to:	
	a. select and use suitable problem solving strategies and efficient techniques to solve numerical problems;	
	b. identify what further information may be required in order to pursue a particular line of enquiry and give reasons for following or rejecting particular approaches;	
	c. break down a complex calculation into simpler steps before attempting to solve it and justify their choice of methods;	
	d. use notation and symbols correctly and consistently within a problem;	
	e. use a range of strategies to create numerical representations of a problem and its solution; move from one form of representation to another in order to get different perspectives on the problem;	
	f. interpret and discuss numerical information presented in a variety of forms;	
	g. present and interpret solutions in the context of the original problem;	
	h. review and justify their choice of mathematical presentation;	
	i. understand the importance of counter-example and identify exceptional cases when solving problems;	
	j. show step-by-step deduction in solving a problem;	
	k. recognise the importance of assumptions when deducing results; recognise the limitations of any assumptions that are made and the effect that varying those assumptions may have on the solution to a problem.	

(27)

H1B Number		Notes and Examples
1. Add, subtract, multiply and divide any number	Candidates should be able to:	
	a. understand and use positive numbers and negative integers, both as positions and translations on a number line;	
	b. add, subtract, multiply and divide integers and then any number;	
	c. multiply or divide any number by powers of 10;	
	d. multiply or divide any positive number by a number between 0 and 1;	
	e. multiply and divide by a negative number;	
	f. recall all positive integer complements to 100;	
	<ul> <li>g. recall all multiplication facts to 10 × 10, and use them to derive quickly the corresponding division facts;</li> </ul>	
	h. develop a range of strategies for mental calculation; derive unknown facts from those they know;	
	i. add and subtract mentally numbers with up to two decimal places;	
	j. multiply and divide numbers with no more than <b>one</b> decimal place, using place value adjustments, factorisation and the commutative, associative, and distributive laws, where possible;	
	k. add and subtract integers and decimals understanding where to position the decimal point;	
	I. perform a calculation involving division by a decimal (up to <b>two</b> decimal places) by transforming it to a calculation involving division by an integer.	

(28)



H1B Number		Notes and Examples
<ol> <li>Approximate to a specified or appropriate degree of accuracy</li> </ol>	Candidates should be able to:	
	a. use their previous understanding of integers and place value to deal with arbitrarily large positive numbers;	Write 13 066 using words and to the nearest 100.
	b. estimate answers to problems involving decimals;	• Round 345 46 to the nearest
	c. use a variety of checking procedures, including working the problem backwards, and considering whether a result is of the right order of magnitude;	<ul> <li>Integer, 1 decimal place, 2 significant figures.</li> <li>Know that 3.5 on a calculator means 3.50 in money context.</li> <li>Know that 3.666666667 on a calculator is a recurring decimal.</li> </ul>
	d. round to the nearest integer, to any number of decimal places, specified or appropriate, and to any number of significant figures;	
	e. give solutions in the context of the problem to an appropriate degree of accuracy and recognise limitations on the accuracy of data and measurements.	
3. Understand and use Venn diagrams and set notation to solve problems	Candidates should be able to:	
	a. use 'two circle' or 'three circle' Venn diagrams including in contexts other than number;	
	b. understand and use set notation, and be able to solve related problems.	

H1C Hierarchy of operations		Notes and Examples
1. Hierarchy of operations	Candidates should be able to:	$(0 \cdot 0)^2$
	a. use brackets and the hierarchy of operations.	• Calculate $\frac{(6+8)^2}{2.5^2 - 1 \times 5^2}$

(29)



H1D Factors, multiples and p	primes	Notes and Examples
1. Factors, multiples and primes	Candidates should be able to:	<ul> <li>Write down a number between 25 and 30 that is         <ul> <li>(i) a multiple of 7,</li> <li>(ii) a prime number and</li> </ul> </li> </ul>
	a. use the concepts and vocabulary of factor (divisor), multiple, common factor, common multiple, highest common factor, least common multiple, prime number and prime factor decomposition;	
	b. find the prime factor decomposition of positive integers;	
	c. understand that the number of factors of a number can be derived from its prime factorisation.	<ul><li>(iii) a factor of 104.</li><li>Write 96 as a product of prime factors using indices.</li></ul>

H1E Fractions, decimals and percentages		Notes and Examples
1. Calculate with fractions	Candidates should be able to:	
	a. calculate a given fraction of a given quantity, expressing the answer as a fraction;	(1) Multiplication by $\frac{1}{5}$ is equivalent to
	b. express a given number as a fraction of another;	division by 5.
	c. add and subtract fractions by writing them with a common denominator;	
	d. perform short division to convert a simple fraction to a decimal;	
	e. multiply and divide a fraction by an integer and by a unit fraction;	
	f. understand and use unit fractions as multiplicative inverses <sup>(1)</sup> ;	
	g. use efficient methods to calculate with fractions, including cancelling common factors before carrying out a calculation.	

(30)

H1E Fractions, decimals and percentages		Notes and Examples
2. Order rational numbers	Candidates should be able to:	
	a. order integers;	
	b. order fractions;	
	c. order decimals.	
3. Understand equivalent	Candidates should be able to:	
fractions	a. understand and use equivalent fractions and simplify a fraction by cancelling all common factors.	
4. Relationship between fractions and decimals	Candidates should be able to:	
	a. use decimal notation and recognise that each terminating decimal is a fraction <sup>(1)</sup> ;	(1) $0 \cdot 137 = \frac{137}{1000}$
	b. distinguish between fractions with denominators that have only prime factors of 2 and 5 (which are represented by terminating decimals), and other fractions <sup>(2)</sup> .	(2) Convert $0.\dot{3}$ to a fraction.

H1F Indices and surds		Notes and Examples
1. Indices in common use	Candidates should be able to:	
	a. use the terms 'square', 'positive square root', 'negative square root', 'cube' and 'cube root';	
	b. recall integer squares from $11 \times 11$ to $15 \times 15$ and the corresponding square roots;	
	c. recall the cubes of 2, 3, 4, 5 and 10.	
2. Index notation	Candidates should be able to:	
	a. use index notation for squares, cubes and powers of 10;	
	b. use index notation for simple integer powers;	
	c. use index laws for multiplication and division of integer powers;	
	d. use index laws to simplify, and calculate the value of, numerical expressions involving multiplication and division of integer, fractional and negative powers;	
	e. know that $n^0$ = 1; understand that the inverse operation of raising a positive number to power <i>n</i> is raising the result of this operation to power 1/ <i>n</i> ;	
	f. know that $n^{-1} = 1/n$ (undefined for $n = 0$ ), and that $n^{\frac{1}{2}} = \sqrt{n}$ and $n^{\frac{1}{3}} = \sqrt[3]{n}$ for any positive number <i>n</i> .	
3. Use surds in exact calculations	Candidates should be able to:	
	a. use surds and $\pi$ in exact calculations without a calculator;	$(1)\frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$
	b. rationalise a denominator <sup>(1)</sup> .	

(32)



H1G Standard index form		Notes and Examples
1. Standard index form	Candidates should be able to:	
	a. use standard index form expressed in conventional notation <sup>(1)</sup> ;	(1) $2 \cdot 4 \times 10^7 \times 5 \times 10^3 = 1 \cdot 2 \times 10^{11}$
	b. calculate with standard index form <sup>(2)</sup> ;	OR $(2.4 \times 10^7) \div (5 \times 10^3) = 4.8$ × 10 <sup>3</sup>
	c. convert between ordinary and standard index form representations, converting to standard index form to make sensible estimates for calculations involving multiplication and/or division.	<ul> <li>(2) Write 165 000 in standard form;</li> <li>write 6.32 × 10<sup>-3</sup> as an ordinary number.</li> </ul>



H1H Algebra		Notes and Examples
1. Symbols and notation	Candidates should be able to:	
	a. distinguish the different roles played by letter symbols in algebra, using the correct notational conventions for multiplying or dividing by a given number;	(1) $5x + 1 = 16$ (2) $V = IR$
	b. know that letter symbols represent definite unknown numbers in equations <sup>(1)</sup> and defined quantities or variables in formulae <sup>(2)</sup> ;	(3) $y = 2x$
	c. know that in functions, letter symbols define new expressions or quantities by referring to known quantities <sup>(3)</sup> .	
2. Algebraic terminology	Candidates should be able to:	
	a. distinguish in meaning between the words 'equation', 'formula' and 'expression'.	

H1I Coordinates		Notes and Examples
1. Use the conventions for coordinates in the plane	Candidates should be able to:	
	a. use the conventions for coordinates in the plane; plot points in all four quadrants;	(1) Plot (3, 6) and (2, -4) on a grid.
	<ul> <li>b. understand that <b>one</b> coordinate identifies a point on a number line, <b>two</b> coordinates identify a point in a plane and <b>three</b> coordinates identify a point in space, using the terms '1D', '2D' and '3D';</li> </ul>	
	c. use axes and coordinates to specify points in all four quadrants;	
	d. locate points with given coordinates <sup>(1)</sup> .	
H1J Sequences and formu	lae	Notes and Examples
-------------------------	---	--------------------
1. Use formulae	Candidates should be able to: a. substitute numbers into formulae.	

H1K Linear equations		Notes and Examples
1. Manipulate algebraic expressions	Candidates should be able to:	(1) $a(b + c) = ab + bc$ (2) $x + 5 - 2x - 1 = 4 - x$ (3) $9x - 3 = 3 (3x - 1)$ or $x^2 - 3x = x(x - 3)$
	a. understand that the transformation of algebraic expressions obeys and generalises the rules of arithmetic <sup>(1)</sup> ;	
	<ul> <li>b. manipulate algebraic expressions by collecting like terms<sup>(2)</sup>, by multiplying a single term over a bracket, and by taking out common factors<sup>(3)</sup>;</li> </ul>	
	c. use index laws in algebra.	
2. Set up and solve simple	Candidates should be able to:	<ul> <li>(1) Richard is <i>x</i> years, Julie is twice as old and their combined age is 24 years. Write an equation to show this information.</li> <li>(2) 11 - 4x = 2; 3(2x + 1) = 8.</li> <li>(3) 2(1 - x) = 6(2 + x)</li> </ul>
equations	a. set up simple equations <sup>(1)</sup> ;	
	b. solve simple equations <sup>(2)</sup> by transforming both sides in the same way;	
	c. solve linear equations, with integer coefficients, in which the unknown appears on either side or on both sides of the equation <sup>(3)</sup> .	





H1L Functions and graph	s	Notes and Examples
<ol> <li>Recognise and plot equations that correspond to straight line graphs in the coordinate plane, including finding gradients</li> </ol>	Candidates should be able to:	<ul> <li>(1) Know that the lines represented by y = 5x and y = 3 + 5x are parallel, each having gradient 5.</li> <li>(2) Know that the line with equation y = <sup>-x</sup>/<sub>5</sub> is perpendicular to these lines and has gradient - <sup>1</sup>/<sub>5</sub>.</li> </ul>
	a. recognise (when values are given for $m$ and $c$ ) that equations of the form $y = mx + c$ correspond to straight line graphs in the coordinate plane;	
	b. find the gradient of lines given by equations of the form $y = mx + c$ (when values are given for <i>m</i> and <i>c</i> ); investigate the gradients of parallel lines <sup>(1)</sup> ;	
	c. plot graphs of functions in which <i>y</i> is given explicitly in terms of <i>x</i> , or implicitly, where no table or axes are given;	
	d. use $y = mx + c$ and understand the relationship between gradients of parallel and perpendicular lines <sup>(2)</sup> .	
2. Use geometric information to complete diagrams on a coordinate grid	Candidates should be able to:	
	a. use geometric information about shapes, or parallel or perpendicular lines, to complete diagrams on a coordinate grid.	

(36)



H1M Angles and properties of shapes		Notes and Examples
1. Lines and angles	Candidates should be able to:	
	a. recall and use properties of angles at a point, angles at a point on a straight line (including right angles), perpendicular lines, and opposite angles;	
	b. distinguish between acute, obtuse, reflex and right angles; estimate the size of an angle in degrees.	
2. Properties of shapes	Candidates should be able to:	
	a. use angle properties of equilateral, isosceles and right-angled triangles;	
	<ul> <li>b. recall the essential properties and definitions of special types of quadrilateral, including square, rectangle, parallelogram, trapezium, kite and rhombus;</li> </ul>	
	c. classify quadrilaterals by their geometric properties;	
	d. understand that inscribed regular polygons can be constructed by equal division of a circle;	
	e. distinguish between centre, radius, chord, diameter, circumference, tangent, arc, sector and segment.	





H1M Angles and propertie	es of shapes	Notes and Examples
3. Understand, prove and use circle theorems	Candidates should be able to:	
	a. understand and use the fact that the tangent at any point on a circle is perpendicular to the radius at that point;	
	b. understand and use the fact that tangents meeting at an external point are equal in length;	
	c. explain why the perpendicular from the centre to a chord bisects that chord;	
	d. prove and use these facts:	
	<ul> <li>i. the angle subtended by an arc at the centre of a circle is twice the angle subtended at any point on the circumference;</li> <li>ii. the angle subtended at the circumference in a semicircle is a right angle;</li> <li>iii. angles in the same segment are equal;</li> <li>iv. the alternate segment theorem;</li> <li>v. the opposite angles of a cyclic quadrilateral sum to 180°.</li> </ul>	



H1N Transformations		Notes and Examples
1. Transformations of 2D	Candidates should be able to:	
shapes	a. recognise and visualise rotations <sup>(1)</sup> , reflections <sup>(2)</sup> and translations, including reflection symmetry of 2D and 3D shapes, and rotation symmetry of 2D shapes;	<ol> <li>Includes the order of rotation symmetry of a shape.</li> </ol>
	b. understand that rotations are specified by a centre and an (anticlockwise) angle;	(2) Includes reflection in x-axis or
	c. understand that reflections are specified by a mirror line, at first using a line parallel to an axis, then a mirror line such as $y = x$ or $y = -x$ ;	<ul> <li>y-axis or in a given mirror line.</li> <li>(3) Includes the single transformation equivalent to a combination of transformations.</li> </ul>
	d. understand that translations are specified by a vector;	
	e. transform triangles and other 2D shapes by translation, rotation and reflection and by combinations of these transformations <sup>(3)</sup> ;	
	f. recognise that these transformations preserve length and angle, and hence that any figure is congruent to its image under any of these transformations;	
	g. understand that enlargements are specified by a centre;	
	h. describe transform and produce enlargements of shapes using positive scale factors;	
	<ul> <li>understand from this that any two circles and any two squares are mathematically similar, while, in general, two rectangles are not;</li> </ul>	
	j. distinguish properties that are preserved under particular transformations;	
	<ul> <li>k. identify the scale factor of an enlargement as the ratio of the lengths of any two corresponding line segments and apply this to triangles;</li> </ul>	
	I. enlarge shapes using positive fractional and negative scale factors.	

H1O Vectors		Notes and Examples
1. Use vectors	Candidates should be able to:	
	a. understand and use vector notation for translations;	
	b. solve simple geometrical problems using vector methods;	
	c. use vector methods to construct geometrical arguments.	

H1P Area and volume		Notes and Examples
1. Perimeter, area and volume	Candidates should be able to:	
	a. find areas of rectangles, recalling the formula, understanding the connection to counting squares and how it extends this approach;	
	b. find the area of a parallelogram and a triangle;	
	c. calculate perimeters and areas of shapes made from triangles and rectangles;	
	d. work out the surface area of simple shapes composed of triangles and rectangles;	
	e. find volumes of cuboids, recalling the formula.	



H1Q Probability		Notes and Examples
H1Q Probability 1. Probability	<ul> <li>Candidates should be able to: <ul> <li>a. understand and use the vocabulary of probability<sup>(1)</sup> and the probability scale<sup>(2)</sup>;</li> <li>b. understand and use theoretical models of probabilities including the model of equally likely outcomes;</li> <li>c. understand and use estimates of probability from relative frequency;</li> <li>d. use sample spaces<sup>(3)</sup> for situations where outcomes are single events and for situations where outcomes are two successive events;</li> <li>e. identify different mutually-exclusive and exhaustive outcomes and know that the sum of the probabilities of these outcomes is 1<sup>(4)</sup>;</li> <li>f. understand that if they repeat an experiment, they may (and usually will) get different outcomes, and that increasing sample size generally leads to better estimates of probability;</li> <li>g. compare experimental data to theoretical probabilities<sup>(5)</sup>, and make informal inferences about the validity of the model giving rise to the theoretical probabilities;</li> <li>h. know when to add or multiply probabilities: <ul> <li>if A and B are mutually exclusive, then the probability of A or B occurring is P(A) + P(B)<sup>(6)</sup>;</li> <li>if A and B are independent events, the probability of A and B occurring is P(A) × P(B)<sup>(7)</sup>;</li> </ul> </li> </ul></li></ul>	<ul> <li>Notes and Examples</li> <li>(1) Use impossible, certain, evens, likely, unlikely.</li> <li>(2) Associate 0, 0.5, 1 with impossible, evens and certain and position events on a probability scale.</li> <li>(3) Use a sample space or list combinations systematically for 2 dice.</li> <li>(4) Given the P(A) find P(not A), and given P(A) and P(B) find P(not A or B).</li> <li>(5) Compare the dice experiment results to theoretical and comment on possible bias.</li> <li>(6) Probability of winning a match is 0.4. Probability of drawing is 0.3. Find probability of getting two sixes.</li> <li>(8) There are 7 black and 4 white discs in a bag. Two are selected at random. Find the probability of getting one of each colour.</li> </ul>
	<ul> <li>i. use tree diagrams to represent outcomes of compound events, recognising when events are independent or dependent<sup>(8)</sup>;</li> <li><i>j. understand and use set notation to describe events and compound events;</i></li> </ul>	
	<i>k. use Venn diagrams to represent the number of possibilities and hence find probabilities;</i>	



## 2.5 Content – Higher Tier – Unit B392/02

H2A General problem solving	ı skills	Notes and Examples
These skills should underpin ar	nd influence the learning experiences of all candidates in mathematics. They will be ass	sessed within this specification.
1. Solve problems using mathematical skills	Candidates should be able to:	
	a. select and use suitable problem solving strategies and efficient techniques to solve numerical problems;	
	b. identify what further information may be required in order to pursue a particular line of enquiry and give reasons for following or rejecting particular approaches;	
	c. break down a complex calculation into simpler steps before attempting to solve it and justify their choice of methods;	
	d. use notation and symbols correctly and consistently within a problem;	
	e. use a range of strategies to create numerical representations of a problem and its solution; move from one form of representation to another in order to get different perspectives on the problem;	
	f. interpret and discuss numerical information presented in a variety of forms;	
	g. present and interpret solutions in the context of the original problem;	
	h. review and justify their choice of mathematical presentation;	_
	i. understand the importance of counter-example and identify exceptional cases when solving problems;	
	j. show step-by-step deduction in solving a problem;	
	k. recognise the importance of assumptions when deducing results; recognise the limitations of any assumptions that are made and the effect that varying those assumptions may have on the solution to a problem.	



H2B Number		Notes and Examples
1. Approximate to a	Candidates should be able to:	
specified or appropriate degree of accuracy	a. use their previous understanding of integers and place value to deal with arbitrarily large positive numbers;	(1) Round 345·46 to the nearest integer, 1 decimal place, 2 significant figures.
	<ul> <li>b. use a variety of checking procedures, including working the problem backwards, and considering whether a result is of the right order of magnitude;</li> </ul>	(2) Know that 3.5 on a calculator means 3.50 in money context.
	<ul> <li>c. round to the nearest integer, to any number of decimal places, specified or appropriate, and to any number of significant figures<sup>(1)</sup>;</li> </ul>	(3) Know that 3.666666667 on a calculator is a recurring decimal.
	<ul> <li>d. give solutions in the context of the problem to an appropriate degree of accuracy, interpreting the solution shown on a calculator display, and recognising limitations on the accuracy of data and measurements;</li> </ul>	
	e. understand the calculator display <sup>(2)</sup> , knowing when to interpret the display <sup>(3)</sup> , when the display has been rounded by the calculator, and not to round during the intermediate steps of a calculation.	
2. Use calculators	Candidates should be able to:	
effectively and	a. use calculators effectively and efficiently for simple calculations <sup>(1)</sup>	(1) $1 \cdot 6^3$ , $\sqrt{7 \cdot 29}$ .
trigonometrical functions	b. perform a calculation involving division by a decimal (up to <b>two</b> decimal places);	(2) $\sqrt[3]{6 \cdot 1^2 - 0 \cdot 81}$ .
	c. know how to enter complex calculations and use function keys for reciprocals, squares and powers <sup>(2)</sup> ;	(3) When using money interpret a calculator display of 2.6 as £2.60.
	d. know how to calculate with numbers expressed in standard index form, and be able to interpret calculator displays of such numbers;	(4) $\frac{5 \times \sin 35}{\sin 62}$ .
	e. perform a range of calculations <sup>(3)</sup> ;	
	f. use an extended range of function keys, including trigonometrical <sup>(4)</sup> functions.	

(43)



H2C Hierarchy of operations		Notes and Examples
1. Hierarchy of operations	Candidates should be able to:	
	a. understand and use number operations and the relationships between them, including inverse operations.	• Calculate $\frac{(6+8)^2}{2 \cdot 5^2 - 1 \cdot 5^2}$ .

H2D Ratio		Notes and Examples
1. Use ratio notation, including reduction to its simplest form and its various links to fraction notation	Candidates should be able to:	
	a. use ratio notation, including reduction to its simplest form expressed as 1: <i>n</i> or <i>n</i> :1 or <i>m</i> : <i>n</i> <sup>(1)</sup> ;	(1) Write the ratio 24:60 in its simplest form.
	b. know and use the links between ratio notation and fraction notation.	
2. Divide a quantity in a	Candidates should be able to:	
given ratio	a. divide a quantity in a given ratio <sup>(1)</sup> ;	(1) Divide £120 in the ratio 3:7.
	<ul> <li>b. determine the original quantity by knowing the size of one part of the divided quantity;</li> </ul>	(2) 8 calculators cost £59·52. How much do 3 calculators cost?
	c. solve word problems about ratio, including using informal strategies and the unitary method of solution <sup>(2)</sup> .	

(44)



H2E Fractions, decimals and percentages		Notes and Examples
1. Calculate with fractions	Candidates should be able to:	
	a. perform short division to convert a simple fraction to a decimal;	
	b. multiply and divide a fraction by an integer and by a unit fraction;	
	c. understand and use unit fractions as multiplicative inverses;	
	d. use efficient methods to calculate with fractions, including cancelling common factors before carrying out a calculation;	
	e. recognise that, in some cases, only a fraction can express the exact answer;	
	f. understand 'reciprocal' as multiplicative inverse and know that any non-zero number multiplied by its reciprocal is 1 (and that zero has no reciprocal, since division by zero is not defined).	
2. Relationship between fractions and decimals	Candidates should be able to:	
	a. recognise that recurring decimals are exact fractions <sup>(1)</sup> ;	(1) $0.137 = \frac{137}{999}$
	b. know that some exact fractions are recurring decimals;	(2) Convert 0.3 to a fraction.
	c. convert a recurring decimal to a fraction <sup>(2)</sup> .	





H2E Fractions, decimals and percentages		Notes and Examples
3. Understand percentage	Candidates should be able to:	
	a. understand that 'percentage' means 'number of parts per 100' and use this to compare proportions;	
	b. know the fraction to percentage (or decimal) conversion of familiar simple fractions.	
4. Interpret fractions,	Candidates should be able to:	
decimals and	a. interpret percentage as the operator 'so many hundredths of';	(1) A 15% decrease in Y is
percentages as operators	b. convert between fractions, decimals and percentages;	calculated as $0.85 \times Y$ .
	c. understand the multiplicative nature of percentages as operators;	(2) £5000 invested at 4%
	d. use multipliers for percentage change <sup>(1)</sup> ;	<ul> <li>(3) Given that a meal in a restaurant costs £136 with VAT at 17.5%, its price before VAT is calculated as £136/1·175.</li> </ul>
	e. work with repeated percentage change <sup>(2)</sup> ;	
	f. solve reverse percentage problems <sup>(3)</sup> .	
5. Proportional change	Candidates should be able to:	
	a. find proportional change using fractions, decimals and percentages <sup>(1)</sup> ;	(1) 5 books cost £23·50, find
	b. understand and use direct <sup>(2)</sup> and inverse proportion <sup>(3)</sup> ;	the cost of 3 books; foreign
	c. set up and use equations to solve problems involving inverse proportion;	best value for money problems.
	d. understand and use repeated proportional change.	(2) $y \propto a x^2$ and $x = 4$ when $y = 8$ . Find y when $x = 12$ .
		(2) A tank can be emptied using 6 pumps in 18 hours. How long will it take to empty the tank using 8 pumps?

(46)



H2F Algebra		Notes and Examples
1. Symbols and notation	Candidates should be able to:	
	a. distinguish the different roles played by letter symbols in algebra, using the correct notational conventions for multiplying or dividing by a given number;	(1) $x^2 + 1 = 82$ . (2) $(x + 1)^2 = x^2 + 2x + 1$ for all values
	<ul> <li>know that letter symbols represent definite unknown numbers in equations<sup>(1)</sup>, defined quantities or variables in formulae and general, unspecified independent numbers in identities<sup>(2)</sup>;</li> </ul>	of x. (3) $y = 2 - 7x$ ; $y = \frac{1}{x}$ with $x \neq 0$ . f (x) notation may be used.
	c. know that in functions, letter symbols define new expressions or quantities by referring to known quantities <sup>(3)</sup> .	
2. Algebraic terminology	Candidates should be able to:	
	a. distinguish in meaning between the words 'equation', 'inequality', 'formula', 'identity' and 'expression'.	
3. Proof	Candidates should be able to:	
l	a. use algebra to support and construct arguments and to construct proofs.	

H2G Coordinates		Notes and Examples
1. Use the conventions for	Candidates should be able to:	
coordinates in the plane	a. given the coordinates of the points A and B, find coordinates of the midpoint of the line segment AB;	
	b. given the coordinates of the points A and B, find the length of AB.	

(47)

H2H Sequences and formulae		Notes and Examples
<ol> <li>Derive a formula, substitute numbers into a formula and change the subject of a formula</li> </ol>	Candidates should be able to:         a. substitute numbers into a formula <sup>(1)</sup> ;         b. derive a formula <sup>(2)</sup> ;         c. change the subject of a formula <sup>(3)</sup> .	<ul> <li>(1) For area of a parallelogram, volume of a prism.</li> <li>(2) Wage earned = hours worked × rate per hour.</li> <li>(3) Find <i>r</i> given that <i>C</i> = π<i>r</i>, find <i>x</i> given <i>y</i> = <i>mx</i> + <i>c</i>.</li> </ul>
2. Generate terms of a sequence using term- to-term and position-to- term definitions of the sequence	<ul> <li>Candidates should be able to:</li> <li>a. generate terms of a sequence using term-to-term and position-to-term<sup>(1)</sup> definitions of the sequence;</li> <li>b. generate common integer sequences (including sequences of odd or even integers, squared integers, powers of 2, powers of 10, triangular numbers).</li> </ul>	(1) Write down the first two terms of the sequence whose <i>n</i> th term is $3n - 5$ .
3. Form linear expressions to describe the <i>n</i> th term of an arithmetic sequence	<ul><li>Candidates should be able to:</li><li>a. use linear expressions to describe the <i>n</i>th term of an arithmetic sequence, justifying its form by referring to the activity or context from which it was generated.</li></ul>	Foundation also includes simple sequence of odd or even numbers, squared integers and sequences derived from diagrams.
4. Form quadratic expressions to describe the <i>n</i> th term of a sequence	Candidates should be able to: a. form quadratic expressions to describe the <i>n</i> th term of a sequence.	-

(48)

H2I Linear equations		Notes and Examples
1. Set up and solve	Candidates should be able to:	
inequalities	a. set up simple inequalities;	
inequalities	b. solve simple inequalities by transforming both sides in the same way;	
	c. solve linear equations that require prior simplification of brackets and/or fractions, including those that have negative signs occurring anywhere in the equation, and those with a negative solution;	
	d. understand that the point of intersection of <b>two</b> different lines in the same <b>two</b> variables that simultaneously describe a real situation is the solution to the simultaneous equations represented by the lines.	

H2J Algebraic manipulati	ion	Notes and Examples
1. Manipulate algebraic expressions	Candidates should be able to:	
	a. set up and use equations that describe direct and indirect proportion;	(1) Expand (2x – 5) (x + 7).
	b. expand the product of <b>two</b> linear expressions <sup>(1)</sup> ;	(2) Factorise 4x <sup>2</sup> – 9.
	c. factorise quadratic expressions including the difference of <b>two</b> squares <sup>(2)</sup> and simplifying rational expressions <sup>(3)</sup> ;	(3) Simplify $\frac{x^2 + 3x + 2}{x^2 - 4x - 5}$
	<ul> <li>d. solve quadratic equations exactly by factorising, completing the square and using the formula;</li> </ul>	
	e. set up and solve simultaneous equations in <b>two</b> unknowns, where one of the equations might include squared terms in one or both unknowns.	

H2K Functions and graphs		Notes and Examples
1. Solve quadratic equations	Candidates should be able to:	
using a graph	a. understand that approximate solutions of quadratic equations can be found from their graphs;	Solve $3x^2 + 4 = 8$ from graph of $y = 3x^2 + 4$ .
	b. draw graphs of quadratic equations and find their approximate solutions.	
2. Recognise and use	Candidates should be able to:	
equivalence in numerical, algebraic and graphical representations	a. recognise that straight line graphs can be represented by equations, and vice versa.	
3. Functions	Candidates should be able to:	
	a. draw, sketch and recognise graphs of linear, quadratic and simple cubic functions <sup>(1)</sup> , the reciprocal function $y = 1/x$ with $x \neq 0$ , the function $y = k^x$ for integer values of $x$ and simple positive values of $k$ , and the trigonometric functions $y = \sin x$ , $y = \cos x$ , and $y = \tan x^{(2)}$ ;	<ul> <li>(1) Draw the graph of <i>y</i> = <i>x</i><sup>3</sup> - 5<i>x</i> + 2 for - 3 ≤ <i>x</i> ≤ 3.</li> <li>(2) Sketch the graph of (a) <i>y</i> = 2sin<i>x</i> and (b) <i>y</i> = cos(<i>x</i> - 90°).</li> </ul>
	b. construct the graphs of simple loci;	
	c. sketch simple transformations of a given function;	
	d. understand and use the Cartesian equation of a circle centred at the origin and link to the trigonometric functions.	

(50)



H2L Pythagoras in 2D and 3I	)	Notes and Examples
1. Use Pythagoras' theorem	Candidates should be able to:	
	a. understand, recall and use Pythagoras' theorem to solve simple cases in 2D;	(1) Find the length of the 'body'
	b. use Pythagoras' theorem to solve more complex cases in 2D;	diagonal in a cuboid.
	c. use Pythagoras' theorem to calculate lengths in three dimensions <sup>(1)</sup> ;	
	d. use Pythagoras' theorem in 3D contexts.	

H2M Angles and properties of shape		Notes and Examples
1. Lines and angles	Candidates should be able to:	
	a. distinguish between lines and line segments;	
	b. use parallel lines, alternate angles and corresponding angles;	
	<ul> <li>c. understand the consequent properties of parallel and intersecting lines, triangles (including a proof that the angle sum of a triangle is 180°) and parallelograms;</li> </ul>	
	d. understand a proof that an exterior angle of a triangle is equal to the sum of the interior angles at the other two vertices;	
	e. explain why the angle sum of a quadrilateral is 360°.	
2. Congruence and similarity	Candidates should be able to:	
	a. understand congruence;	
	b. understand similarity of plane figures including the relationship between lengths, areas and volumes.	





H2M Angles and properti	es of shapes	Notes and Examples
3. Angles and polygons	Candidates should be able to:	
	a. calculate and use the sums of the interior and exterior angles of polygons;	
	b. calculate and use the angles of regular polygons;	
	c. solve problems in the context of tiling patterns and tessellations.	
4. Understand and use	Candidates should be able to:	
midpoint and intercept theorems	a. understand and use midpoint and intercept theorems.	
5. Proof	Candidates should be able to:	
	a. understand and construct geometrical proofs using formal arguments, including proving the congruence, or non-congruence, of two triangles in all possible cases.	



H2N Area and volume		Notes and Examples
1. Perimeter, area (including circles), and volume	<ul> <li>Candidates should be able to:</li> <li>a. solve problems involving areas;</li> <li>b. find circumferences of circles and areas enclosed by circles<sup>(1)</sup>, recalling relevant formulae;</li> <li>c. calculate volumes of right prisms<sup>(2)</sup> and of shapes made from cubes and cuboids;</li> <li>d. use <i>π</i> in exact calculations;</li> <li>e. calculate volumes of objects made from pyramids, prisms and spheres<sup>(3)</sup>;</li> <li>f. calculate the lengths of arcs and the areas of sectors of circles<sup>(4)</sup>;</li> <li>g. solve problems involving more complex shapes and solids, including segments of circles and frustums of cones<sup>(5)</sup>.</li> </ul>	<ul> <li>(1) Could involve semicircles, and inverse problems e.g. find the diameter if the circumference is 60cm.</li> <li>(2) Could involve inverse calculations – find the length of an edge given the volume and two other edges.</li> <li>(3) Calculate the volume of a sphere of radius 1.5cm.</li> <li>(4) Calculate the arc length of the sector of a circle radius 5cm subtended by an angle of 65°.</li> <li>(5) A cone is 20cm high and has a base radius of 12cm. The top 15cm of the cone is removed. Find the volume of the remaining frustum.</li> </ul>
2. Use 2D representations of 3D shapes	Candidates should be able to: a. use 2D representations of 3D shapes, including plans and elevations.	_

H2O Trigonometry		Notes and Examples
1. Trigonometry in 2D and	Candidates should be able to:	
3D	a. understand, recall and use trigonometrical relationships in right-angled triangles <sup>(1)</sup> , and use these to solve problems, including those involving bearings;	(1) Use sin, cos and tan to find lengths and angles in right-
	b. use trigonometrical ratios to solve 2D and 3D problems;	angled and isosceles triangles.
	c. use the sine and cosine rules to solve 2D and 3D problems <sup>(2)</sup> ;	(2) Find the angle between the longest diagonal and the base of
	d. calculate the area of a triangle using $\frac{1}{2}ab\sin C$ .	a cuboid.

(53)

#### **3.1** Overview of the assessment in GCSE Methods in Mathematics

For GCSE Methods in Mathematics candidates must take both units.

Unit B391/01	•	All units are externally assessed.
<i>Methods in Mathematics 1</i> (Foundation)	•	Candidates answer <b>all</b> questions on each paper.
40% of the total GCSE marks	•	In some questions candidates have to decide for themselves what mathematics they need to use.
(non-calculator)	•	In each question paper, candidates are expected to support their answers with appropriate working.
Unit B391/02 Mothods in Mathematics 1	•	Quality of written communication (QWC) is
(Higher)		assessing QWC are indicated by an asterisk (*).
40% of the total GCSE marks 1 hour 15 mins written paper	•	Candidates are permitted to use a scientific or graphical calculator for Unit B392. All
(non-calculator) 60 marks		in the document <i>Instructions for Conducting</i> <i>Examinations</i> , published annually by the Joint
Unit B392/01		Council for Qualifications (http://www.jcq.org.uk).
Methods in Mathematics 2	•	All candidates should have the usual geometric
(Foundation)		instruments available. Tracing paper can be used
60% of the total GCSE marks		specified on the front of the question paper.
1 hour 30 mins written paper		
90 marks		
Unit B392/02		
Methods in Mathematics 2		
(Higher)		
60% of the total GCSE marks		
2 hour written paper		
90 marks		

## 3.2 Tiers

54

All written papers are set in one of two tiers: Foundation Tier and Higher Tier. Foundation Tier papers assess grades G to C and Higher Tier papers assess Grades D to A\*. An allowed grade E may be awarded on the Higher Tier components.

Candidates are entered for an option in either the Foundation Tier or the Higher Tier.

Candidates may enter for either the Foundation Tier or Higher Tier in each of the externally assessed units. So, a candidate may take, for example B391/F and B392/H.

## **3.3** Assessment Objectives (AOs)

Candidates are expected to demonstrate their ability to:

		Assessment Objectives	Weighting (%)
AO1	•	recall and use their knowledge of the prescribed content	50-60
AO2	•	select and apply mathematical methods	15-25
AO3	•	interpret and analyse problems and use mathematical reasoning to solve them	20-30

## AO weightings – GCSE Methods in Mathematics

The relationship between the units and the assessment objectives in terms of **raw marks** is shown in the following grid:

llait	G	Total		
Onit	AO1	AO2	AO3	TOLAI
Unit B391/01: <i>Methods in</i> <i>Mathematics 1 (Foundation)</i>	30-36	9-15	12-18	60
Unit B391/02: <i>Methods in</i> <i>Mathematics 1 (Higher)</i>	30-36	9-15	12-18	60
Unit B392/01: <i>Methods in</i> <i>Mathematics 2 (Foundation)</i>	45-54	13-23	18-27	90
Unit B392/02: <i>Methods in</i> <i>Mathematics 2 (Higher)</i>	45-54	13-23	18-27	90

55)



## **3.4 Grading and awarding grades**

GCSE results are awarded on the scale A\* to G. Units are awarded a\* to g. Grades are indicated on certificates. However, results for candidates who fail to achieve the minimum grade (G or g) will be recorded as *unclassified* (U or u) and this is **not** certificated.

Most GCSEs are unitised schemes. When working out candidates' overall grades OCR needs to be able to compare performance on the same unit in different series when different grade boundaries may have been set, and between different units. OCR uses a Uniform Mark Scale to enable this to be done.

A candidate's uniform mark for each unit is calculated from the candidate's raw mark on that unit. The raw mark boundary marks are converted to the equivalent uniform mark boundary. Marks between grade boundaries are converted on a pro rata basis.

When unit results are issued, the candidate's unit grade and uniform mark are given. The uniform mark is shown out of the maximum uniform mark for the unit, e.g. 84/120.

The specification is graded on a Uniform Mark Scale. The uniform mark thresholds for each of the assessments are shown below:

(GCSE)	Maximum Unit	Unit Grade								
Unit Weighting	Uniform Mark	a*	а	b	С	d	е	f	g	u
40% F	83				72	60	48	36	24	0
40% H	120	108	96	84	72	60	54			0
60% F	125				108	90	72	54	36	0
60% H	180	162	144	126	108	90	81			0

Higher tier candidates who fail to gain a 'd' grade may achieve an "allowed e". Higher tier candidates who miss the allowed grade 'e' will be graded as 'u'.

A candidate's uniform marks for each unit are aggregated and grades for the specification are generated on the following scale:

Qualification	Max Uniform Mark	Qualification Grade								
		<b>A</b> *	Α	В	С	D	E	F	G	U
GCSE	300	270	240	210	180	150	120	90	60	0

The written papers will have a total weighting of 100%.

The candidate's grade will be determined by the total uniform mark.

## **3.5 Grade descriptions**

Grade descriptions are provided to give a general indication of the standards of achievement likely to have been shown by candidates awarded particular grades. The descriptions must be interpreted in relation to the content in the specification; they are not designed to define that content. The grade awarded will depend in practice upon the extent to which the candidate has met the assessment objectives overall. Shortcomings in some aspects of the assessment may be balanced by better performance in others.

The grade descriptors have been produced by the regulatory authorities in collaboration with the awarding bodies.

#### Grade F

Candidates use some mathematical techniques, terminology, diagrams and symbols from the foundation tier consistently, appropriately and accurately. Candidates use some different representations effectively and can select information from them. They complete straightforward calculations competently with and without a calculator. They use simple fractions and percentages, simple formulae and some geometric properties, including symmetry.

Candidates work mathematically in everyday and meaningful contexts. They make use of diagrams and symbols to communicate mathematical ideas. Sometimes, they check the accuracy and reasonableness of their results.

Candidates test simple hypotheses and conjectures based on evidence. Candidates are able to use data to look for patterns and relationships. They state a generalisation arising from a set of results and identify counter-examples. They solve simple problems, some of which are non-routine.

#### Grade C

Candidates use a range of mathematical techniques, terminology, diagrams and symbols consistently, appropriately and accurately. Candidates are able to use different representations effectively and they recognise some equivalent representations e.g. numerical, graphical and algebraic representations of linear functions; percentages, fractions and decimals. Their numerical skills are sound and they use a calculator accurately. They apply ideas of proportionality to numerical problems and use geometric properties of angles, lines and shapes.

Candidates identify relevant information, select appropriate representations and apply appropriate methods and knowledge. They are able to move from one representation to another, in order to make sense of a situation. Candidates use different methods of mathematical communication.

Candidates tackle problems that bring aspects of mathematics together. They identify evidence that supports or refutes conjectures and hypotheses. They understand the limitations of evidence and sampling, and the difference between a mathematical argument and conclusions based on experimental evidence.

They identify strategies to solve problems involving a limited number of variables. They communicate their chosen strategy, making changes as necessary. They construct a mathematical argument and identify inconsistencies in a given argument or exceptions to a generalisation.



#### Grade A

Candidates use a wide range of mathematical techniques, terminology, diagrams and symbols consistently, appropriately and accurately. Candidates are able to use different representations effectively and they recognise equivalent representations for example numerical, graphical and algebraic representations. Their numerical skills are sound, they use a calculator effectively and they demonstrate algebraic fluency. They use trigonometry and geometrical properties to solve problems.

Candidates identify and use mathematics accurately in a range of contexts. They evaluate the appropriateness, effectiveness and efficiency of different approaches. Candidates choose methods of mathematical communication appropriate to the context. They are able to state the limitations of an approach or the accuracy of results. They use this information to inform conclusions within a mathematical or statistical problem.

Candidates make and test hypotheses and conjectures. They adopt appropriate strategies to tackle problems (including those that are novel or unfamiliar), adjusting their approach when necessary. They tackle problems that bring together different aspects of mathematics and may involve multiple variables. They can identify some variables and investigate them systematically; the outcomes of which are used in solving the problem.

Candidates communicate their chosen strategy. They can construct a rigorous argument, making inferences and drawing conclusions. They produce simple proofs and can identify errors in reasoning.

## **3.6 Quality of Written Communication**

*Quality of written communication* (QWC) is assessed in all units and is integrated in the marking criteria.

Candidates are expected to:

- ensure that text is legible and that spelling, punctuation and grammar are accurate so that meaning is clear
- present information in a form that suits its purpose
- use an appropriate style of writing and, where applicable, specialist terminology.

Questions assessing QWC are indicated by an asterisk (\*).

# **Support for GCSE Methods in Mathematics**

In order to help you implement this GCSE Methods in Mathematics specification effectively, OCR offers a comprehensive package of support. This includes:

## 4.1 Free resources available from the OCR website

The following materials will be available on the OCR website:

- GCSE Methods in Mathematics specification
- <u>specimen assessment materials for each unit</u>
- sample schemes of work and lesson plans

Additional sample assessment materials for each unit can be found on OCR Interchange.

#### 4.2 Training

OCR will offer a range of support activities for practitioners throughout the lifetime of the qualification to ensure they have the relevant knowledge and skills to deliver the qualification.

Please see Event Booker for further information.

### 4.3 OCR support services

4.3.1 Active Results

# activeresults

Active Results is available to all centres offering OCR's GCSE Mathematics specifications.

Active Results is a free results analysis service to help teachers review the performance of individual candidates or whole schools.

Data can be analysed using filters on several categories such as gender and other demographic information, as well as providing breakdowns of results by question and topic.

Active Results allows you to look in greater detail at your results:

- Richer and more granular data will be made available to centres including question level data available from e-marking
- You can identify the strengths and weaknesses of individual candidates and your centre's cohort as a whole
- Our systems have been developed in close consultation with teachers so that the technology delivers what you need.

Further information on Active Results can be found on the OCR website.

#### **4.3.2** OCR Mathematics support team

A direct number gives access to a dedicated and trained support team handling all queries relating to GCSE Methods in Mathematics and other mathematics qualifications - 0300 456 3142.

59)



## 4.3.3 OCR Interchange

OCR Interchange has been developed to help you to carry out day-to-day administration functions online, quickly and easily. The site allows you to register and enter candidates online. In addition, you can gain immediate and free access to candidate information at your convenience. Sign up on the <u>OCR website</u>.

## **5.1 Equality Act Information relating to GCSE Methods in Mathematics**

GCSEs often require assessment of a broad range of competences. This is because they are general qualifications and, as such, prepare candidates for a wide range of occupations and higher level courses.

The revised GCSE qualification and subject criteria were reviewed by the regulators in order to identify whether any of the competences required by the subject presented a potential barrier to any disabled candidates. If this was the case, the situation was reviewed again to ensure that such competences were included only where essential to the subject. The findings of this process were discussed with disability groups and with disabled people.

Reasonable adjustments are made for disabled candidates in order to enable them to access the assessments and to demonstrate what they know and can do. For this reason, very few candidates will have a complete barrier to the assessment. Information on reasonable adjustments is found in *Access Arrangements, Reasonable Adjustments and Special Consideration* produced by the Joint Council www.jcq.org.uk.

Candidates who are unable to access part of the assessment, even after exploring all possibilities through reasonable adjustments, may still be able to receive an award based on the parts of the assessment they have taken.

	Yes/No	Type of Assessment
Readers	Yes	All assessments
Scribes	Yes	All assessments
Practical assistants	Yes	All assessments
Word processors	Yes	All assessments
Transcripts	Yes	All assessments
Oral language modifiers	Yes	All assessments
BSL signers	Yes	All assessments
Modified question papers	Yes	All assessments
Extra time	Yes	All assessments

The access arrangements permissible for use in this specification are in line with Ofqual's GCSE subject criteria equalities review and are as follows:

## 5.2 Arrangements for candidates with particular requirements

All candidates with a demonstrable need may be eligible for access arrangements to enable them to show what they know and can do. The criteria for eligibility for access arrangements can be found in the JCQ document *Access Arrangements, Reasonable Adjustments and Special Consideration*.

Candidates who have been fully prepared for the assessment but who have been affected by adverse circumstances beyond their control at the time of the examination may be eligible for special consideration. As above, centres should consult the JCQ document *Access Arrangements, Reasonable Adjustments and Special Consideration*.

## **Administration of GCSE Methods in Mathematics**

The sections below explain in more detail the rules that apply from the June 2014 examination series onwards.

#### 6.1 Availability of assessment from 2014

There will be:

- one examination series available each year in June to all candidates
- one re-take opportunity available in November each year for candidates in GCSE Mathematics with any awarding body.

	Unit B391	Unit B392	Certification availability
June 2014	$\checkmark$	$\checkmark$	$\checkmark$
November 2014	Re-take only	Re-take only	Re-take only
June 2015	$\checkmark$	$\checkmark$	$\checkmark$
November 2015	Re-take only	Re-take only	Re-take only

#### 6.2 Certification rules

For GCSE Methods in Mathematics, a 100% terminal rule applies. Candidates must enter for all their units in the series in which the qualification is certificated.

#### 6.3 Rules for re-taking a qualification

Candidates may enter for the qualification an unlimited number of times.

Where a candidate re-takes a qualification, **all** units must be re-entered and all units must be re-taken in the same series as the qualification is re-certificated. The new results for these units will be used to calculate the new qualification grade. Any results previously achieved cannot be re-used.

#### 6.4 Making entries

#### 6.4.1 Unit entries

Centres must be approved to offer OCR qualifications before they can make any entries, including estimated entries. It is recommended that centres apply to OCR to become an approved centre well in advance of making their first entries. Centres must have made an entry for a unit in order for OCR to supply the appropriate forms and administrative materials.

It is essential that correct unit entry codes are used when making unit entries.

For units B391 and B392 candidates must be entered for either component 01 (Foundation Tier) or 02 (Higher Tier) using the appropriate unit entry code from the table below. It is not possible for a candidate to take both components for a particular unit within the same series; however, different units

may be taken at different tiers.

## 6.4.2 Certification entries

Candidates must be entered for qualification certification separately from unit assessment(s). If a certification entry is **not** made, no overall grade can be awarded.

Candidates must enter for:

• GCSE Methods in Mathematics certification code J926.

#### 6.5 Enquiries about results

Under certain circumstances, a centre may wish to query the result issued to one or more candidates.

Unit entry code	Component code	Assessment method	Unit titles
B391F	01	Written Paper	Methods in Mathematics 1 (Foundation Tier)
B391H	02	Written Paper	<i>Methods in Mathematics 1</i> (Higher Tier)
B392F	01	Written Paper	Methods in Mathematics 2 (Foundation Tier)
B392H	02	Written Paper	Methods in Mathematics 2 (Higher Tier)

Enquiries about results for GCSE units must be made immediately following the series in which the relevant unit was taken and by the relevant enquiries about results deadline for that series.

Please refer to the JCQ *Post-Results Services* booklet and the OCR *Admin Guide:* 14–19 *Qualifications* for further guidance on enquiries about results and deadlines. Copies of the latest versions of these documents can be obtained from the <u>OCR website</u>.

## 6.6 **Prohibited qualifications and classification code**

Every specification is assigned a national classification code indicating the subject area to which it belongs. The classification code for this specification is 2214.

Centres should be aware that candidates who enter for more than one GCSE qualification with the same classification code will have only one grade (the highest) counted for the purpose of the School and College Performance Tables.

Centres may wish to advise candidates that, if they take two specifications with the same classification code, colleges are very likely to take the view that they have achieved only one of the two GCSEs. The same view may be taken if candidates take two GCSE specifications that have different classification codes but have significant overlap of content. Candidates who have any doubts



about their subject combinations should seek advice, either from their centre or from the institution to which they wish to progress.

## 7.1 Overlap with other qualifications

There is a small degree of overlap between the content of this specification and those for GCSE Statistics and Free Standing Mathematics Qualifications.

There is a significant overlap with the single GCSE in Mathematics.

## **7.2 Progression from this qualification**

GCSE qualifications are general qualifications which enable candidates to progress either directly to employment, or to proceed to further qualifications.

Progression to further study from GCSE will depend upon the number and nature of the grades achieved. Broadly, candidates who are awarded mainly Grades D to G at GCSE could either strengthen their base through further study of qualifications at Level 1 within the National Qualifications Framework or could proceed to Level 2. Candidates who are awarded mainly Grades A\* to C at GCSE would be well prepared for study at Level 3 within the National Qualifications Framework.

This specification provides progression from the Entry Level Certificate in Mathematics specification R448.

#### 7.3 Avoidance of bias

OCR has taken great care in preparation of this specification and assessment materials to avoid bias of any kind. Special focus is given to the 9 strands of the Equality Act with the aim of ensuring both direct and indirect discrimination is avoided.

## 7.4 **Regulatory requirements**

This specification complies in all respects with the current: *General Conditions of Recognition; GCSE, GCE, Principal Learning and Project Code of Practice and the GCSE subject criteria for Methods in Mathematics*. All documents are available on the <u>Ofqual website</u>.

#### 7.5 Language

This specification and associated assessment materials are in English only. Only answers written in English will be assessed.



## 7.6 Spiritual, moral, ethical, social, legislative, economic and cultural issues

This specification offers opportunities which can contribute to an understanding of these issues in the following topics.

Issue	Opportunities for developing an understanding of the issue during the course
Spiritual issues	Spiritual development: helping candidates obtain an insight into the infinite, and explaining the underlying mathematical principles behind natural forms and patterns.
Moral issues	Moral development: helping candidates recognise how logical reasoning can be used to consider the consequences of particular decisions and choices and helping them learn the value of mathematical truth.
Social issues	Social development: helping candidates work together productively on complex mathematical tasks and helping them see that the result is often better than any of them could achieve separately.
Economic issues	Economic development: helping candidates make informed decisions about the management of money.
Cultural issues	Cultural development: helping candidates appreciate that mathematical thought contributes to the development of our culture and is becoming increasingly central to our highly technological future, and recognising that mathematicians from many cultures have contributed to the development of modern day mathematics.

# 7.7 Sustainable development, health and safety considerations and European developments, consistent with international agreements

This specification supports these issues, consistent with current EU agreements, through questions set in relevant contexts.

Sustainable development issues could be supported through questions set on carbon emissions or life expectancy, for example.

Health and safety considerations could be supported through questions on maximum safe loads or a nutrition analysis, for example.

European developments could be supported through questions on currency and foreign exchange, for example.

OCR encourages teachers to use appropriate contexts in the delivery of the subject content.



## 7.8 Key Skills

This specification provides opportunities for the development of the Key Skills of *Communication, Application of Number, Information and Communication Technology, Working with Others, Improving Own Learning and Performance and Problem Solving* at Levels 1 and/or 2. However, the extent to which this evidence fulfils the Key Skills criteria at these levels will be totally dependent on the style of teaching and learning adopted.

The following table indicates where opportunities may exist for at least some coverage of the various Key Skills criteria at Levels 1 and/or 2.

	С		C AoN		οN	ICT		WwO		loLP		PS	
	1	2	1	2	1	2	1	2	1	2	1	2	
J926	$\checkmark$												

### 7.9 ICT

In order to play a full part in modern society, candidates need to be confident and effective users of ICT. Where appropriate, candidates should be given opportunities to use ICT in order to further their study of mathematics.

The assessment of this course requires candidates to:

- Use calculators effectively and efficiently, knowing how to
  - enter complex calculations
  - use an extended range of function keys, including trigonometrical and statistical functions relevant to the programme of study.

Questions will be set in Unit B392 that will specifically test the use of calculators.

In addition, the programme of study requires candidates to:

Become familiar with a range of resources, including ICT such as spreadsheets, dynamic geometry, graphing software and calculators, to develop mathematical ideas.

## 7.10 Citizenship

From September 2002, the National Curriculum for England at Key Stage 4 includes a mandatory programme of study for Citizenship.

The key process of **critical thinking and enquiry** can be developed, for example, where candidates have to decide for themselves how to solve a mathematical problem, or decide which information is relevant and redundant.



#### **Your checklist**

Our aim is to provide you with all the information and support you need to deliver our specifications.



Bookmark www.ocr.org.uk/gcse2012

Be among the first to hear about support materials and resources as they become available. Register for email updates at **www.ocr.org.uk/updates** 

Book your inset training place online at

www.ocreventbooker.org.uk

Learn more about active results at

www.ocr.org.uk/activeresults

Join our social network community for teachers at www.social.ocr.org.uk

#### **Need more help?**

Here's how to contact us for specialist advice: Phone: 0300 456 3142 Email: maths@ocr.org.uk Online: http://answers.ocr.org.uk Fax: 01223 552627 Post: Customer Contact Centre, OCR, Progress House, Westwood Business Park, Coventry CV4 8JQ

## What to do next

Become an approved OCR centre – if your centre is completely new to OCR and has not previously used us for any examinations, visit **www.ocr.org.uk/centreapproval** to become an approved OCR centre.

# **OCR Mathematics support team**

IN

JOW

If you'd like to find out more about our Mathematics qualifications, please call our dedicated and trained mathematics support team on **0300 456 3142** 

TOUCH

They are available from 8am–5.30pm, Monday – Friday. You can also email us at maths@ocr.org.uk



 Telephone
 01223 553998

 Facsimile
 01223 552627

maths@ocr.org.uk 1 Hills Road, Cambridge CB1 2EU

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored. © OCR 2012 Oxford Cambridge and RSA Examinations is a Company Limited by Guarantee. Registered in England. Registered office 1 Hills Road, Cambridge CB1 2EU. Registered company number 3484466. OCR is an exempt charity.